

# Exponential functions

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# Introduction


▶  $y = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$

▶  $y = x^2$

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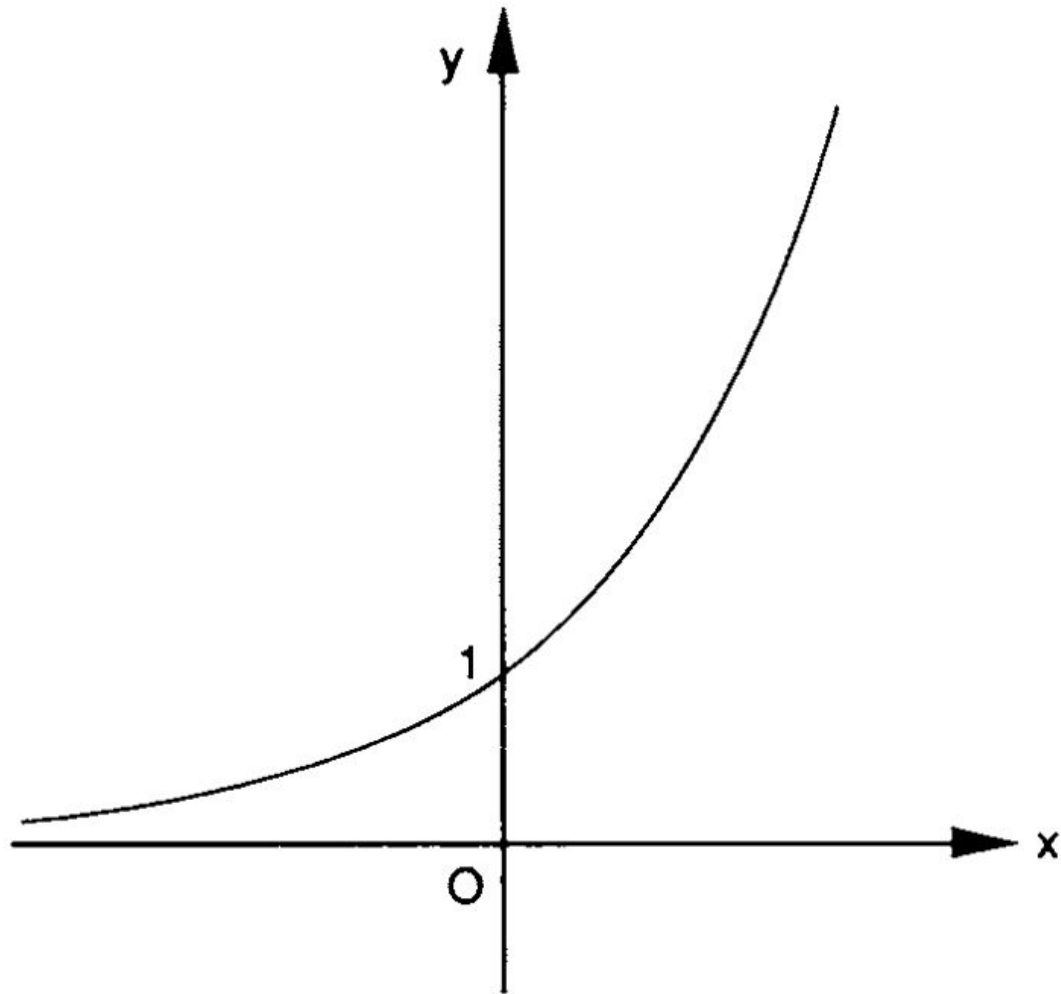


# Introduction

$$y = x^2 \xrightarrow{\text{green arrow}} y = 2^x \xrightarrow{\text{green arrow}} y = b^x$$

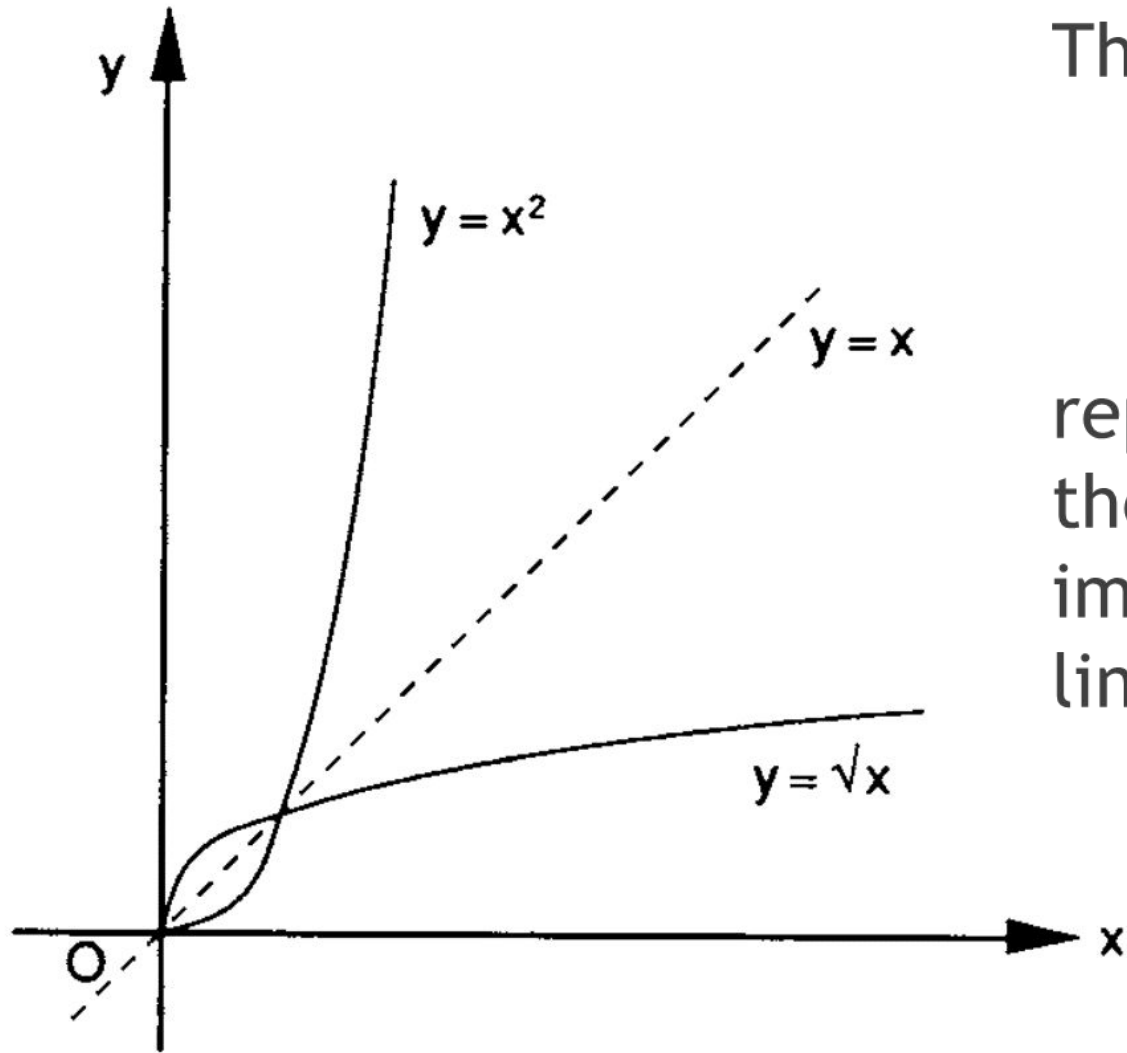
$u^v$  was introduced by Leibniz in  
1695

# Graph of the exponential function



$$y = b^x$$

# Inverse functions



The equations

$$y = x^2$$

and

$$y = \sqrt{x}$$

represent inverse functions;  
their graphs are mirror  
images of each other in the  
line  $y = x$ .

# Inverse functions

▶

$$y = b^x$$

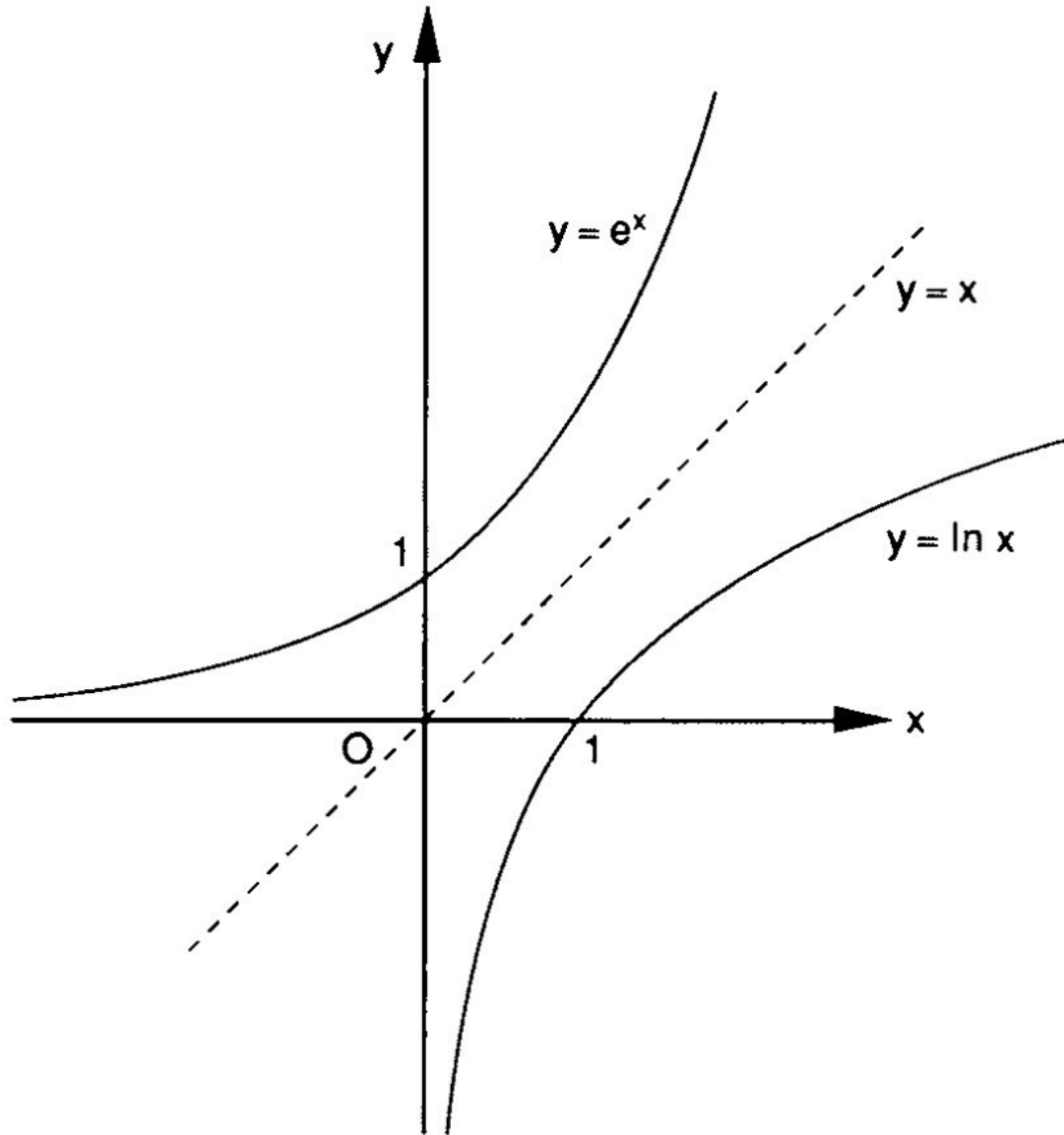


$$x = \log_b y$$

$$y = \log_b x$$

(or  $y = \ln x$  if  $b = e$ )

# Inverse functions



The equations  
 $y = e^x$   
and  
 $y = \ln x$   
represent inverse  
functions.



# Derivative of an exponential function

1.  $\frac{dy}{dx} = \lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x}, y = b^x$

2.  $\Delta y = b^{x+\Delta x} - b^x = b^x b^{\Delta x} - b^x = b^x (b^{\Delta x} - 1)$

3.  $\frac{dy}{dx} = \lim_{\Delta x \rightarrow 0} \frac{b^x (b^{\Delta x} - 1)}{\Delta x} \longrightarrow \frac{dy}{dx} = b^x \lim_{\Delta x \rightarrow 0} \frac{(b^{\Delta x} - 1)}{\Delta x}$

If  $k = \lim_{\Delta x \rightarrow 0} \frac{(b^{\Delta x} - 1)}{\Delta x}$ , then  $\frac{dy}{dx} = kb^x = ky$

# The end



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