

Comparing Means  
(Parametric tests)

One Population  
Inference

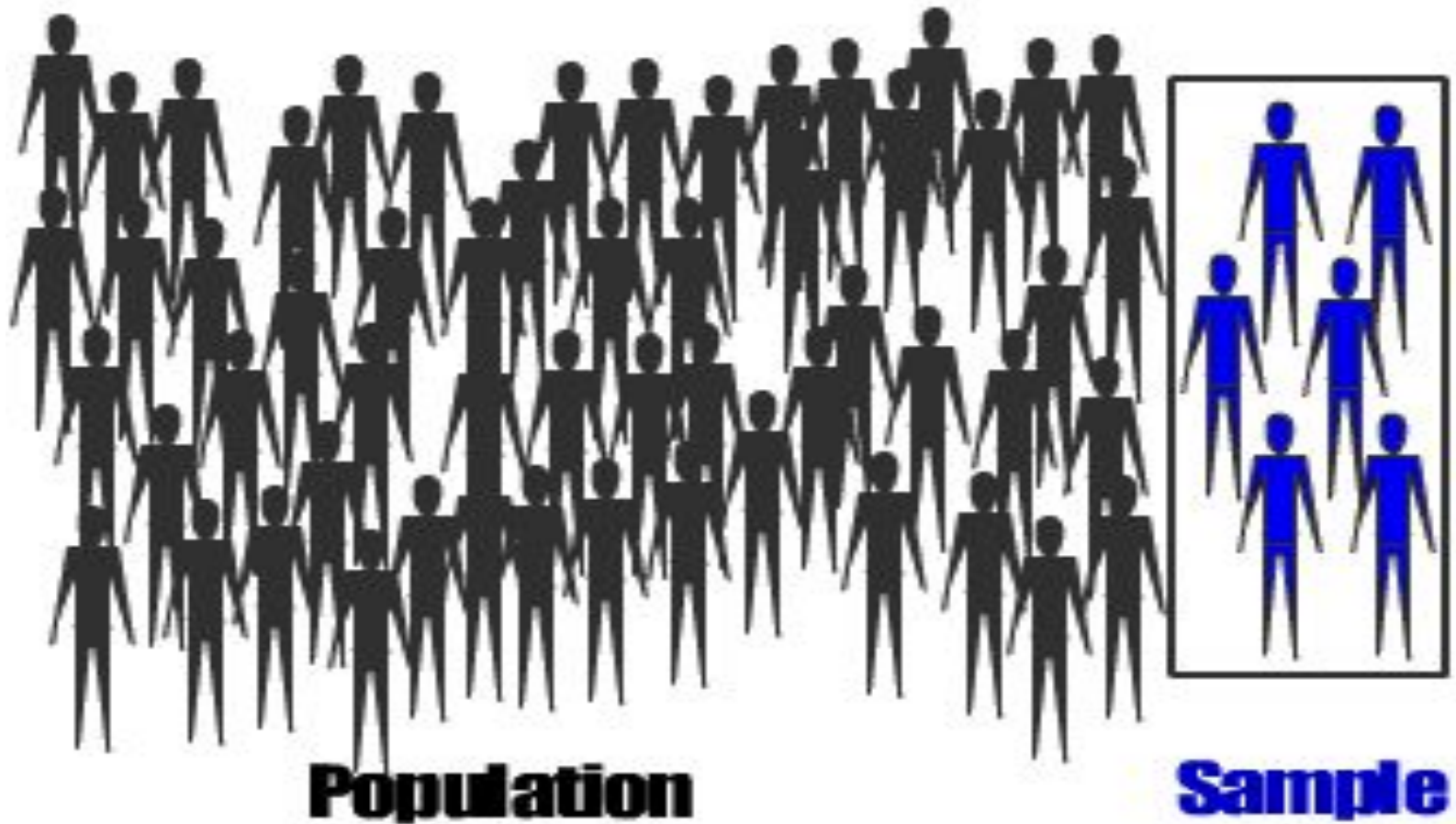
Two Population  
Inference

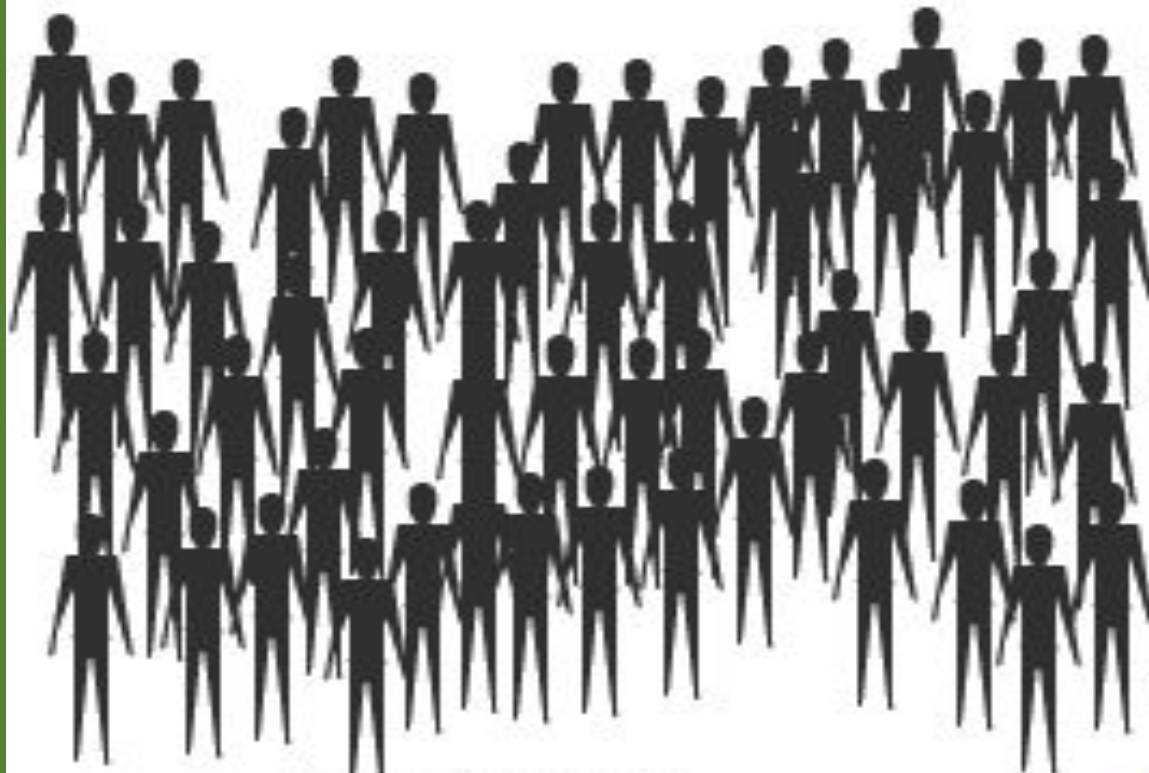
Analysis of  
Variance (ANOVA)

Independent  
Sampling Model

Dependent  
Sampling Model

**Test of population mean vs. hypothesized value,  
population standard deviation unknown**





## **Population**

**quantity (count) =  $N$**

**mean =  $\mu$**

**variance =  $\sigma^2$**

**standard deviation =  $\sigma$**



## **Sample**

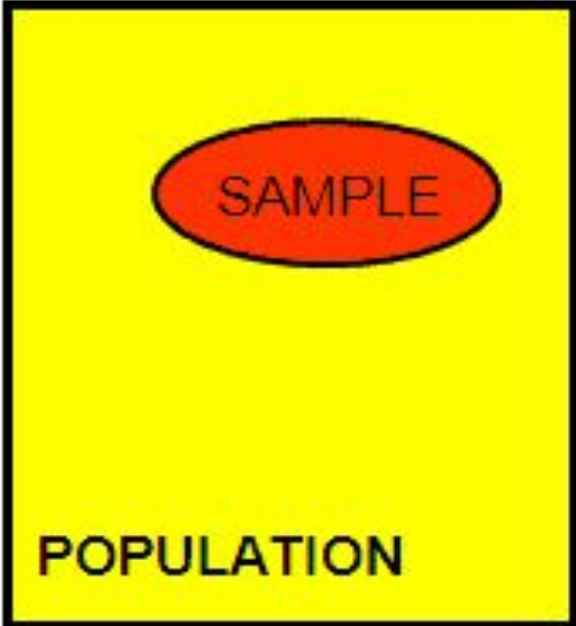
**quantity (count) =  $n$**

**mean =  $\bar{x}$**

**variance =  $s^2$**

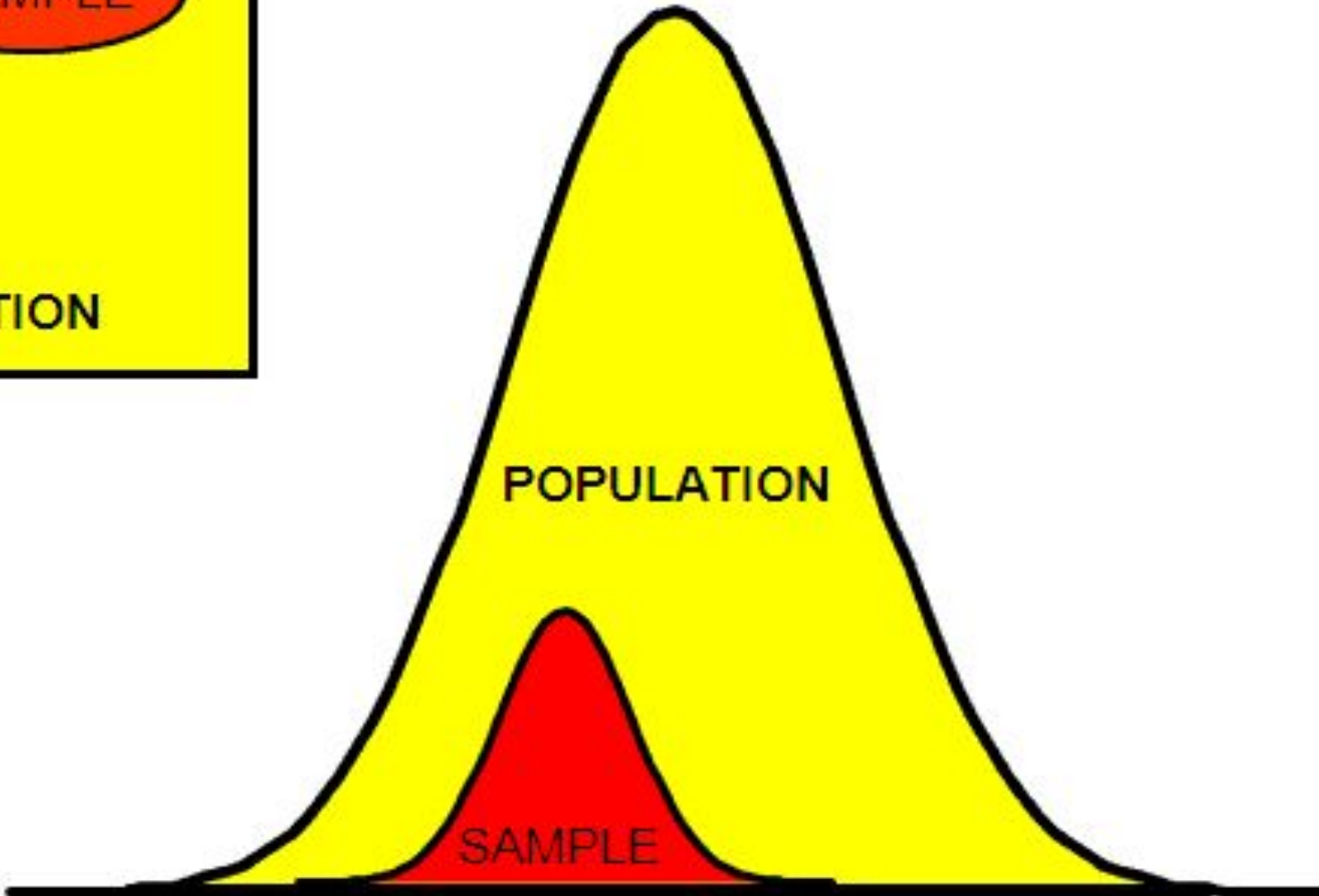
**standard deviation =  $s$**

SAMPLE



POPULATION

POPULATION



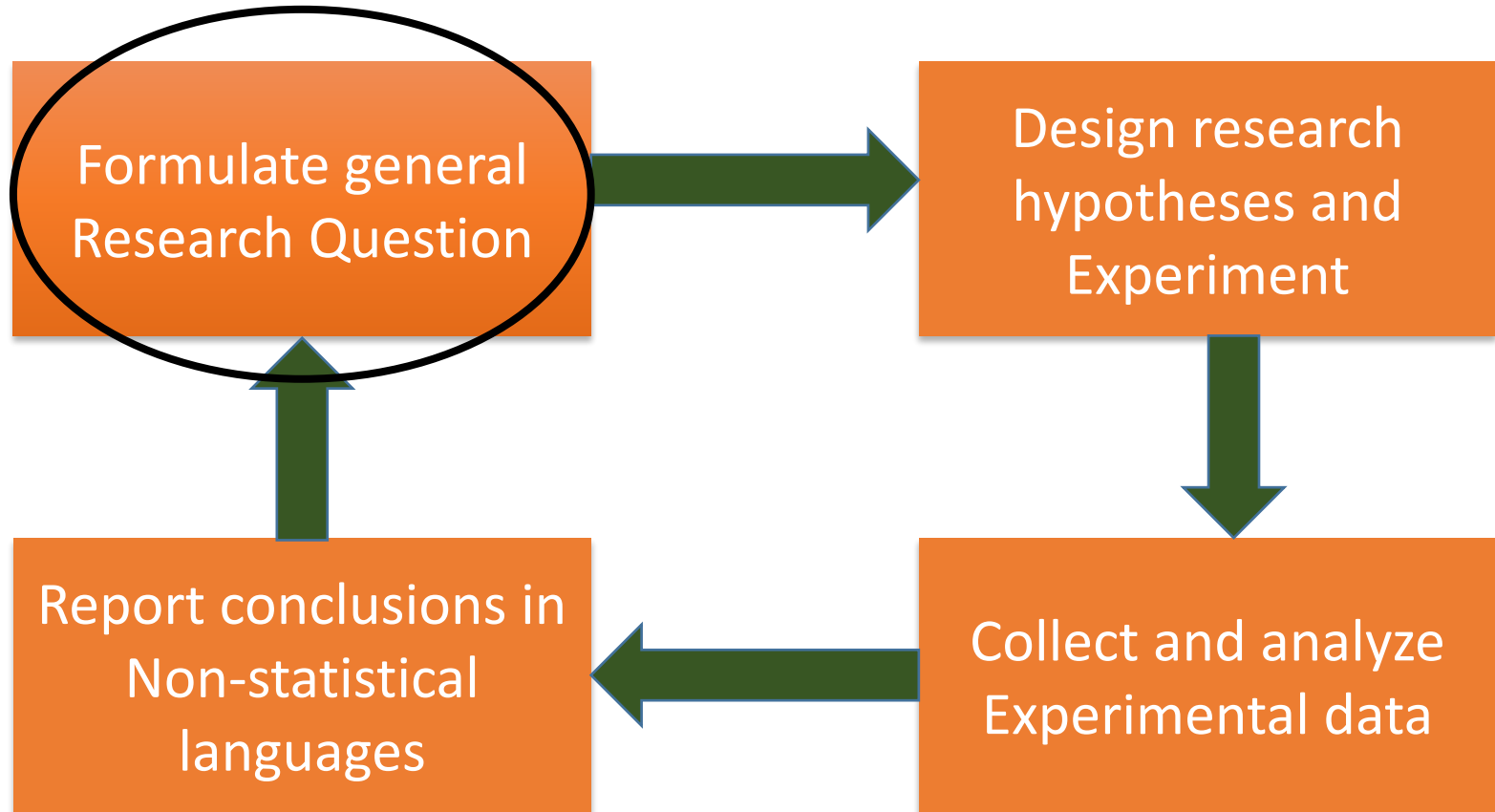
SAMPLE

# **Exercise (13)**

### Exercise (13):

It is known that the mean Haemoglobin percent (Hb%) of adult females in a community is 89%. A researcher wanted to test whether pregnancy has a significant effect on hemoglobin level. He randomly selected 25 pregnant females and conducted measurement of their Hb level. The mean Hb% for the sample was of  $86 \pm 7\%$ . The researcher selected level of significance  $\alpha = 0.05$ . The critical value at df of 24 and level of significance 0.05 is 2.064.

# Procedures of Hypotheses Testing and the Scientific Method



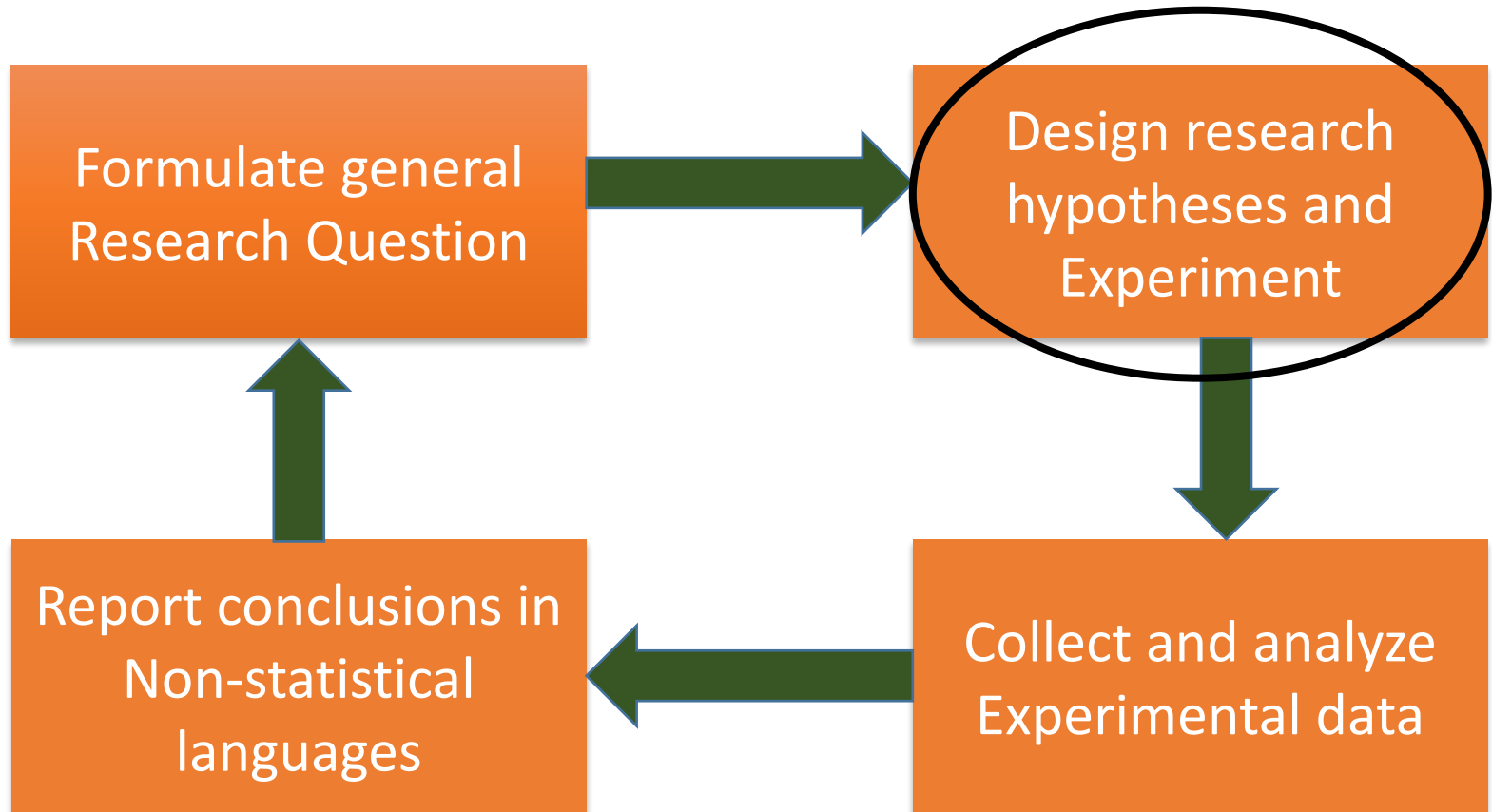
# **I. Formulate general Research Question**



## **I. Formulate general Research Question**

Does pregnancy have significant effect on mean Hb%?

# Procedures of Hypotheses Testing and the Scientific Method



**II. State Research Hypotheses**

**III. What is the appropriate test statistic?**

**IV. What is the appropriate test Model? (One or Two tailed)**

## **II. State Research Hypotheses**

Ho:  $\mu = X$  (pregnancy has no significant effect on mean Hb%)

Ho:  $\mu \neq X$  (pregnancy has significant effect on mean Hb%)

## **III. What is the appropriate test statistic?**

## **IV. What is the appropriate test Model? (One or Two tailed)**

## II. State Research Hypotheses

Ho:  $\mu = X$  (pregnancy has no significant effect on mean Hb%)

Ho:  $\mu \neq X$  (pregnancy has significant effect on mean Hb%)

## III. What is the appropriate test statistic?

One sample t test

$$t = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$$

## IV. What is the appropriate test Model? (One or Two tailed)

## II. State Research Hypotheses

Ho:  $\mu = X$  (pregnancy has no significant effect on mean Hb%)

Ho:  $\mu \neq X$  (pregnancy has significant effect on mean Hb%)

## III. What is the appropriate test statistic?

One sample t test

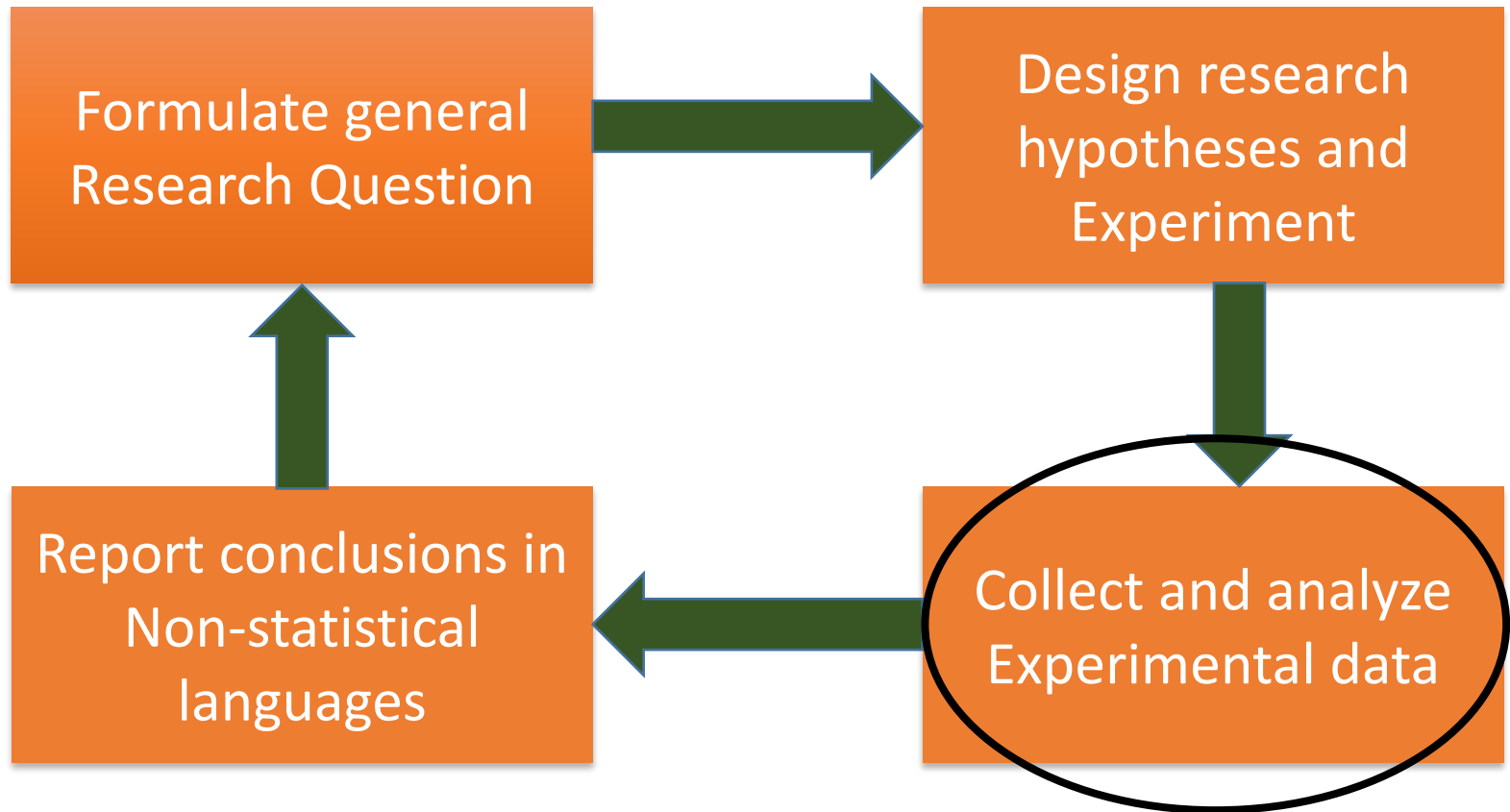
$$t = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$$

## IV. What is the appropriate test Model? (One or Two tailed)

Two Tailed Test Model

# **Design Research Hypotheses and Experiment**

# Procedures of Hypotheses Testing and the Scientific Method





**V. Calculate test statistic**

**VI. Make a Decision regarding Research Hypotheses  
(Specify the Decision Method)**

## V. Calculate test statistic

$$t = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$$

$$t = \frac{(86 - 89)}{\frac{7}{\sqrt{25}}} = 2.14$$

## VI. Make a Decision regarding Research Hypotheses (Specify the Decision Method)

## V. Calculate test statistic

$$t = \frac{\bar{X} - \mu_0}{s/\sqrt{n}}$$

$$t = \frac{(86 - 89)}{\frac{7}{\sqrt{25}}} = 2.14$$

## VI. Make a Decision regarding Research Hypotheses (Specify the Decision Method)

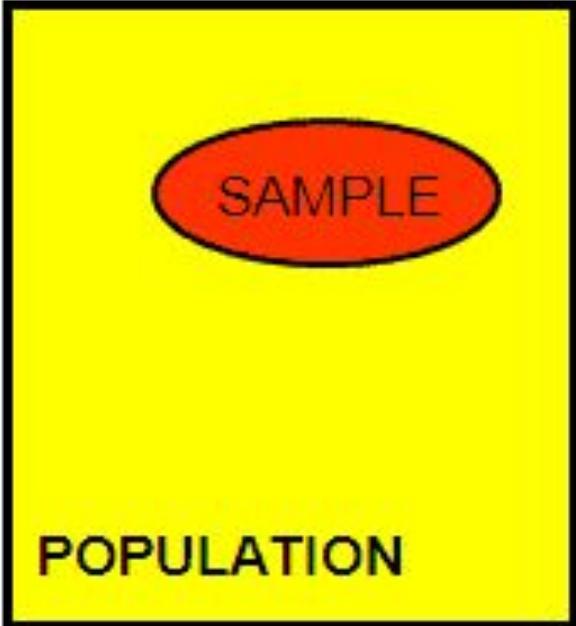
**Reject Null Hypothesis Ho**

Test statistic (t=2.14) > critical value (2.064)

(Critical value method)

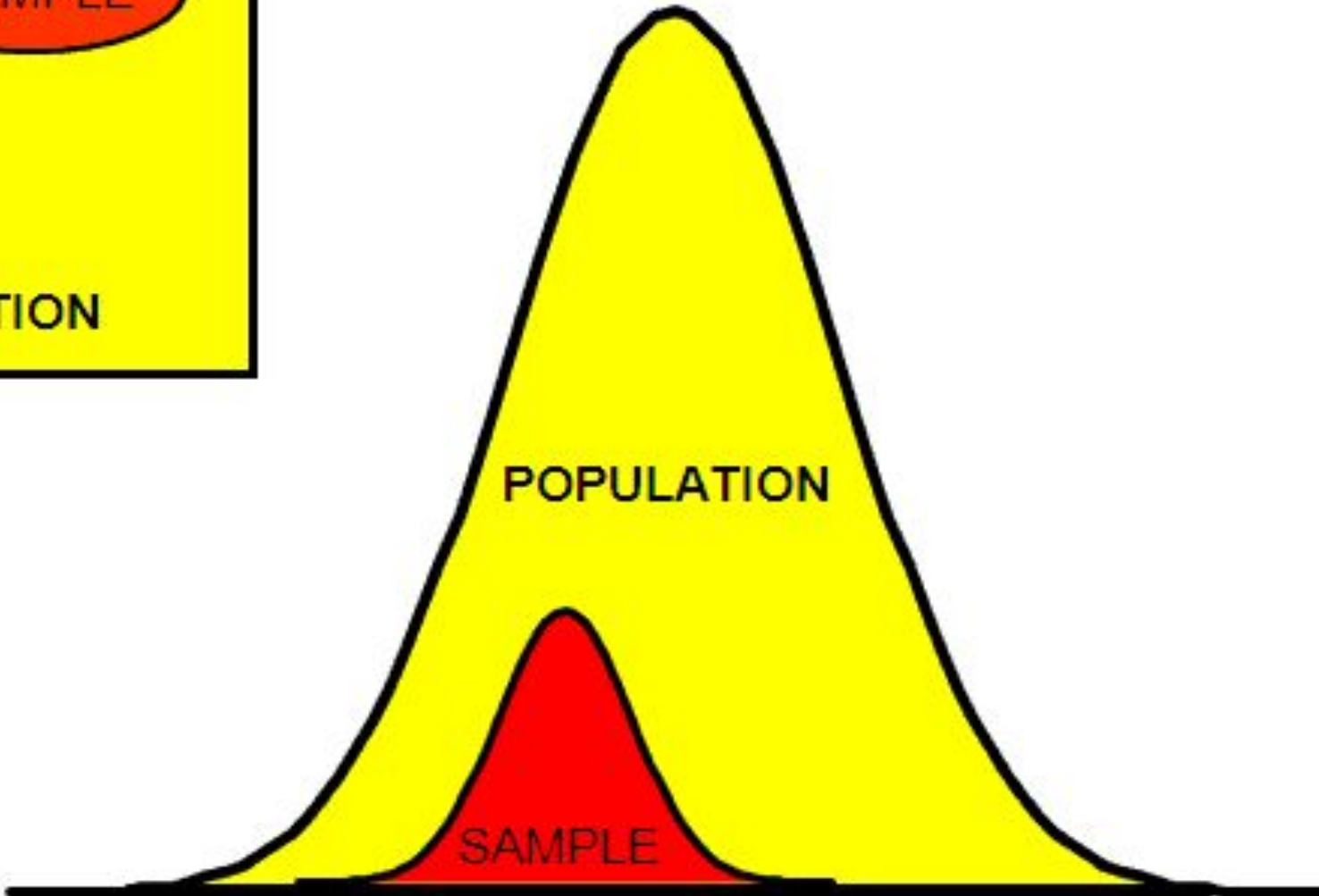
# **Collect and Analyze Experimental Data**

SAMPLE



POPULATION

POPULATION



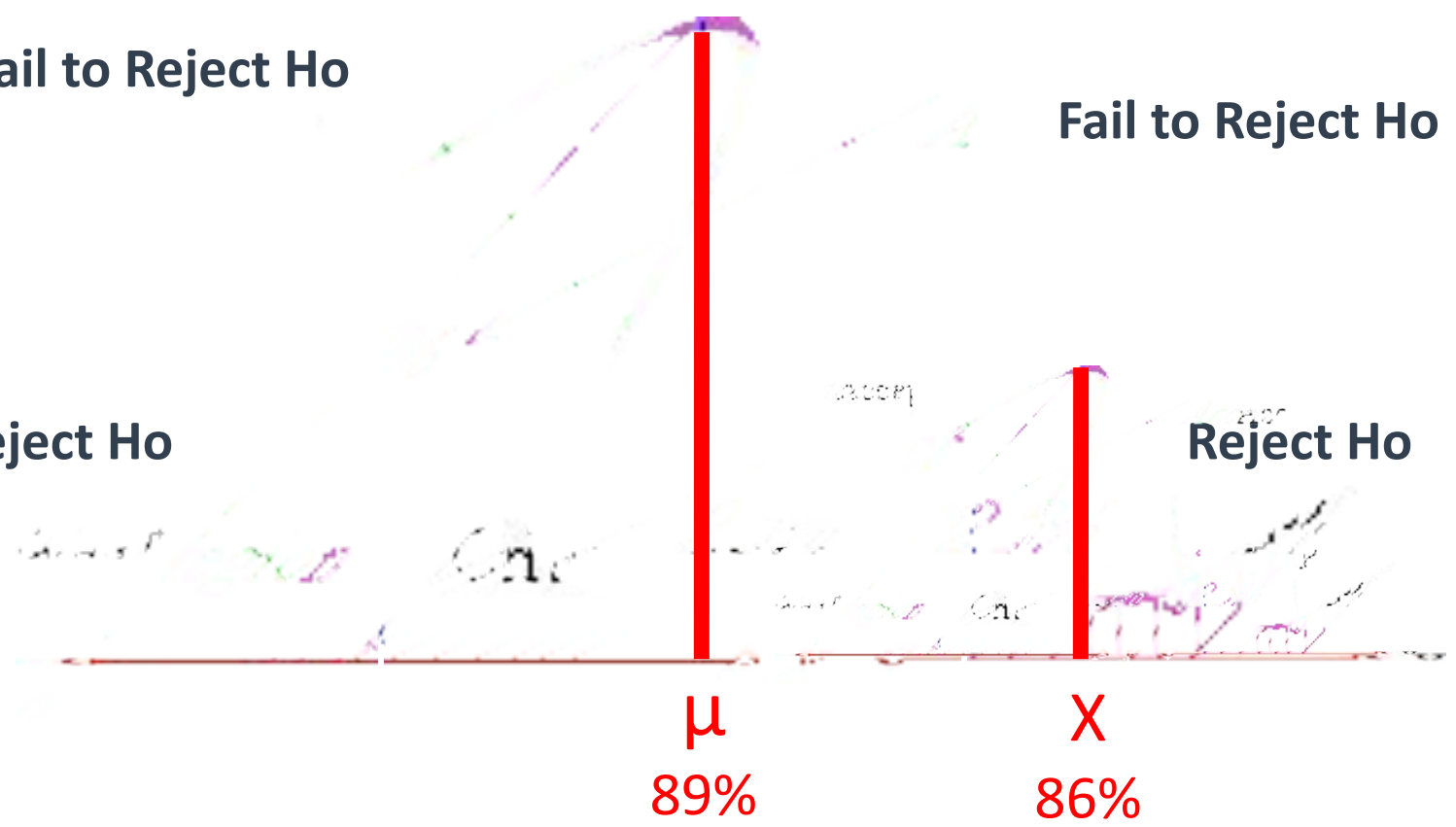
SAMPLE

Fail to Reject Ho

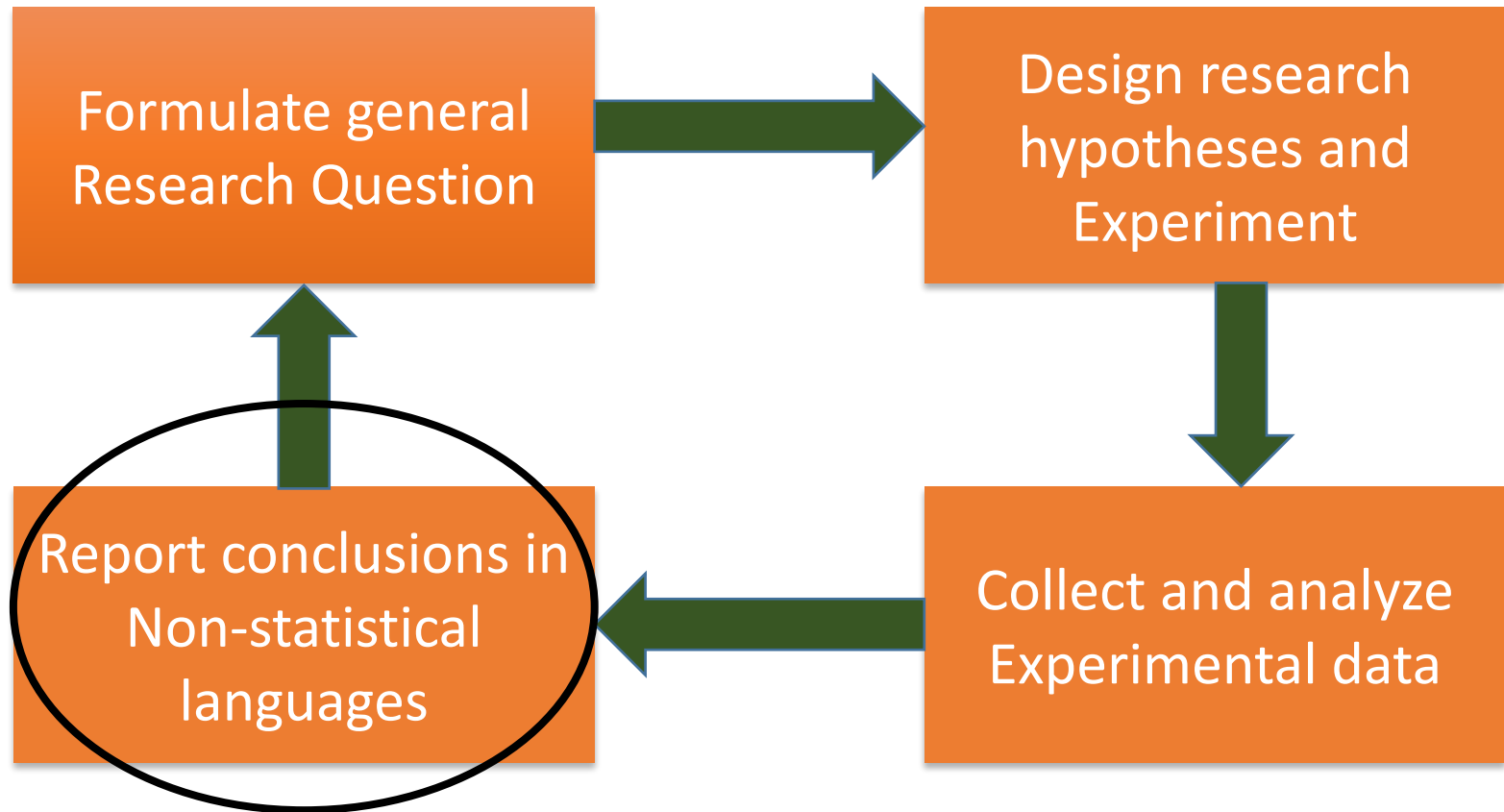
Fail to Reject Ho

Reject Ho

Reject Ho



# Procedures of Hypotheses Testing and the Scientific Method



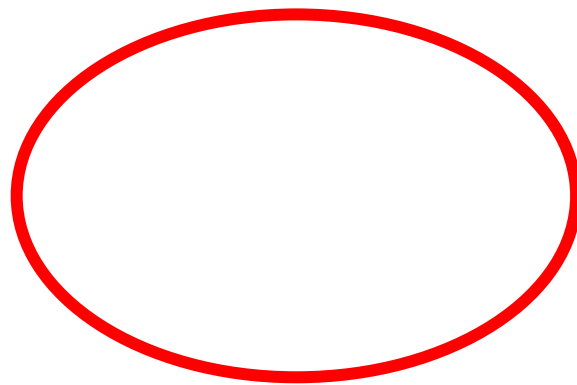
## **VII. Report a conclusion**



## VII. Report a conclusion

Pregnancy has a significant effect on mean Hb%.

The mean Hb% of pregnant females (86%) was significantly lower than the mean Hb% of adult females in the community (89%).



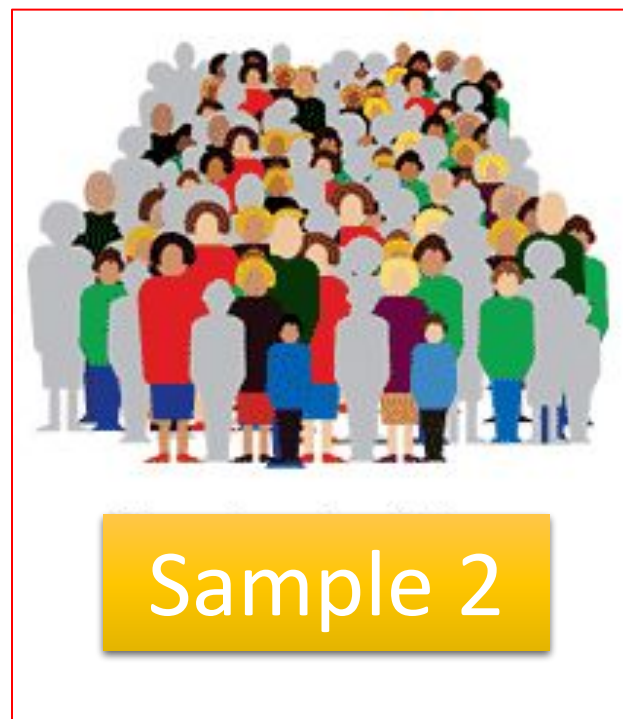
Comp  
(Par  
One P

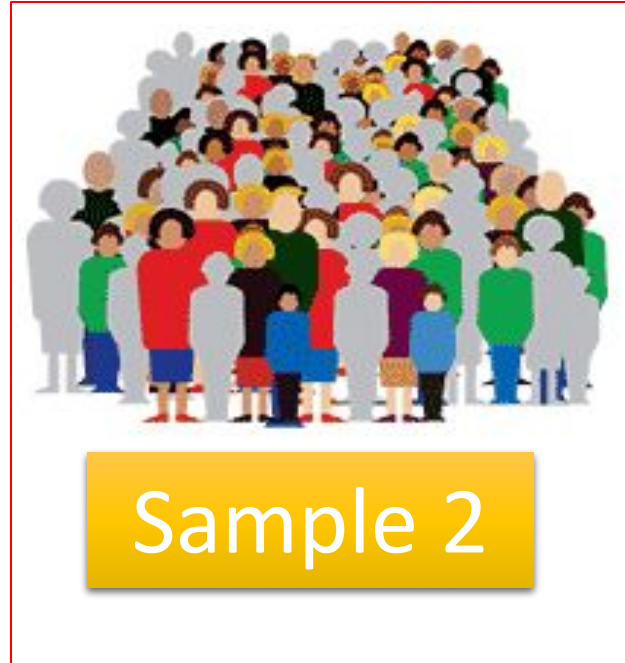
Two P  
Indep

Depe

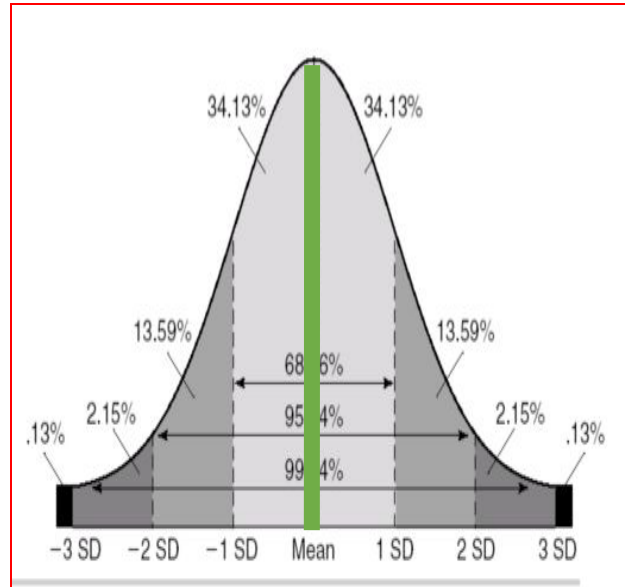
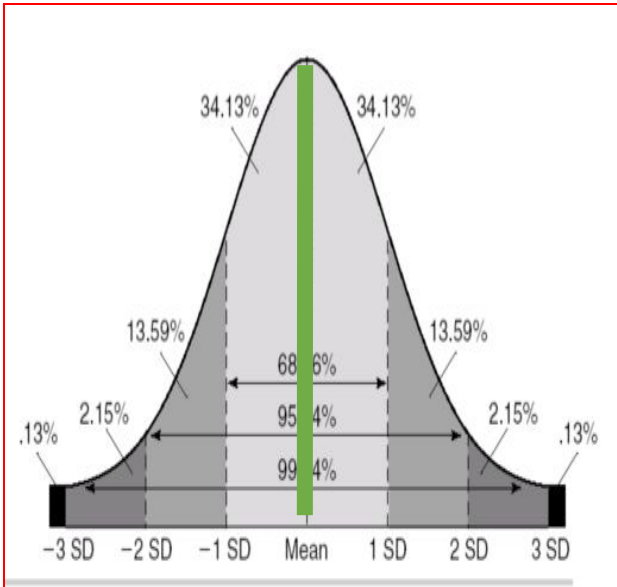
Analy

The data is collected by two **simple random samples** from **separate and unrelated populations**. This data will then be used to **compare the two population means**. This is typical of an experimental or **treatment** population versus a **control** population.





$$\frac{n_1}{X_1 S_1}$$



$$\frac{n_2}{X_2 S_2}$$

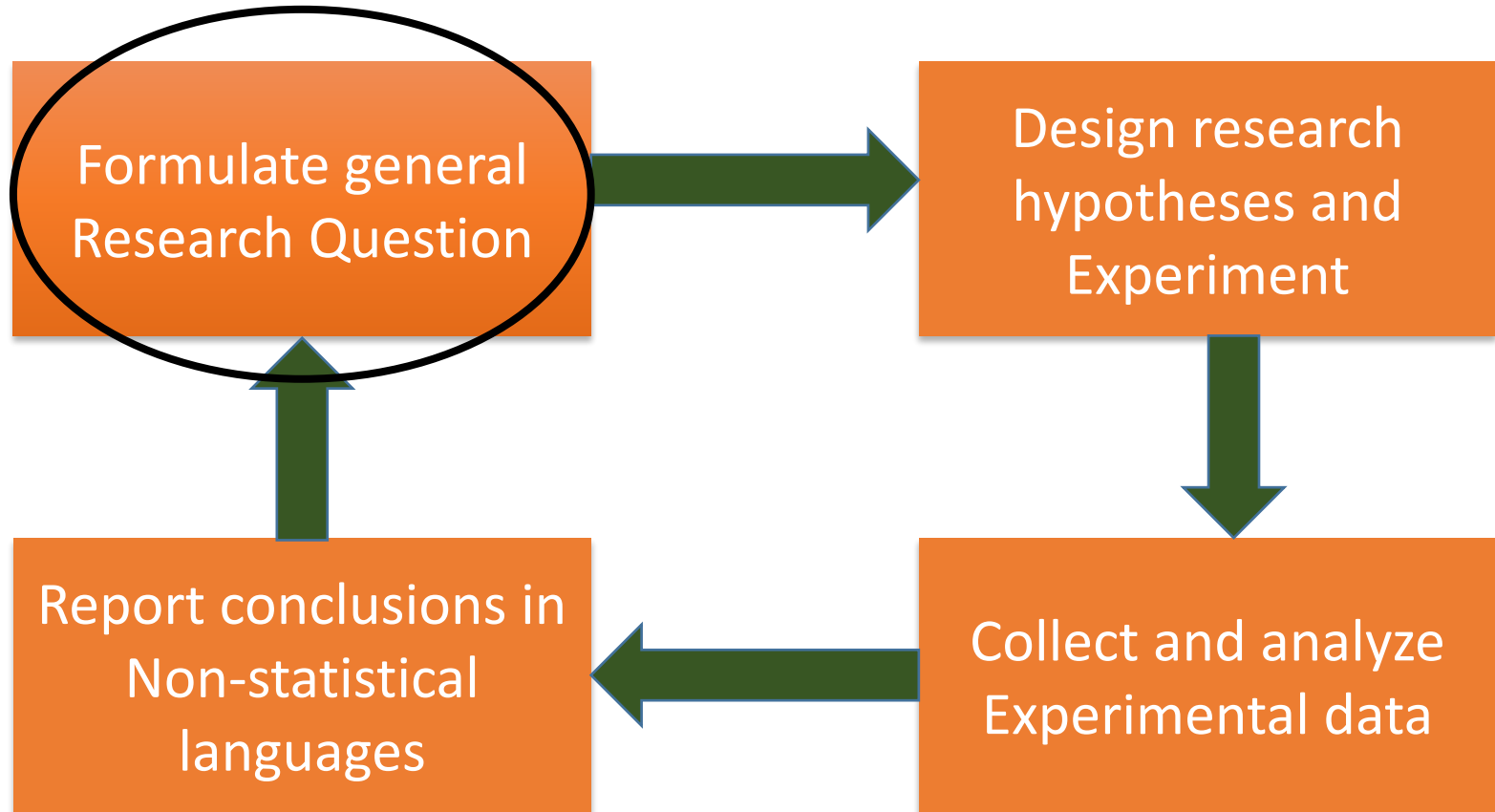
# Exercise (14)

Researchers were motivated to test a new antihypertensive drug (A) on a group of patients. They needed to know whether Drug (A) achieves significant reduction in the systolic blood pressure compared with the conventional antihypertensive drug (B).

In the current research, 200 randomly selected patients suffering from essential hypertension and fulfilled the inclusion and exclusion criteria were included. The participants were randomly allocated into two groups; 100 patients were given drug (A) and 100 were given the drug (B). The researchers selected level of significance  $\alpha = 0.05$ .

After a period of 10 weeks, the mean systolic blood pressure of the first group receiving drug (A) decreased by  $12 \pm 2.36$  mm Hg while that of the second group decreased by  $9 \pm 5.69$ . The collected data were typed onto computer and analyzed using SPSS software program. The program revealed the value of the test statistic=2.56 ( $p=0.06$ )

# Procedures of Hypotheses Testing and the Scientific Method



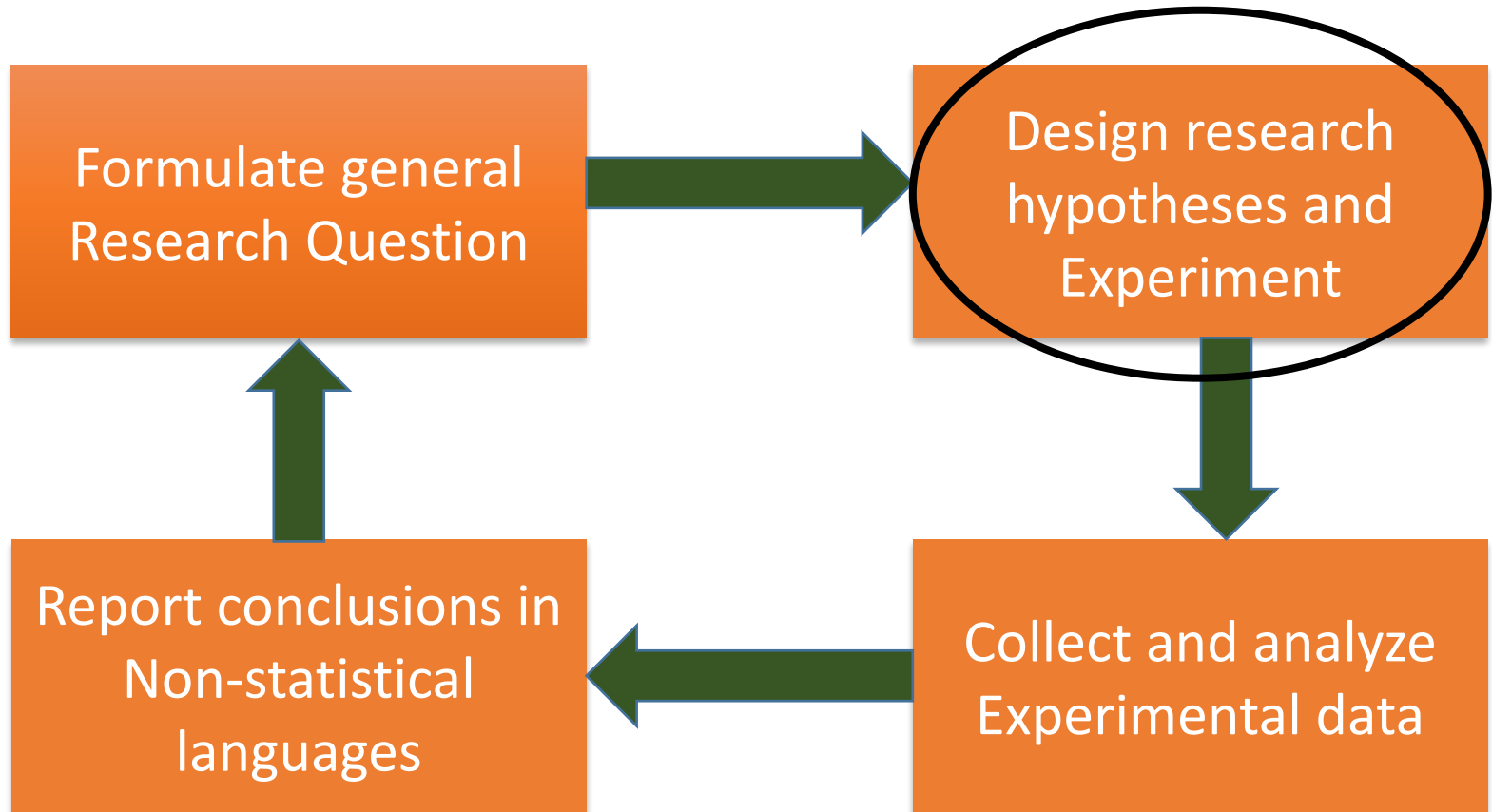
# **I. Formulate general Research Question**



## **I. Formulate general Research Question**

Is there any significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)?

# Procedures of Hypotheses Testing and the Scientific Method



## **II. State Research Hypotheses**

**III. What is the appropriate test statistic?**

**IV. What is the appropriate test Model? (One or Two tailed)**

## II. State Research Hypotheses

$$\text{Ho: } \bar{X}_1 = \bar{X}_2$$

There is no significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

$$\text{Ha: } \bar{X}_1 \neq \bar{X}_2$$

There is a significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

## III. What is the appropriate test statistic?

## IV. What is the appropriate test Model? (One or Two tailed)

## II. State Research Hypotheses

$$\text{Ho: } \bar{X}_1 = \bar{X}_2$$

There is no significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

$$\text{Ha: } \bar{X}_1 \neq \bar{X}_2$$

There is a significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

## III. What is the appropriate test statistic?

Two Independent sample t test

$$t = \frac{(\bar{X}_1 - \bar{X}_2)}{\sqrt{\frac{S^2_p}{n_1} + \frac{S^2_p}{n_2}}}$$

## IV. What is the appropriate test Model? (One or Two tailed)

## II. State Research Hypotheses

$$\text{Ho: } \bar{X}_1 = \bar{X}_2$$

There is no significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

$$\text{Ha: } \bar{X}_1 \neq \bar{X}_2$$

There is a significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)

## III. What is the appropriate test statistic?

Two Independent sample t test

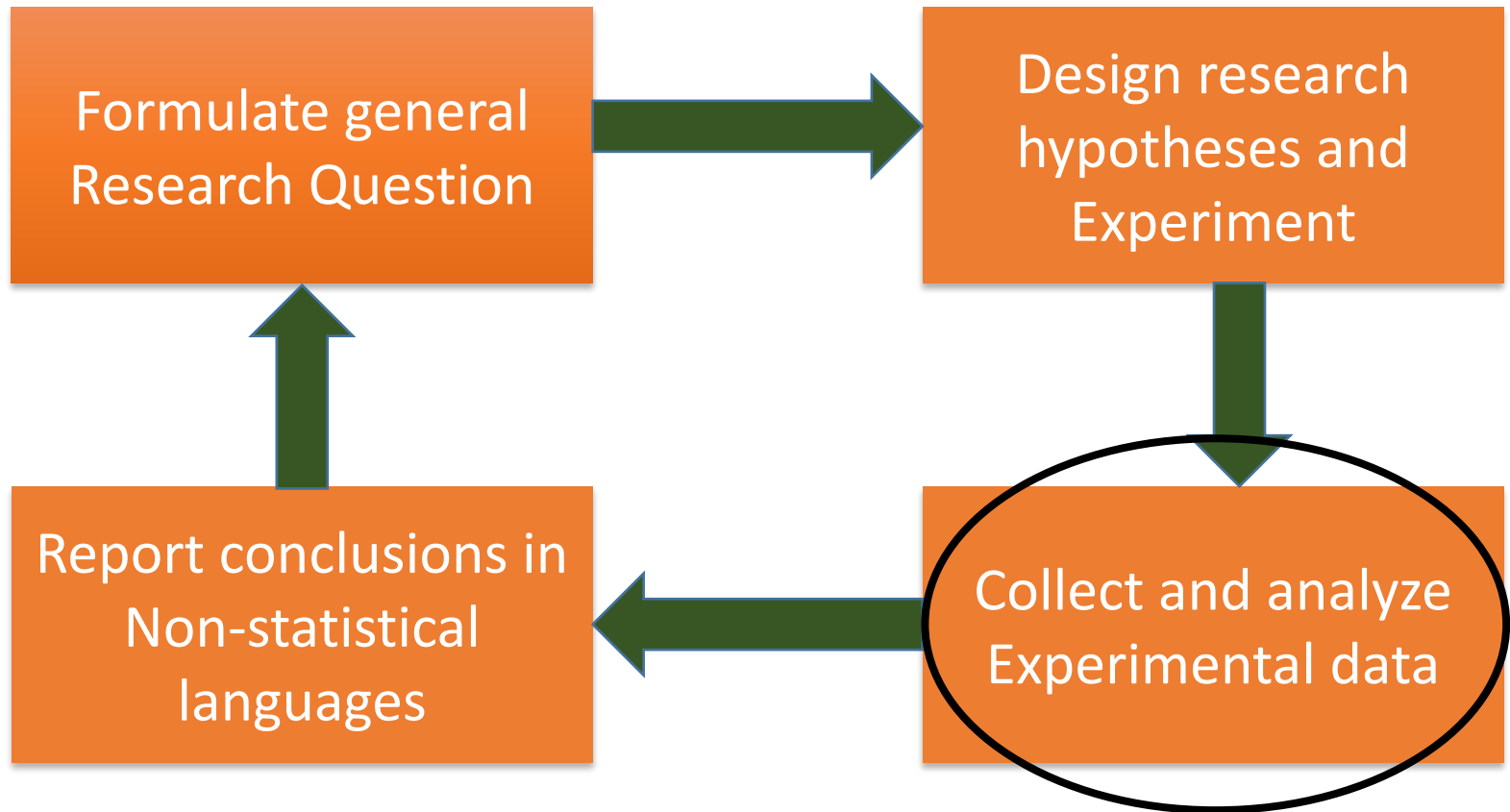
$$t = \frac{(X_1 - X_2)}{\frac{S^2p}{n_1} + \frac{S^2p}{n_2}}$$

## IV. What is the appropriate test Model? (One or Two tailed)

Two Tailed Test Model

# **Design Research Hypotheses and Experiment**

# Procedures of Hypotheses Testing and the Scientific Method





## **V. Make a Decision regarding Research Hypotheses (Specify the Decision Method)**

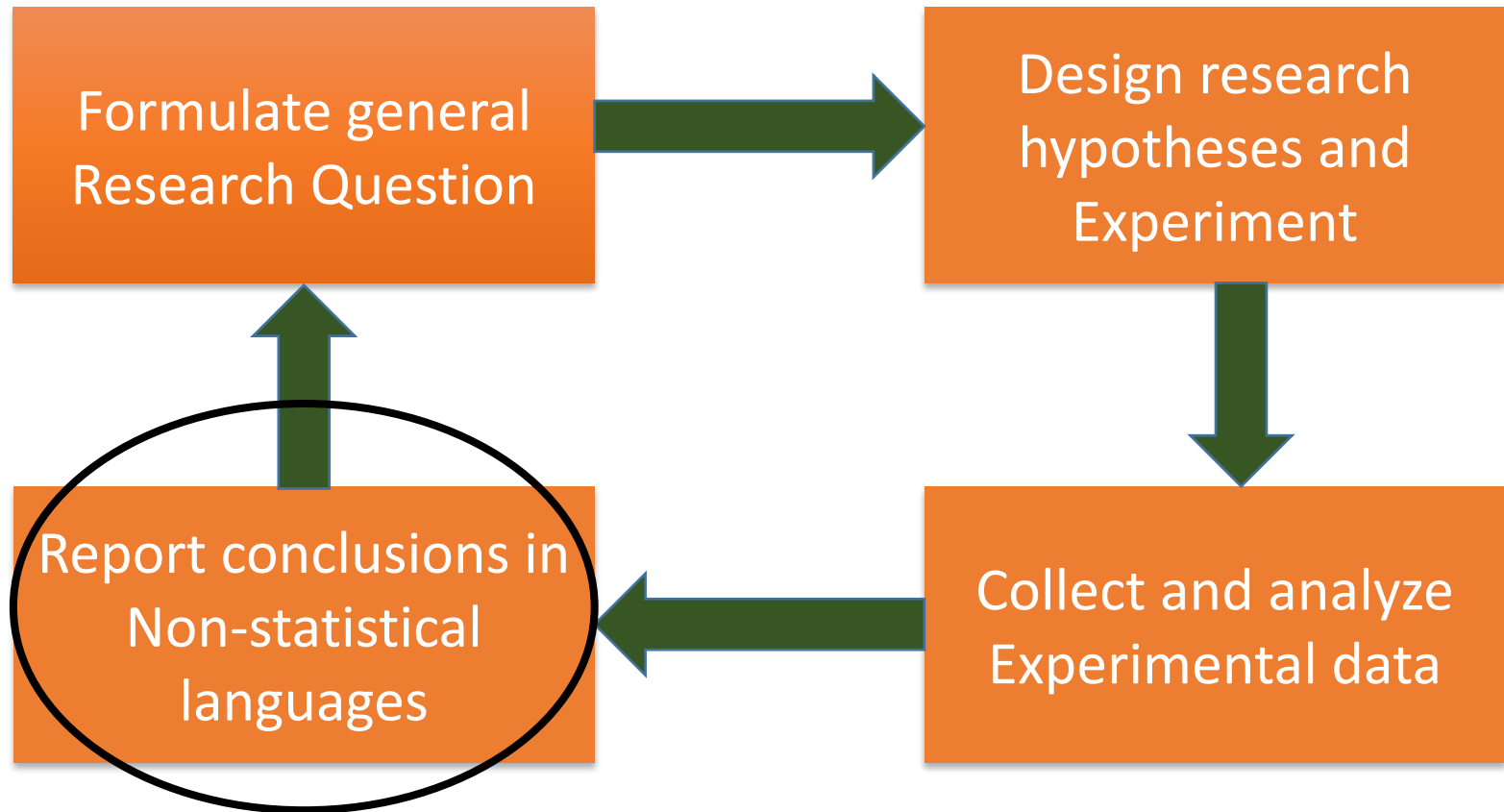
**Fail to Reject Null Hypothesis  $H_0$**

P-value (0.6) >  $\alpha$  (0.05)

(p-value method)

# **Collect and Analyze Experimental Data**

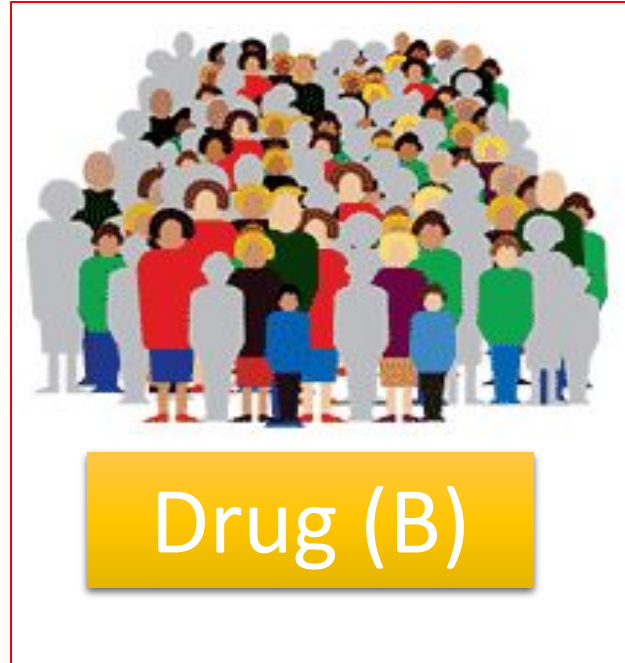
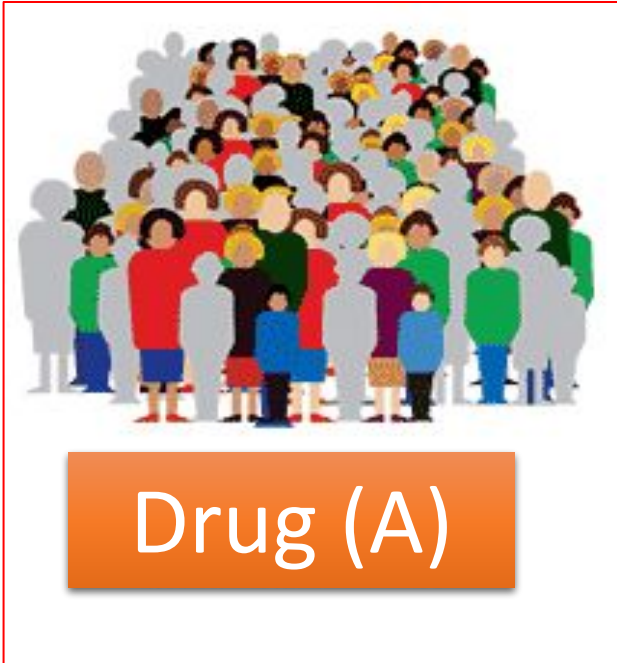
# Procedures of Hypotheses Testing and the Scientific Method



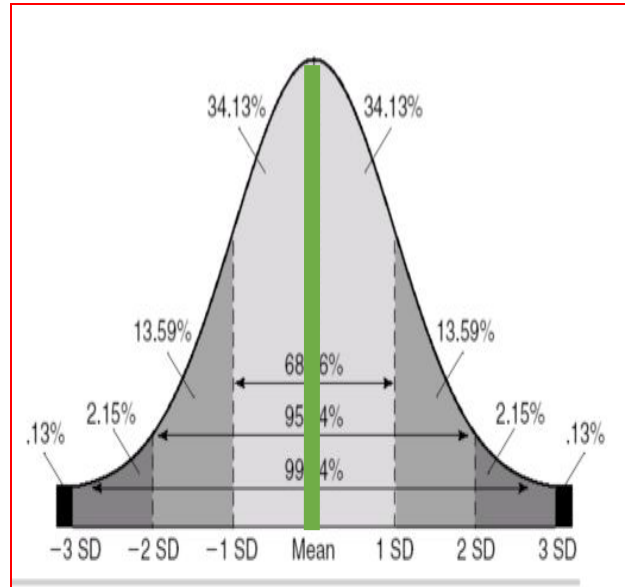
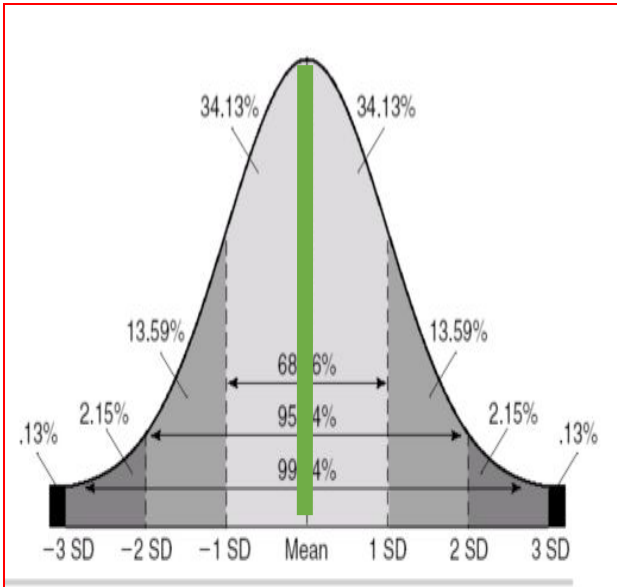
## **VI. Report a conclusion**

## **VI. Report a conclusion**

There is insufficient evidence to support the claim that there is a significant difference in the mean reduction of systolic blood pressure achieved by drug (A) and drug (B)



$$\frac{n_1}{X_1 S_1}$$



$$\frac{n_2}{X_2 S_2}$$

Fail to Reject  $H_0$

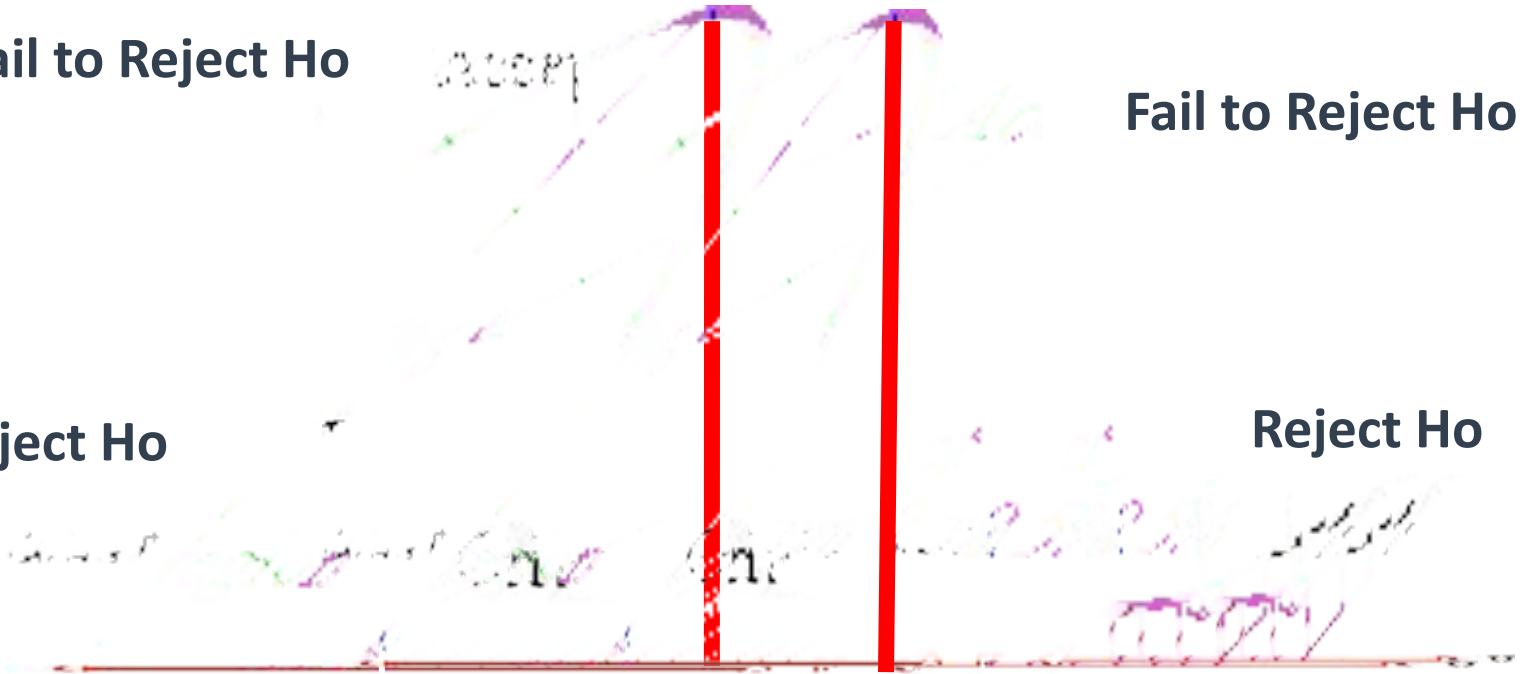
Fail to Reject  $H_0$

Reject  $H_0$

Reject  $H_0$

$X_1$   
9

$X_2$   
12

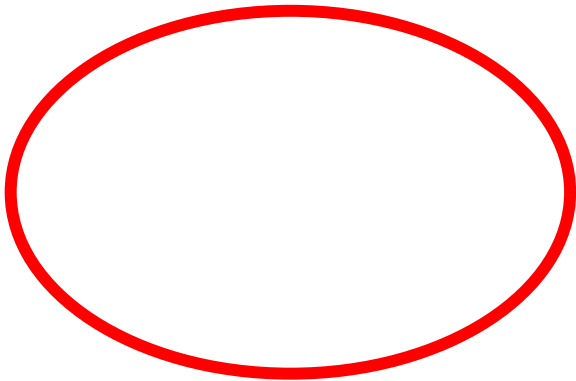


Comp  
(Par  
One P

Two P  
Indep

Depe

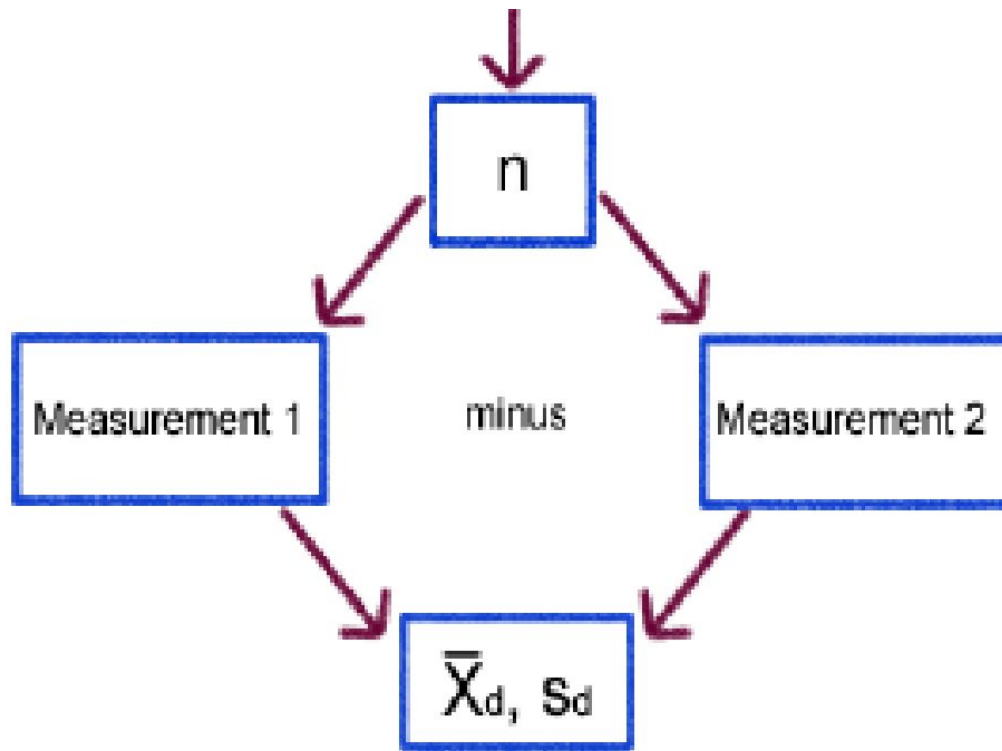
Analy





The data consists of a **single population** and **two measurements**. A simple random sample is taken from the population and pairs of measurement are collected. This is also called **related sampling** or **matched pair design**.





$\bar{X}_d$  is the sample mean of the differences of each pair

$S_d$  is the sample standard deviation of the differences of each pair

## **Matched pairs t-test**

**compares the means for two dependent populations  
(paired difference t-test)**

### **Model Assumptions**

Variable is quantitative continuous

Data is normally distributed

Dependent sampling

## Matched pairs t-test

compares the means for two dependent populations  
(paired difference t-test)

### Test Statistic

$$t = \frac{\bar{X}_d - \mu_d}{s_d / \sqrt{n}} \quad df = n - 1$$

$$X_d = X_1 - X_2$$

$$\bar{X}_d = \bar{X}_1 - \bar{X}_2 \text{ approximately Normal}$$

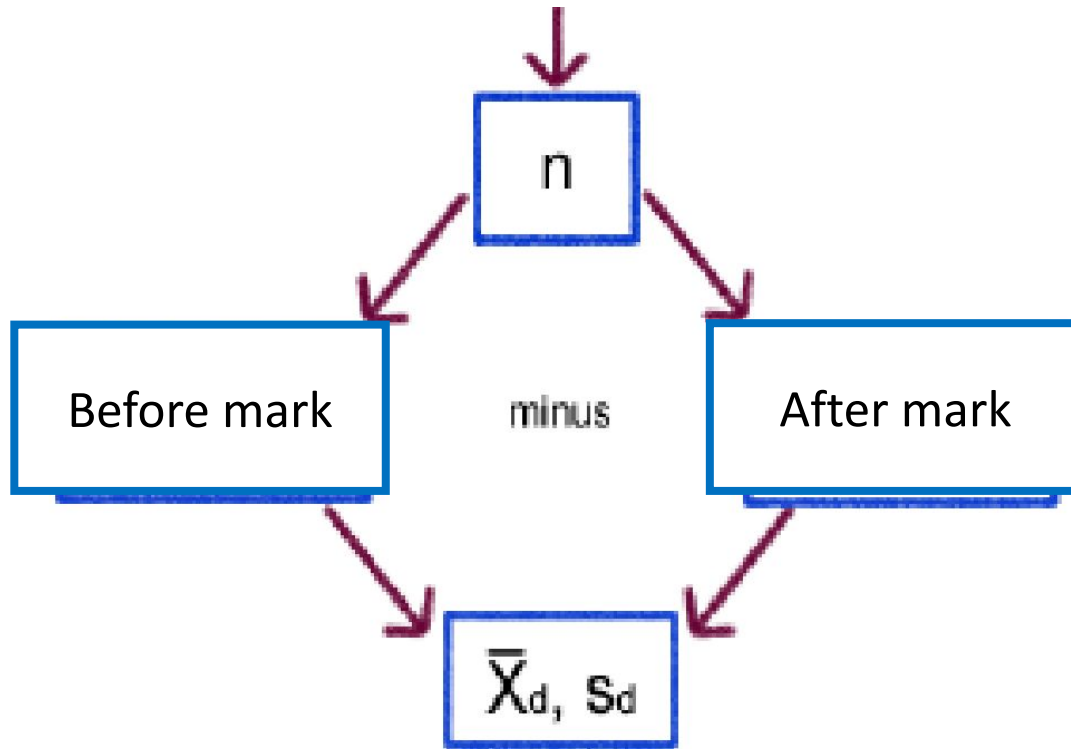
$\bar{X}_d$  sample mean of the differences of each pair

$S_d$  sample standard deviation of the differences of each pair

# **Exercise (15)**

## **Exercise (15):**

An instructor of Anatomy course wants to know if student marks are different on the second midterm compared to the first exam after implementation of a new teaching intervention; TBL (team-based learning). The first and second midterm marks for 35 students were taken and the mean difference in marks is determined.



$\bar{X}_d$  is the sample mean of the differences of each pair (2.05)  
 $S_d$  is the sample standard deviation of the differences of each pair

Diff	After Mark	Before Mark	Student
4	22	18	1
4	25	21	2
1	17	16	3
2	24	22	4
-3	16	19	5
5	29	24	6
3	20	17	7
-4	19	2	9
.	.	.	.
.	.	.	.
.	.	.	.
4	19	15	34
-1	16	17	35
2.05	20.45	18.40	Mean



Data were typed and analyzed using SPSS software program. The level of significance was 0.05. The appropriate statistical test was conducted and revealed test statistic = 3.23 (p=0.004). The followings are SPSS output tables.

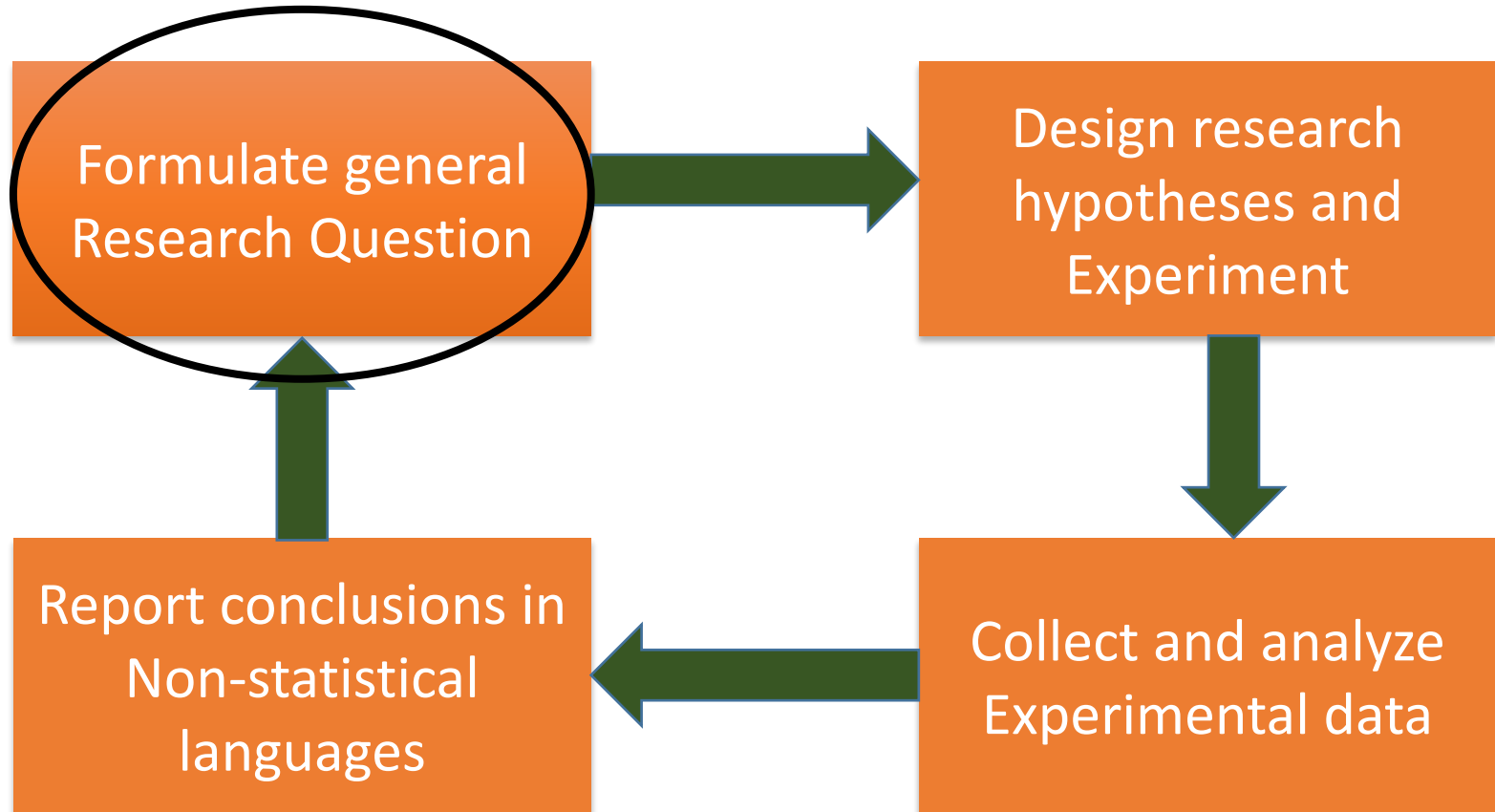
**Paired Samples Statistics**

		Mean	N	Std. Deviation	Std. Error Mean
Pair 1	Mark after	20.45	35	4.058	.907
	Mark before	18.40	35	3.152	.705

**Paired Samples Test**

	Paired Differences					t	df	Sig. (2-tailed)
	Mean	Std. Deviation	Std. Error Mean	95% Confidence Interval of the Difference				
				Lower	Upper			
Mark after - Mark before	2.050	2.837	.634	.722	3.378	3.231	19	.004

# Procedures of Hypotheses Testing and the Scientific Method

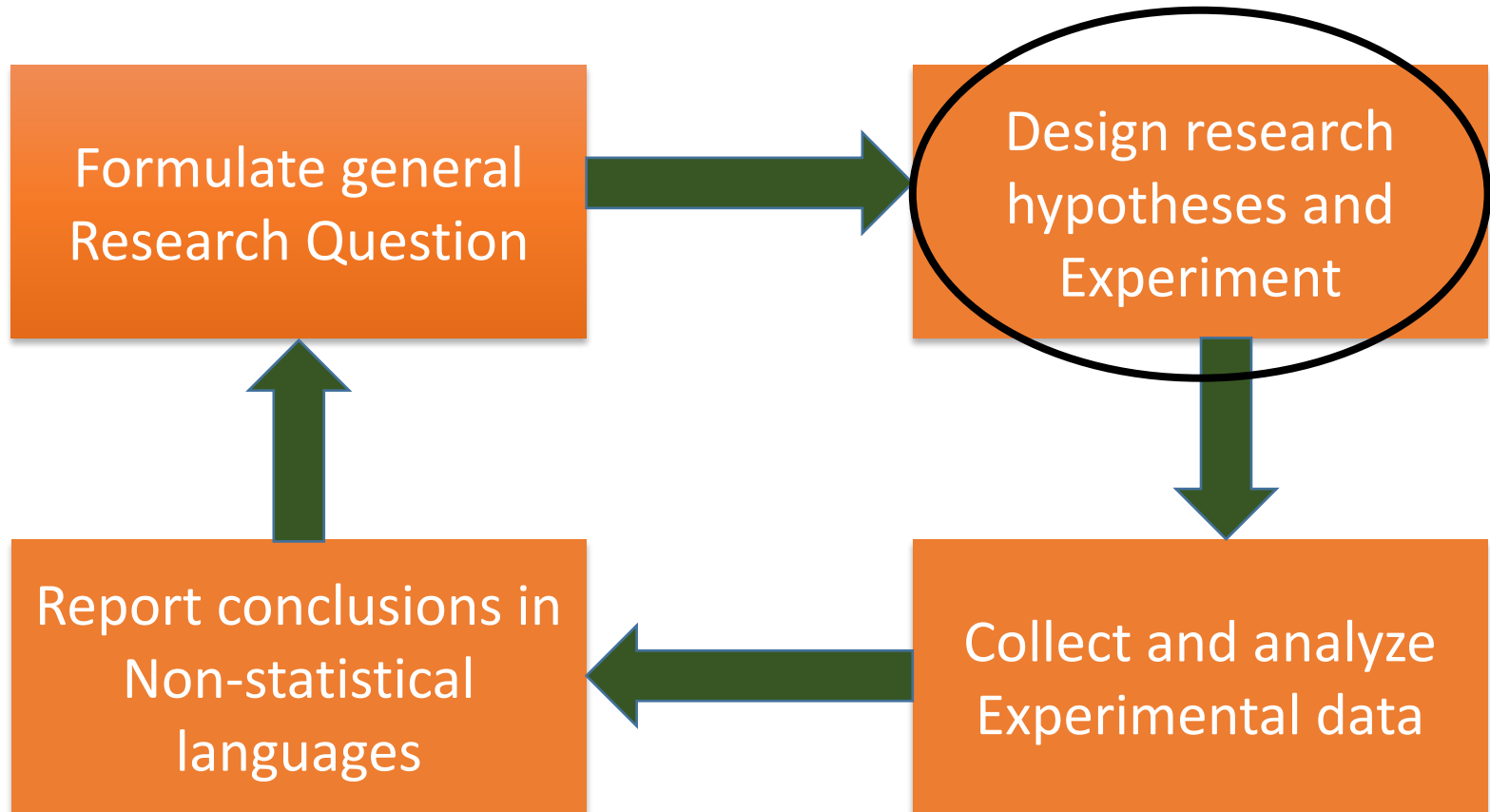


# **I. Formulate general Research Question**

## I. Formulate general Research Question

Is there a **difference** in students' marks following implementation of TBL (Team-based Learning)?

# Procedures of Hypotheses Testing and the Scientific Method



**II. State Research Hypotheses**

**III. What is the appropriate test statistic?**

**IV. What is the appropriate test Model? (One or Two tailed)**

## **II. State Research Hypotheses**

Ho: There is no difference in mean pre- and post-TBL marks

H1: There is a difference in mean pre- and post-TBL marks

## **III. What is the appropriate test statistic?**

## **IV. What is the appropriate test Model? (One or Two tailed)**

## II. State Research Hypotheses

Ho: There is no difference in mean pre- and post-TBL marks

H1: There is a difference in mean pre- and post-TBL marks

## III. What is the appropriate test statistic?

Matched pairs t-test

$$t = \frac{\bar{X}_d - \mu_d}{s_d / \sqrt{n}} \quad df = n - 1$$

## IV. What is the appropriate test Model? (One or Two tailed)



## II. State Research Hypotheses

Ho: There is no difference in mean pre- and post-TBL marks

H1: There is a difference in mean pre- and post-TBL marks

## III. What is the appropriate test statistic?

Matched pairs t-test

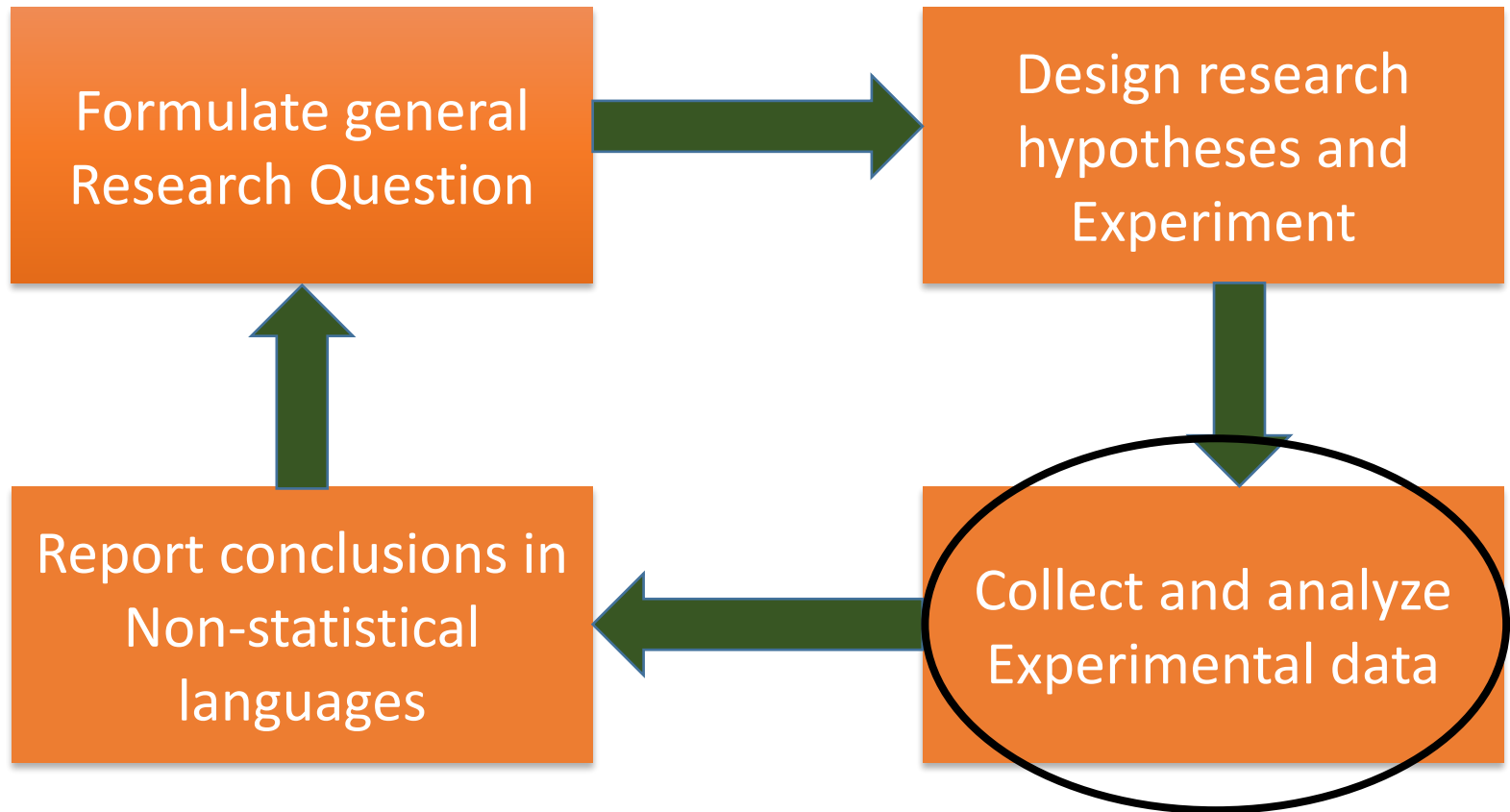
$$t = \frac{\bar{X}_d - \mu_d}{s_d / \sqrt{n}} \quad df = n - 1$$

## IV. What is the appropriate test Model? (One or Two tailed)

Two Tailed Test Model

# **Design Research Hypotheses and Experiment**

# Procedures of Hypotheses Testing and the Scientific Method



# **Collect and Analyze Experimental Data**

**V. Make a Decision regarding Research Hypotheses  
(Specify the Decision Method)**

Data were typed and analyzed using SPSS software program. The level of significance was 0.05. The appropriate statistical test was conducted and revealed test statistic = 3.23 (p=0.004). The followings are SPSS output tables.

**Paired Samples Statistics**

		Mean	N	Std. Deviation	Std. Error Mean
Pair 1	Mark after	20.45	35	4.058	.907
	Mark before	18.40	35	3.152	.705

**Paired Samples Test**

	Paired Differences					t	df	Sig. (2-tailed)
	Mean	Std. Deviation	Std. Error Mean	95% Confidence Interval of the Difference				
				Lower	Upper			
Mark after - Mark before	<b>2.050</b>	2.837	.634	.722	3.378	3.231	19	<b>.004</b>

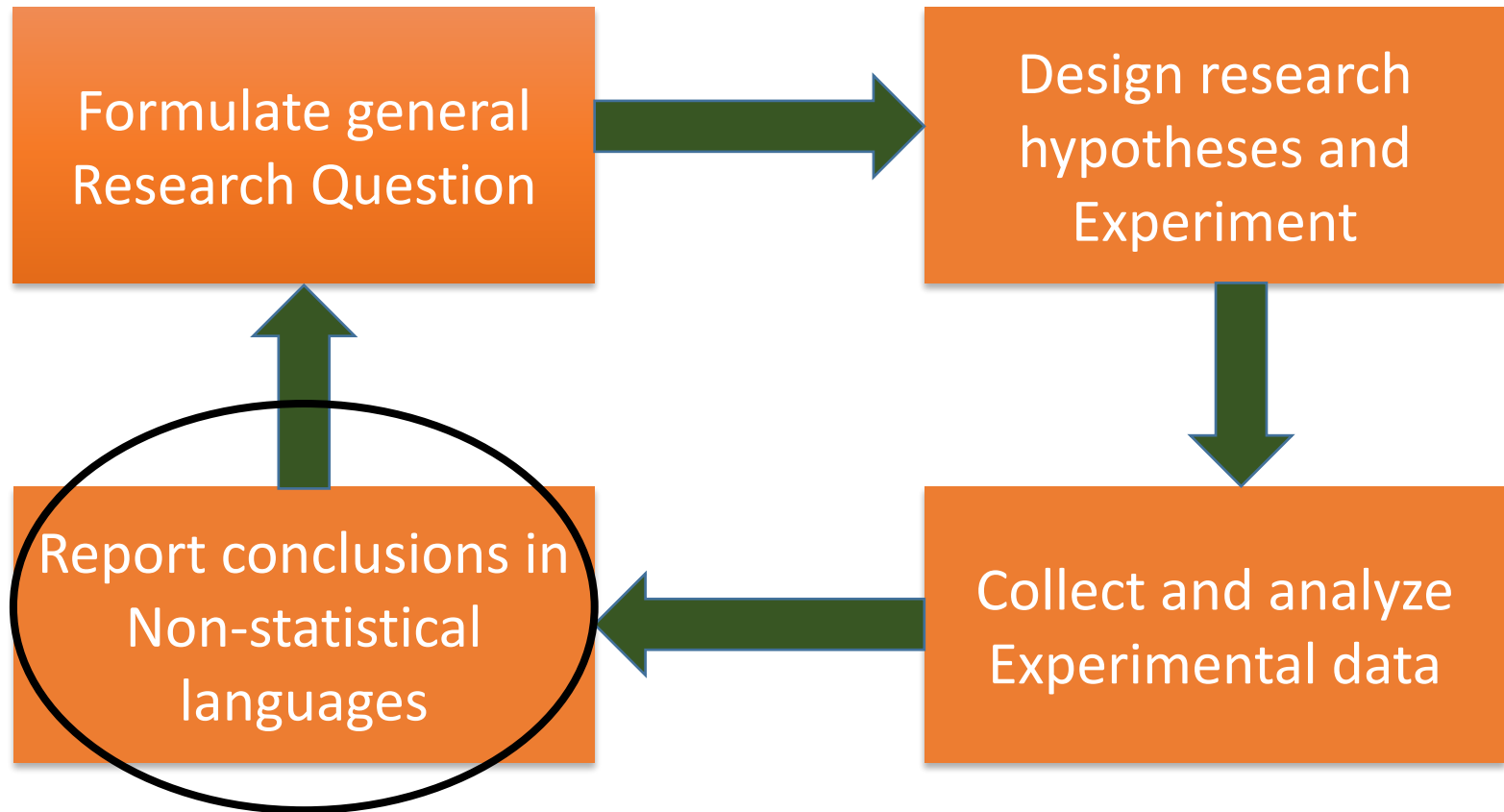
## V. Make a Decision regarding Research Hypotheses (Specify the Decision Method)

**Reject Null Hypothesis  $H_0$**

P-value (0.004) <  $\alpha$  (0.05)

(p-value method)

# Procedures of Hypotheses Testing and the Scientific Method

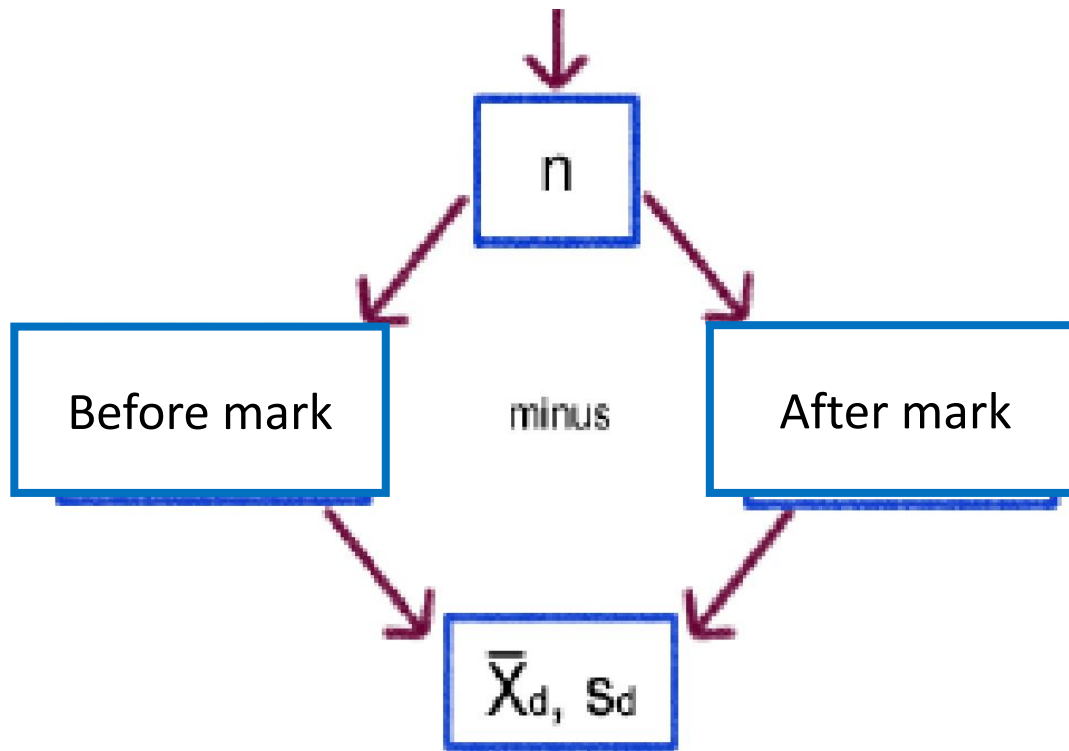




## **VI. Report a conclusion**

## VI. Report a conclusion

There is a strong evidence ( $t = 3.23$ ,  $p = 0.004$ ) that TBL as a teaching intervention improves students' marks. In this data set, it improved marks, on average, by approximately 2 points (mean paired difference = 2.05).



$\bar{X}_d$  is the sample mean of the differences of each pair (2.05)

$S_d$  is the sample standard deviation of the differences of each pair

Fail to Reject  $H_0$

Fail to Reject  $H_0$

Reject  $H_0$

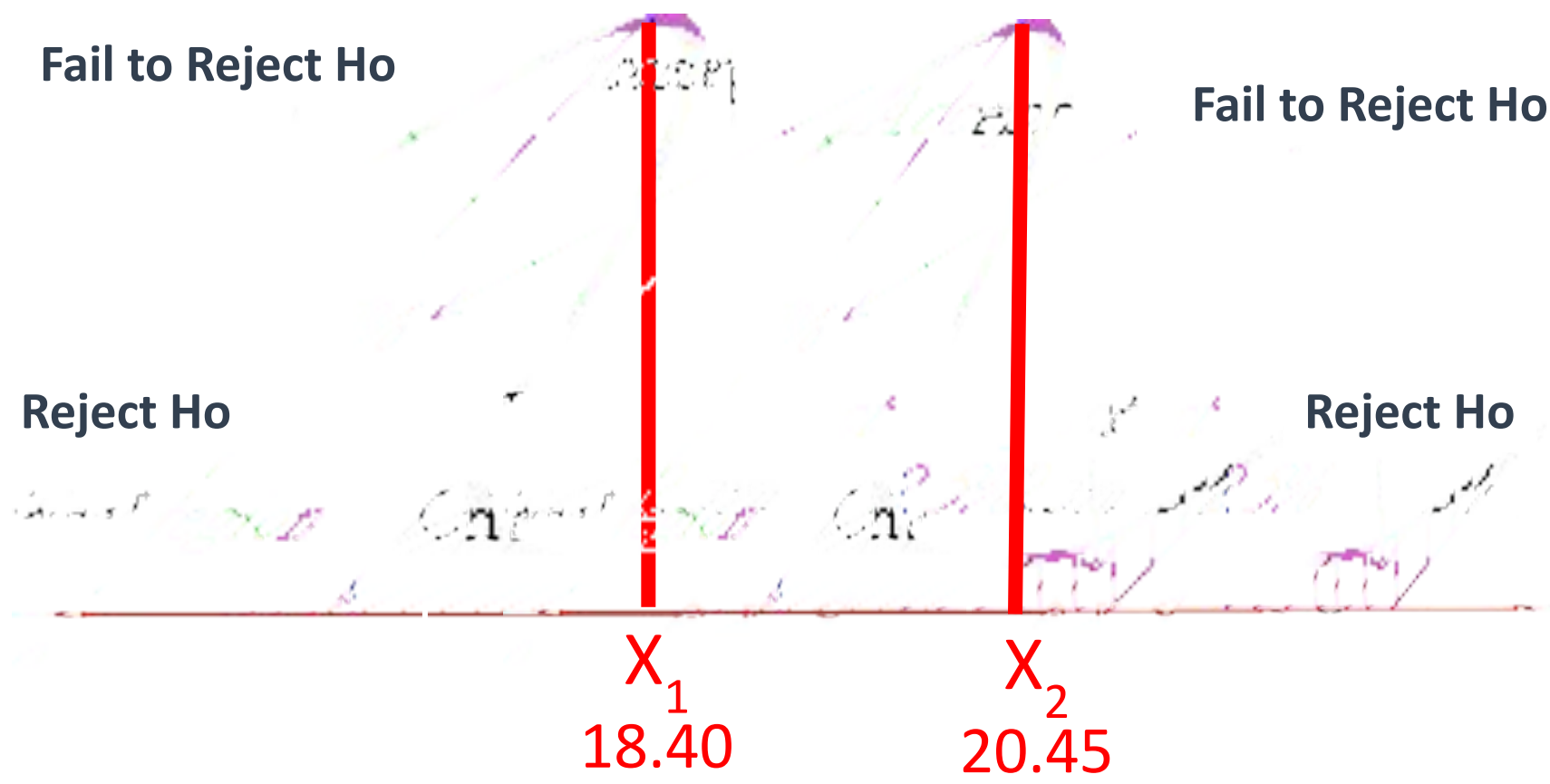
Reject  $H_0$

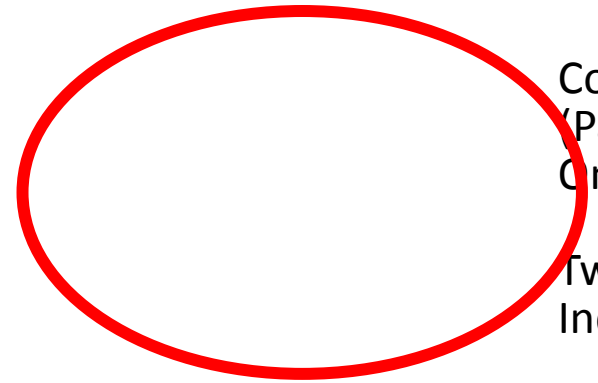
$X_1$

18.40

$X_2$

20.45





Comp

(Par

One P

Two P

Indep

Depe

Analy

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

Suppose we wanted to compare the means of more than two (k) independent populations and want to test the null hypothesis  $H_0: \mu_1 = \mu_2 = \dots = \mu_k$ .

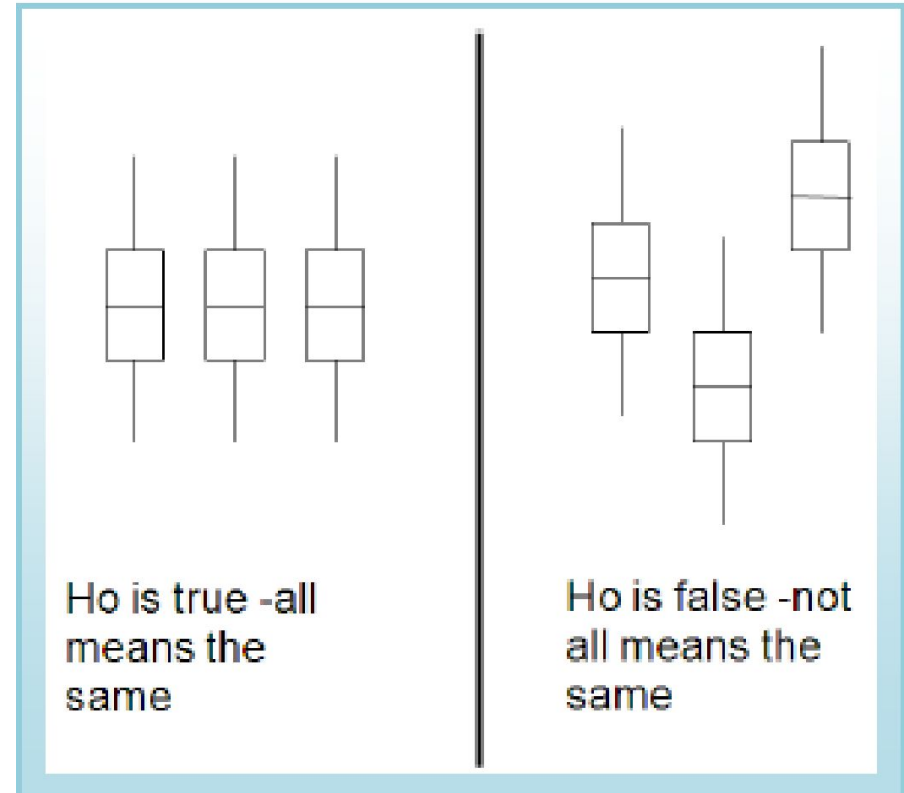
If we can **assume all population variances are equal**, we can expand the pooled variance t-test for two populations to one factor ANOVA for k populations.

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

If  $H_0: \mu_1 = \mu_2 = \mu_3$  is true, then each population would have the same distribution and the **variance of the combined data** would be approximately the **same**.

If the  $H_0$  is false, then the difference between centers would cause the **combined data** to have an **increased variance**.



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Data Requirements

1. Dependent variable that is continuous.
2. Independent variable (Factor) that is categorical ( $\geq 3$  groups)
3. Cases that have values on both the dependent and independent variables



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Data Requirements

4. Independent samples/groups (i.e., independence of observations); there is no relationship between the subjects in each sample.

This means that:

- A. subjects in the first group cannot also be in the second group
- B. no subject in either group can influence subjects in the other group
- C. no group can influence the other group

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Data Requirements

5. Random sample of data from the population.
6. Normal distribution (approximately) of the dependent variable for each group (i.e., for each level of the factor)
7. Homogeneity of variances (i.e., variances approximately equal across groups)
8. No outliers

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Model Assumptions

The populations being sampled are normally distributed

The populations have equal standard deviations

The samples are randomly selected and are independent

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Research Hypotheses

$$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$$

("all  $k$  population means are equal")

**$H_a$ : At least one  $\mu_i$  different**

("at least one of the  $k$  population means is not equal to the others")

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Test Statistic

P-value	F	Mean Square (MS)	df	Sum of Squares (SS)	Source of Variation
	$F = MS_{\text{Factor}} / MS_{\text{Error}}$	$MS_{\text{Factor}} = SS_{\text{Factor}} / k - 1$	$k - 1$	$SS_{\text{Factor}}$	Factor (Between)
		$MS_{\text{Error}} = SS_{\text{Error}} / n - k$	$n - k$	$SS_{\text{Error}}$	Error (Within)
			$n - 1$	$SS_{\text{Total}}$	Total

$SS_{\text{Factor}}$  = the regression sum of squares;  $SS_{\text{Error}}$  = the error sum of squares

$SS_{\text{Total}}$  = the total sum of squares (SST = SSR + SSE)

$k$  = the total number of groups;  $n$  = the total number of valid observations

$MS_{\text{Factor}}$  = the regression mean square;  $MS_{\text{Error}}$  = the mean square error

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct an  
exploratory  
analysis

**Why?**

- a) Examine descriptive statistics
- b) Check for outliers
- c) Check that the normality assumption is met
- d) Verify that there are mean differences between groups to justify ANOVA

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**



Conduct One  
Way ANOVA

**Why?**

1. Determine whether group means are different from one another (warranting post hoc comparison tests)
2. Check that the homogeneity of variance assumption is met

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct Post  
hoc  
comparison  
test

**Why?**

To confirm where the differences occurred between groups

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# **Exercise (16)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Exercise (16)

A research was conducted to examine if there a difference in mean score of medical students at 4 universities located at different geographical locations (North-East, North-Central, South, and West region).

In order to conduct the research, 400 randomly selected students from the 4 universities were included, and their scores were reported. Data were typed and analyzed by SPSS software program. The statistician selected level of significance = 0.05.

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **I. State the Research Question**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### I. State the Research Question

Are there any differences in the mean score of medical students enrolled at North-East, North-Central, South, and West Universities?



# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **II. State the Research Hypotheses**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### II. State the Research Hypotheses

$$H_0: \mu_1 = \mu_2 = \mu_3 = \mu_4$$

$\mu_1$ : mean score of students at North-East University

$\mu_2$ : mean score of students at North-Central University

$\mu_3$ : mean score of students at North-East University

$\mu_4$ : mean score of students at North-East University

**$H_a$ : At least one  $\mu_i$  different**

("at least one of the 4 population means is not equal to the others")

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**III. Specify the Dependent and Independent variables**  
**Mention the type of variable and number of groups**

Type of variable number of groups	Variable	
		Dependent Variable
		Independent Variable (Factor)

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### III. Specify the Dependent and Independent variables

Mention the type of variable and number of groups

Type of variable number of groups	Variable	
Quantitative Continuous	Score	<b>Dependent Variable</b>
Categorical/Qualitative (4 groups)	Geographic Region of Medical School	<b>Independent Variable (Factor)</b>

# **Exercise (17)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Exercise (17)

A manager of a pharmaceutical company wants to raise the productivity at his company by increasing the speed at which his pharmacists carry out pharmaceutical formulation.

As he does not have the skills in-house, he employs an external agency which provides training in pharmaceutical formulation Development. They offer 3 packages - a beginner, intermediate and advanced course.

He is unsure which course is needed for the type of work they do at his company so he sends 10 pharmacists on the beginner course, 10 on the intermediate and 10 on the advanced course.

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### Exercise (17)

When they all return from the training he gives them a task to formulate certain parenteral drug produced by the company and times how long it takes them to complete the task.

He wishes to then compare the three courses (beginner, intermediate, advanced) to see if there are any differences in the average time it took to complete the task.

The statistician selected level of significance = 0.05

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **I. State the Research Question**



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### I. State the Research Question

Are there any differences in the average time taken by the pharmacists who attended the three training courses (Beginner, Intermediate, and Advanced courses), to complete the drug formulation task?

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **II. State the Research Hypotheses**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### II. State the Research Hypotheses

$$H_0: \mu_1 = \mu_2 = \mu_3$$

$\mu_1$ : Mean time (hour) taken by the pharmacists who attended the beginner course to complete the task.

$\mu_2$ : Mean time (hour) taken by the pharmacists who attended the intermediate course to complete the task.

$\mu_3$ : Mean time (hour) taken by the pharmacists who attended the advanced course to complete the task.

**$H_a$ : At least one  $\mu_i$  different**

("at least one of the 3 population means is not equal to the others")

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### III. Specify the Dependent and Independent variables

Mention the type of variable and number of groups

Type of variable number of groups	Variable	
		Dependent Variable
		Independent Variable (Factor)

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### III. Specify the Dependent and Independent variables

Mention the type of variable and number of groups

Type of variable number of groups	Variable	
Quantitative Continuous	Time	<b>Dependent Variable</b>
Categorical/Qualitative (3 groups)	Course	<b>Independent Variable (Factor)</b>

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct an  
exploratory  
analysis

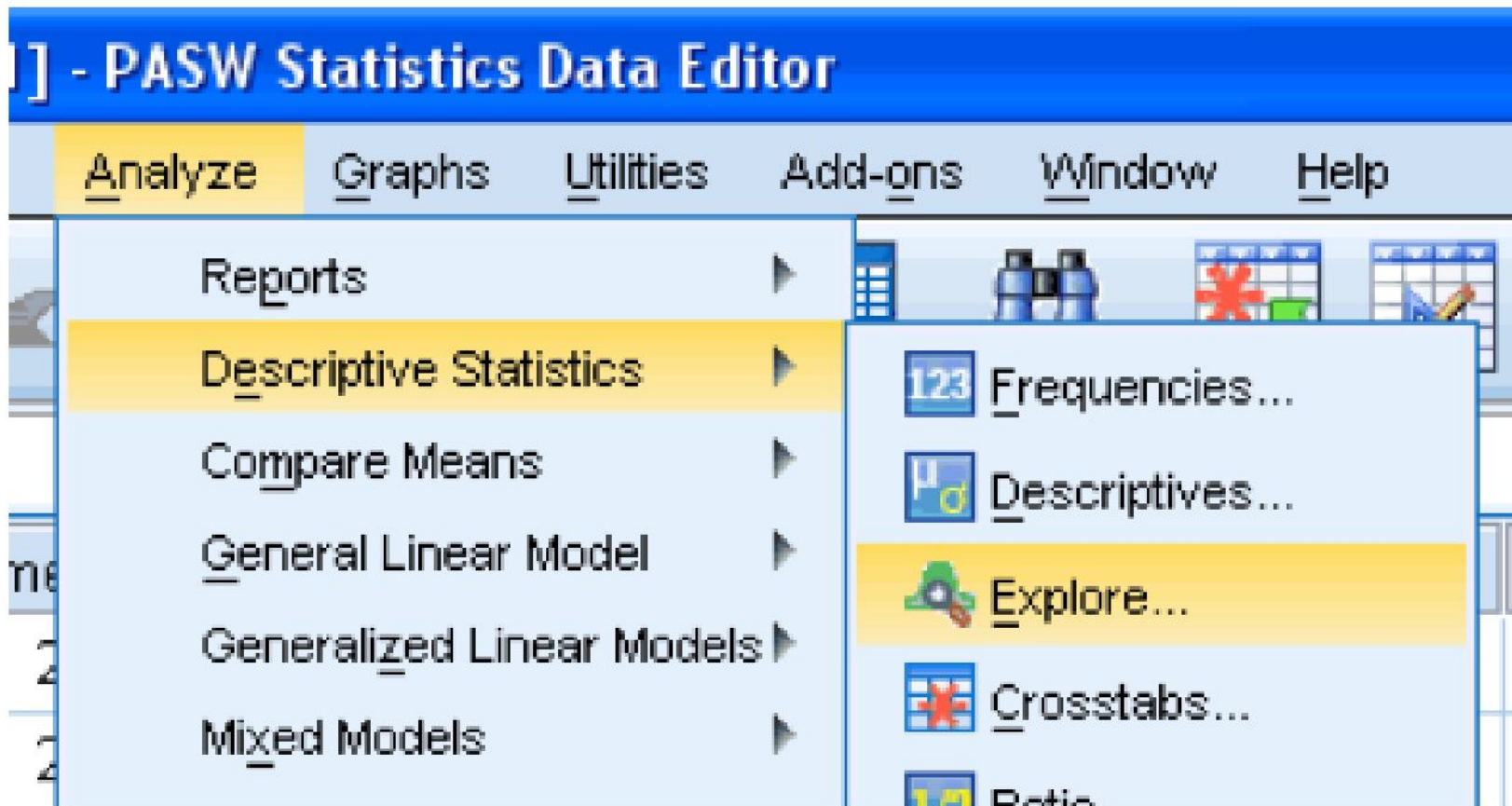
**Why?**

- a) Examine descriptive statistics
- b) Check for outliers

# One Factor ANOVA model - One Way ANOVA

Comparing means from more than two Independent Populations

Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)





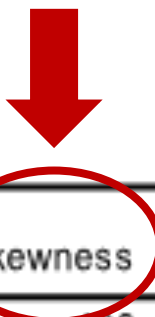
# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)

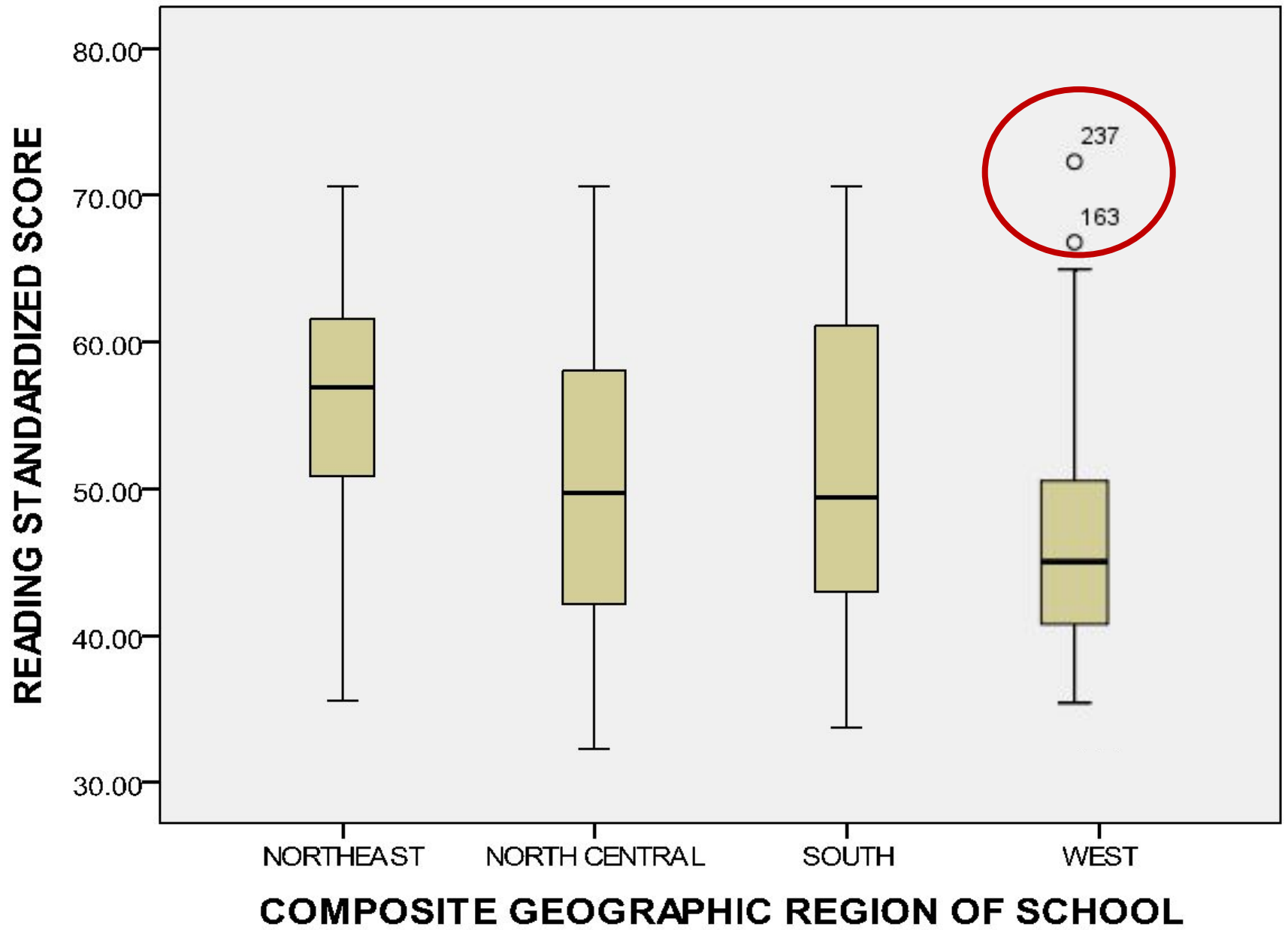
Report

READING STANDARDIZED SCORE



COMPOSITE GEOGRAPHIC REGI...	Mean	N	Std. Deviation	Variance	Skewness	Std. Error of Skewness
NORTHEAST	55.8918	100	9.86641	97.346	-.486	.316
NORTH CENTRAL	50.8328	100	10.01432	100.287	.224	.267
SOUTH	51.3382	100	10.00440	100.088	.246	.241
WEST	49.0311	100	9.81560	96.346	.502	.304
Total	51.5901	400	10.14505	102.922	.152	.141

# Box plot graph



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct an  
exploratory  
analysis

**Why?**

- a) Examine descriptive statistics
- b) Check for outliers
- c) Check that the normality assumption is met

# Histogram

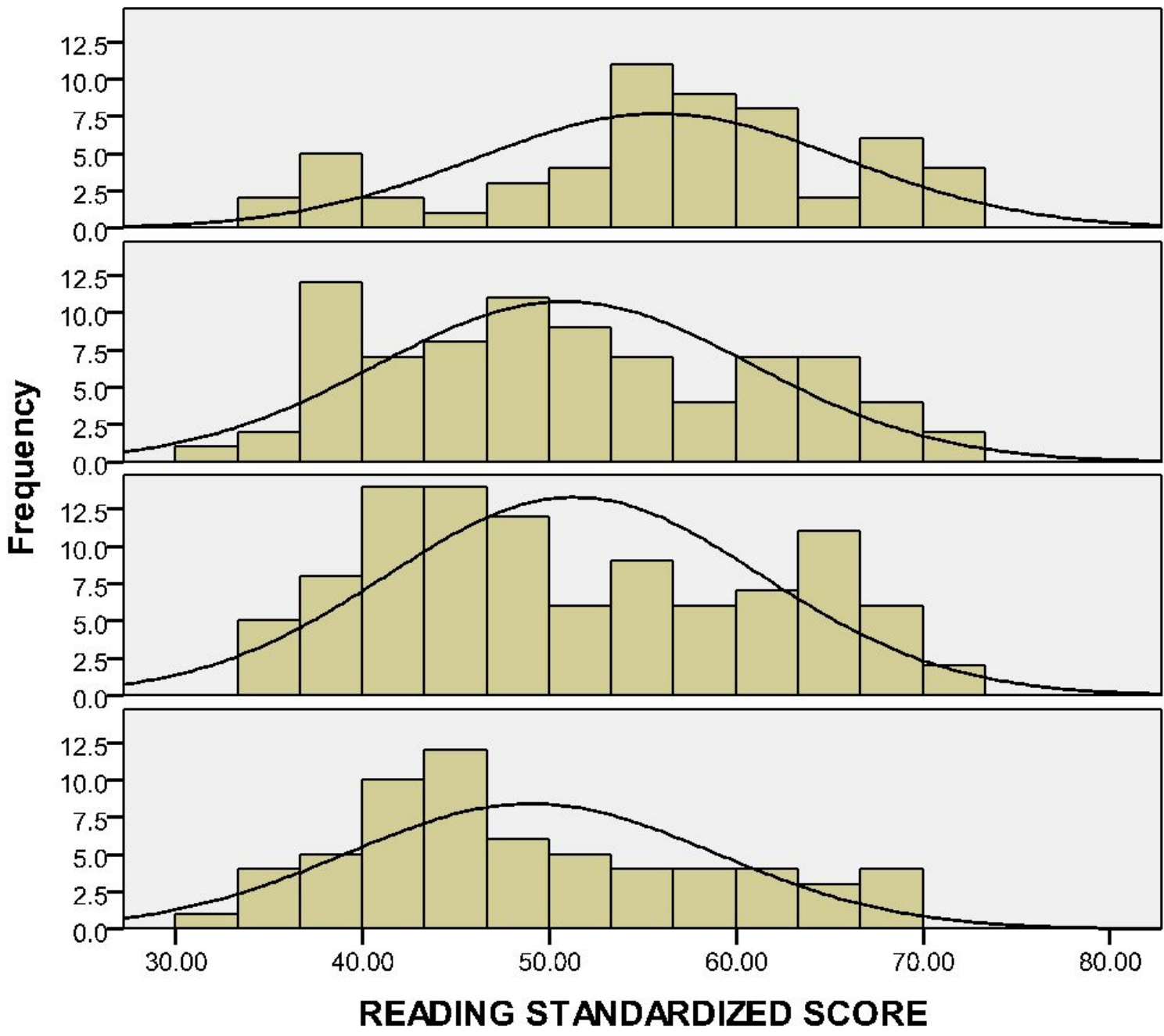
**COMPOSITE GEOGRAPHIC REGION OF SCHOOL**

**NORTHEAST**

**NORTH  
CENTRAL**

**SOUTH**

**WEST**



# Tests of Normality



Empty list box for variable selection



Dependent List:

Time



Factor List:

Course



Label Cases by:

Empty text box for label cases

Statistics...

Plots...

Options...

Display

- Both
- Statistics
- Plots

OK Paste Reset Cancel Help





## Explore: Plots



### Boxplots

- Factor levels together
- Dependents together
- None

### Descriptive

- Stem-and-leaf
- Histogram

Normality plots with tests

### Spread vs Level with Levene Test

- None
- Power estimation
- Transformed Power:
- Untransformed

Continue

Cancel

Help

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)

### Shapiro-Wilk Test of Normality

Tests of Normality

Course		Kolmogorov-Smirnov <sup>a</sup>			Shapiro-Wilk		
		Statistic	df	Sig.	Statistic	df	Sig.
Time	Beginner	.177	10	.200 <sup>*</sup>	.964	10	.827
	Intermediate	.166	10	.200 <sup>*</sup>	.969	10	.882
	Advanced	.151	10	.200 <sup>*</sup>	.965	10	.837

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

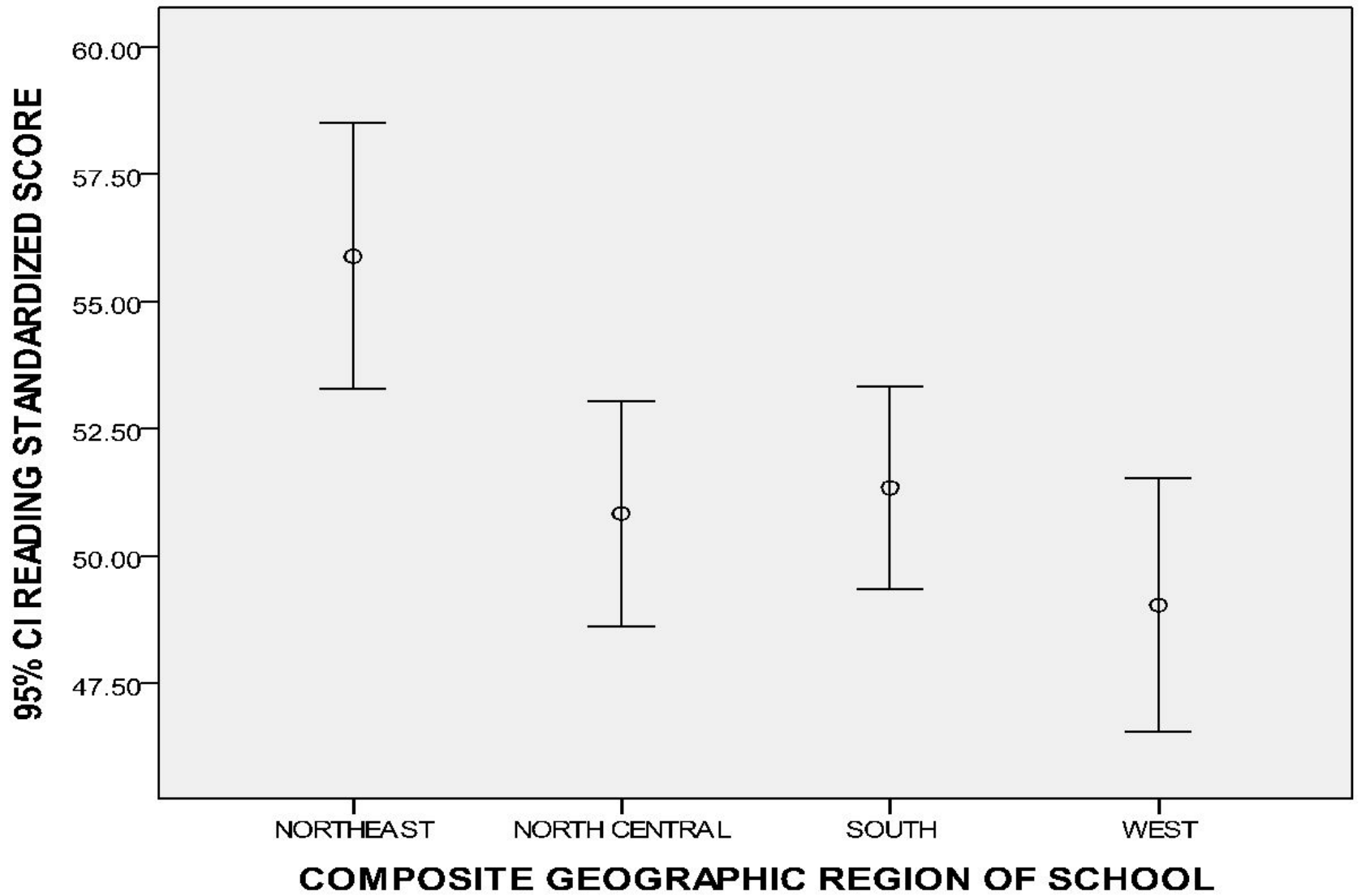
**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct an  
exploratory  
analysis

**Why?**

- a) Examine descriptive statistics
- b) Check for outliers
- c) Check that the normality assumption is met
- d) Verify that there are mean differences between groups to justify ANOVA

# Error Bar graph



# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct an  
exploratory  
analysis

**Why?**

- a) Examine descriptive statistics
- b) Check for outliers
- c) Check that the normality assumption is met
- d) Verify that there are mean differences between groups to justify ANOVA

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**



Conduct One  
Way ANOVA

**Why?**

1. Determine whether group means are different from one another (warranting post hoc comparison tests)
2. Check that the homogeneity of variance assumption is met



# 1] - PASW Statistics Data Editor

Analyze   Graphs   Utilities   Add-ons   Window   Help

Reports ▶

Descriptive Statistics ▶

Compare Means ▶

General Linear Model ▶

Generalized Linear Models ▶

Mixed Models ▶

Correlate ▶

Regression ▶

Loglinear ▶



**M** Means...

**t** One-Sample T Test...

**t**  
**A-B** Independent-Samples T Test...

**t**  
**A<sub>1</sub>-A<sub>2</sub>** Paired-Samples T Test...

**F**  
**0** One-Way ANOVA...

# One-Way ANOVA



- Course
- Time



Dependent List:



Factor:

Contrasts...

Post Hoc...

Options...

OK

Paste

Reset


Cancel

Help

# One-Way ANOVA



Dependent List:

 Time

Contrasts...

Post Hoc...

Options...



Factor:

 Course

OK

Paste

Reset

Cancel

Help



## One-Way ANOVA: Options



### Statistics

- Descriptive
- Fixed and random effects
- Homogeneity of variance test
- Brown-Forsythe
- Welch

- Means plot

### Missing Values

- Exclude cases analysis by analysis
- Exclude cases listwise

Continue

Cancel

Help

### Descriptives

Time

	N	Mean	Std. Deviation	Std. Error	95% Confidence Interval for Mean		Minimum	Maximum
					Lower Bound	Upper Bound		
Beginner	10	27.2000	3.04777	.96379	25.0198	29.3802	22.00	33.00
Intermediate	10	23.6000	3.30656	1.04563	21.2346	25.9654	18.00	29.00
Advanced	10	23.4000	3.23866	1.02415	21.0832	25.7168	18.00	29.00
Total	30	24.7333	3.56161	.65026	23.4034	26.0633	18.00	33.00

### Test of Homogeneity of Variances

Time

Levene Statistic	df1	df2	Sig.
.105	2	27	.901

### ANOVA

Time

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	91.467	2	45.733	4.467	.021
Within Groups	276.400	27	10.237		
Total	367.867	29			

Used with written permission from SPSS Inc. an IBM Company

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**



Conduct One  
Way ANOVA

**Why?**

1. Determine whether group means are different from one another (warranting post hoc comparison tests)
2. Check that the homogeneity of variance assumption is met



# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct Post  
hoc  
comparison  
test

**Why?**

To confirm where the differences occurred between groups

# 1] - PASW Statistics Data Editor

Analyze   Graphs   Utilities   Add-ons   Window   Help

Reports ▶

Descriptive Statistics ▶

Compare Means ▶

General Linear Model ▶

Generalized Linear Models ▶

Mixed Models ▶

Correlate ▶

Regression ▶

Loglinear ▶



**M** Means...

**t** One-Sample T Test...

**t**  
**A-B** Independent-Samples T Test...

**t**  
**A1-A2** Paired-Samples T Test...


**F**  
**0** One-Way ANOVA...



# One-Way ANOVA



Dependent List:

-  Time

Contrasts...

Post Hoc...

Options...



Factor:

-  Course

OK

Paste

Reset

Cancel

Help

# One-Way ANOVA: Post Hoc Multiple Comparisons



## Equal Variances Assumed

 LSD Bonferroni Sidak Scheffe R-E-G-W F R-E-G-W Q S-N-K Tukey Tukey's-b Duncan Hochberg's GT2 Gabriel Waller-DuncanType I/Type II Error Ratio:  DunnettControl Category : 

## Test

 2-sided  < Control  > Control

## Equal Variances Not Assumed

 Tamhane's T2 Dunnett's T3 Games-Howell Dunnett's CSignificance level:

### Multiple Comparisons

Dependent Variable: Time

	(I) Course	(J) Course	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
						Lower Bound	Upper Bound
Tukey HSD	Beginner	Intermediate	3.60000 <sup>*</sup>	1.43088	.046	.0523	7.1477
		Advanced	3.80000 <sup>*</sup>	1.43088	.034	.2523	7.3477
	Intermediate	Beginner	-3.60000 <sup>*</sup>	1.43088	.046	-7.1477	-.0523
		Advanced	.20000	1.43088	.989	-3.3477	3.7477
	Advanced	Beginner	-3.80000 <sup>*</sup>	1.43088	.034	-7.3477	-.2523
		Intermediate	-.20000	1.43088	.989	-3.7477	3.3477

### Multiple Comparisons

READING STANDARDIZED SCORE  
Tukey HSD

(I) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	(J) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
NORTHEAST	NORTH CENTRAL	5.05891 <sup>*</sup>	1.71890	.018	.6178	9.5000
	SOUTH	4.55355 <sup>*</sup>	1.65008	.031	.2903	8.8168
	WEST	6.86063 <sup>*</sup>	1.82445	.001	2.1468	11.5744
NORTH CENTRAL	NORTHEAST	-5.05891 <sup>*</sup>	1.71890	.018	-9.5000	-.6178
	SOUTH	-.50536	1.48624	.986	-4.3453	3.3346
	WEST	1.80171	1.67773	.706	-2.5330	6.1364
SOUTH	NORTHEAST	-4.55355 <sup>*</sup>	1.65008	.031	-8.8168	-.2903
	NORTH CENTRAL	.50536	1.48624	.986	-3.3346	4.3453
	WEST	2.30707	1.60714	.478	-1.8453	6.4594
WEST	NORTHEAST	-6.86063 <sup>*</sup>	1.82445	.001	-11.5744	-2.1468
	NORTH CENTRAL	-1.80171	1.67773	.706	-6.1364	2.5330
	SOUTH	-2.30707	1.60714	.478	-6.4594	1.8453

\*. The mean difference is significant at the 0.05 level.

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

Conduct Post  
hoc  
comparison  
test

**Why?**

To confirm where the differences occurred between groups



# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**

# **Return to Exercise (16)**

## ANOVA

READING STANDARDIZED SCORE

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	1513.532	3	504.511	5.104	.002
Within Groups	29260.128	296	98.852		
Total	30773.660	299			

### Multiple Comparisons

READING STANDARDIZED SCORE  
Tukey HSD

(I) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	(J) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
NORTHEAST	NORTH CENTRAL	5.05891 <sup>*</sup>	1.71890	.018	.6178	9.5000
	SOUTH	4.55355 <sup>*</sup>	1.65008	.031	.2903	8.8168
	WEST	6.86063 <sup>*</sup>	1.82445	.001	2.1468	11.5744
NORTH CENTRAL	NORTHEAST	-5.05891 <sup>*</sup>	1.71890	.018	-9.5000	-.6178
	SOUTH	-.50536	1.48624	.986	-4.3453	3.3346
	WEST	1.80171	1.67773	.706	-2.5330	6.1364
SOUTH	NORTHEAST	-4.55355 <sup>*</sup>	1.65008	.031	-8.8168	-.2903
	NORTH CENTRAL	.50536	1.48624	.986	-3.3346	4.3453
	WEST	2.30707	1.60714	.478	-1.8453	6.4594
WEST	NORTHEAST	-6.86063 <sup>*</sup>	1.82445	.001	-11.5744	-2.1468
	NORTH CENTRAL	-1.80171	1.67773	.706	-6.1364	2.5330
	SOUTH	-2.30707	1.60714	.478	-6.4594	1.8453

\*. The mean difference is significant at the 0.05 level.

Report

READING STANDARDIZED SCORE

COMPOSITE GEOGRAPHIC REGI...	Mean	N	Std. Deviation	Variance	Skewness	Std. Error of Skewness
NORTHEAST	55.8918	100	9.86641	97.346	-.486	.316
NORTH CENTRAL	50.8328	100	10.01432	100.287	.224	.267
SOUTH	51.3382	100	10.00440	100.088	.246	.241
WEST	49.0311	100	9.81560	96.346	.502	.304
Total	51.5901	400	10.14505	102.922	.152	.141

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **IV. Make your Decision regarding Research Hypotheses**

## ANOVA

READING STANDARDIZED SCORE

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	1513.532	3	504.511	5.104	.002
Within Groups	29260.128	296	98.852		
Total	30773.660	299			

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### IV. Make your Decision regarding Research Hypotheses

**Reject Null Hypothesis  $H_0$**

p-value of F statistic = 0.002

P-value <  $\alpha$

0.002 < 0.05



# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **V. Report a conclusion**

### Multiple Comparisons

READING STANDARDIZED SCORE  
Tukey HSD

(I) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	(J) COMPOSITE GEOGRAPHIC REGION OF SCHOOL	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
NORTHEAST	NORTH CENTRAL	5.05891*	1.71890	.018	.6178	9.5000
	SOUTH	4.55355*	1.65008	.031	.2903	8.8168
	WEST	6.86063*	1.82445	.001	2.1468	11.5744
NORTH CENTRAL	NORTHEAST	-5.05891*	1.71890	.018	-9.5000	-.6178
	SOUTH	-.50536	1.48624	.986	-4.3453	3.3346
	WEST	1.80171	1.67773	.706	-2.5330	6.1364
SOUTH	NORTHEAST	-4.55355*	1.65008	.031	-8.8168	-.2903
	NORTH CENTRAL	.50536	1.48624	.986	-3.3346	4.3453
	WEST	2.30707	1.60714	.478	-1.8453	6.4594
WEST	NORTHEAST	-6.86063*	1.82445	.001	-11.5744	-2.1468
	NORTH CENTRAL	-1.80171	1.67773	.706	-6.1364	2.5330
	SOUTH	-2.30707	1.60714	.478	-6.4594	1.8453

\*. The mean difference is significant at the 0.05 level.

Report

READING STANDARDIZED SCORE

COMPOSITE GEOGRAPHIC REGI...	Mean	N	Std. Deviation	Variance	Skewness	Std. Error of Skewness
NORTHEAST	55.8918	100	9.86641	97.346	-.486	.316
NORTH CENTRAL	50.8328	100	10.01432	100.287	.224	.267
SOUTH	51.3382	100	10.00440	100.088	.246	.241
WEST	49.0311	100	9.81560	96.346	.502	.304
Total	51.5901	400	10.14505	102.922	.152	.141

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### V. Report a conclusion

The mean score of medical students at North-East University was significantly higher ( $55.89 \pm 9.86$ ) than the mean score of students at North-Central, West, and South Universities ( $50.83 \pm 10.01$ ,  $49.03 \pm 10.00$ ,  $51.33 \pm 9.8$  respectively).

# **Return to Exercise (17)**

### ANOVA

Time

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	91.467	2	45.733	4.467	.021
Within Groups	276.400	27	10.237		
Total	367.867	29			

### Multiple Comparisons

Dependent Variable: Time

	(I) Course	(J) Course	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
						Lower Bound	Upper Bound
Tukey HSD	Beginner	Intermediate	3.60000 <sup>*</sup>	1.43088	.046	.0523	7.1477
		Advanced	3.80000 <sup>*</sup>	1.43088	.034	.2523	7.3477
	Intermediate	Beginner	-3.60000 <sup>*</sup>	1.43088	.046	-7.1477	-.0523
		Advanced	.20000	1.43088	.989	-3.3477	3.7477
	Advanced	Beginner	-3.80000 <sup>*</sup>	1.43088	.034	-7.3477	-.2523
		Intermediate	-.20000	1.43088	.989	-3.7477	3.3477

### Descriptives

Time

	N	Mean	Std. Deviation	Std. Error	95% Confidence Interval for Mean		Minimum	Maximum
					Lower Bound	Upper Bound		
Beginner	10	27.2000	3.04777	.96379	25.0198	29.3802	22.00	33.00
Intermediate	10	23.6000	3.30656	1.04563	21.2346	25.9654	18.00	29.00
Advanced	10	23.4000	3.23866	1.02415	21.0832	25.7168	18.00	29.00
Total	30	24.7333	3.56161	.65026	23.4034	26.0633	18.00	33.00



# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **IV. Make your Decision regarding Research Hypotheses**

### ANOVA

Time

	Sum of Squares	df	Mean Square	F	Sig.
Between Groups	91.467	2	45.733	4.467	.021
Within Groups	276.400	27	10.237		
Total	367.867	29			

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### IV. Make your Decision regarding Research Hypotheses

**Reject Null Hypothesis  $H_0$**

p-value of F statistic = 0.021

P-value <  $\alpha$

0.021 < 0.05

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

### **V. Report a conclusion**

### Multiple Comparisons

Dependent Variable: Time

	(I) Course	(J) Course	Mean Difference (I-J)	Std. Error	Sig.	95% Confidence Interval	
						Lower Bound	Upper Bound
Tukey HSD	Beginner	Intermediate	3.60000 <sup>*</sup>	1.43088	.046	.0523	7.1477
		Advanced	3.80000 <sup>*</sup>	1.43088	.034	.2523	7.3477
	Intermediate	Beginner	-3.60000 <sup>*</sup>	1.43088	.046	-7.1477	-.0523
		Advanced	.20000	1.43088	.989	-3.3477	3.7477
	Advanced	Beginner	-3.80000 <sup>*</sup>	1.43088	.034	-7.3477	-.2523
		Intermediate	-.20000	1.43088	.989	-3.7477	3.3477

### Descriptives

Time

	N	Mean	Std. Deviation	Std. Error	95% Confidence Interval for Mean		Minimum	Maximum
					Lower Bound	Upper Bound		
Beginner	10	27.2000	3.04777	.96379	25.0198	29.3802	22.00	33.00
Intermediate	10	23.6000	3.30656	1.04563	21.2346	25.9654	18.00	29.00
Advanced	10	23.4000	3.23866	1.02415	21.0832	25.7168	18.00	29.00
Total	30	24.7333	3.56161	.65026	23.4034	26.0633	18.00	33.00

# One Factor ANOVA model - One Way ANOVA

## Comparing means from more than two Independent Populations

### V. Report a conclusion

Pharmacists who attended the Beginner course spent significantly longer duration of time to formulate the drug ( $27.20 \pm 3.04$  hours) compared with Pharmacists who attended the Intermediate and the Advanced courses ( $23.60 \pm 3.30$  hours, and  $23.40 \pm 3.23$  hours respectively).

# **One Factor ANOVA model - One Way ANOVA**

## **Comparing means from more than two Independent Populations**

**Run a One Way ANOVA (SPSS's One Way ANOVA Procedure)**



Comp  
(Par  
One P

Two P  
Indep

Depe

Analy



Thank you