

# Double-Beta Decay of $^{96}\text{Zr}$ and Double-Electron Capture of $^{156}\text{Dy}$ to Excited Final States

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Thesis Defense

March 25, 2015



# Outline

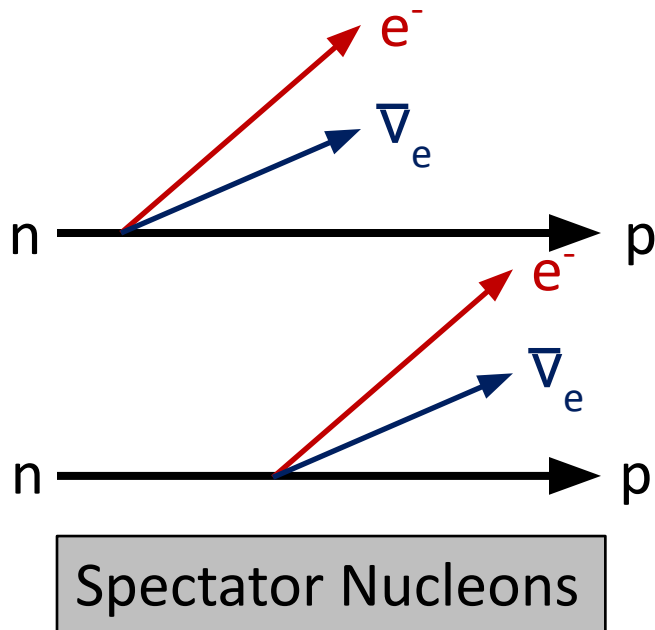
- Introduction to second-order weak decays
  - Nature of the neutrino
- Double- $\beta$  decay of  $^{96}\text{Zr}$ 
  - Two-coaxial HPGe apparatus
  - Analysis and results
- Resonantly enhanced double-electron capture of  $^{156}\text{Dy}$ 
  - Two-clover HPGe apparatus
  - Analysis and results
- Concluding remarks

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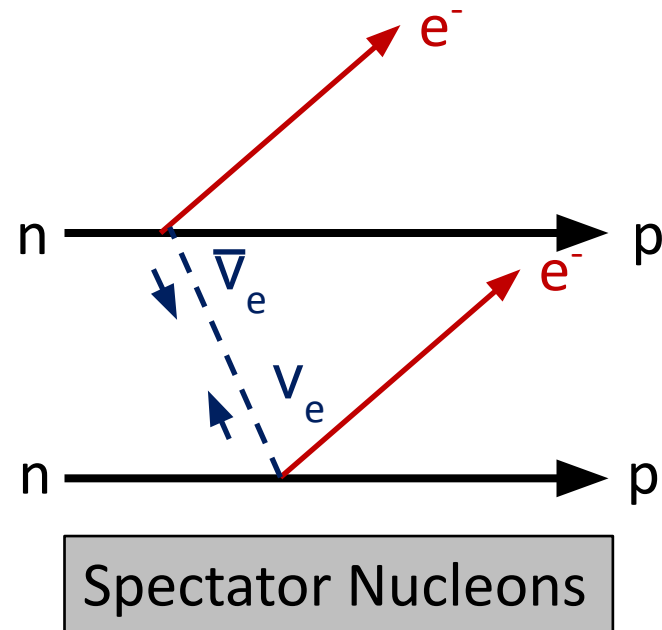
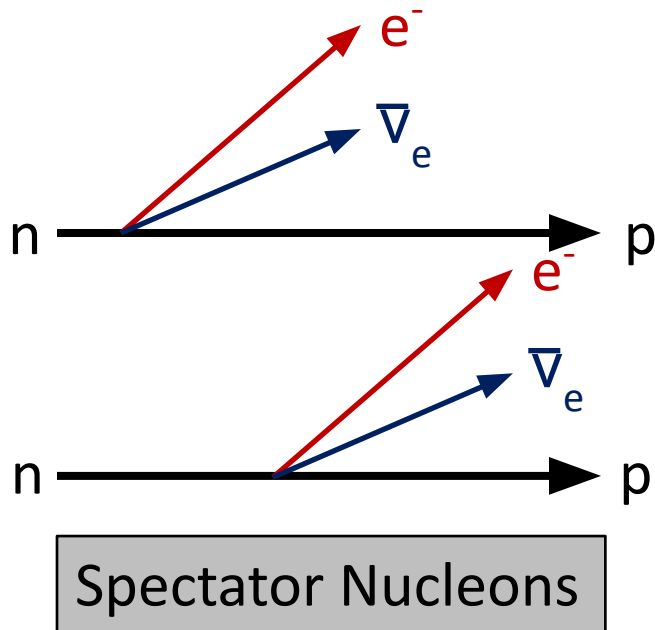
# Weak Nuclear Decays

- $\beta$  decay:  $n \rightarrow p + e^- + \bar{\nu}_e$  —
- Double- $\beta$  decay:  $2n \rightarrow 2p + 2e^- + 2\bar{\nu}_e$  —
- 35 nuclides capable of  $\beta\beta$ ; Observed in 11



# Neutrinoless- $\beta\beta$ Decay

- $n_1 \rightarrow p_1 + e^- + \text{“}v_e\text{”}$   
     $\text{“}v_e\text{”} + n_2 \rightarrow p_2 + e^-$
- Never observed (one questionable claim)



# Majorana Neutrinos

$0\nu\beta\beta$  requires:

- Helicity flip
  - Solved by massive neutrinos
- Neutrinos are their own antiparticle
  - Solved by Majorana neutrinos

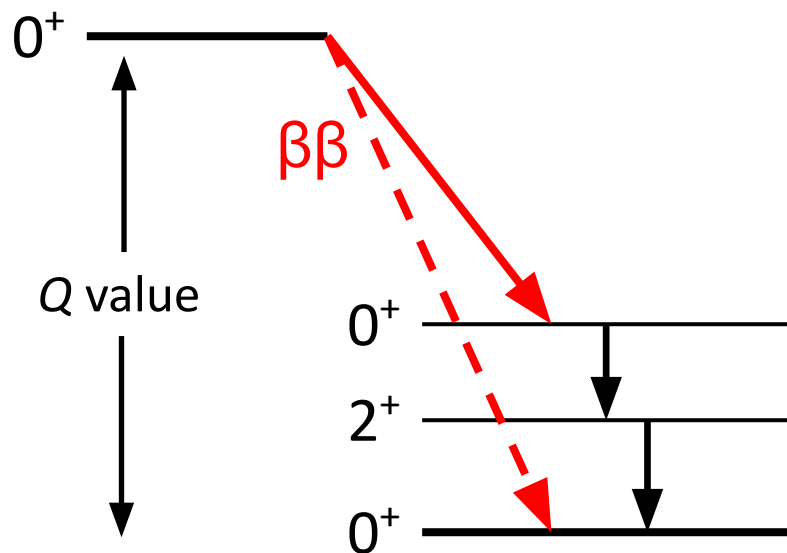
Why is this interesting?

- $0\nu\beta\beta$  violates lepton number conservation
- Allows measurement of neutrino mass:
  - $\lambda_{2\nu\beta\beta} = G_{2\nu} |M_{2\nu}|^2$
  - $\lambda_{0\nu\beta\beta} = G_{0\nu} |M_{0\nu}|^2 \langle m_\nu \rangle^2$
- Best limits on  $^{76}\text{Ge}$  (GERDA)
  - $T_{1/2}(2\nu) = 1.84^{+0.14}_{-0.10} \times 10^{21} \text{ yr}$
  - $T_{1/2}(0\nu) > 2.1 \times 10^{25} \text{ yr}$
  - $m_\nu < 200\text{-}400 \text{ meV}$

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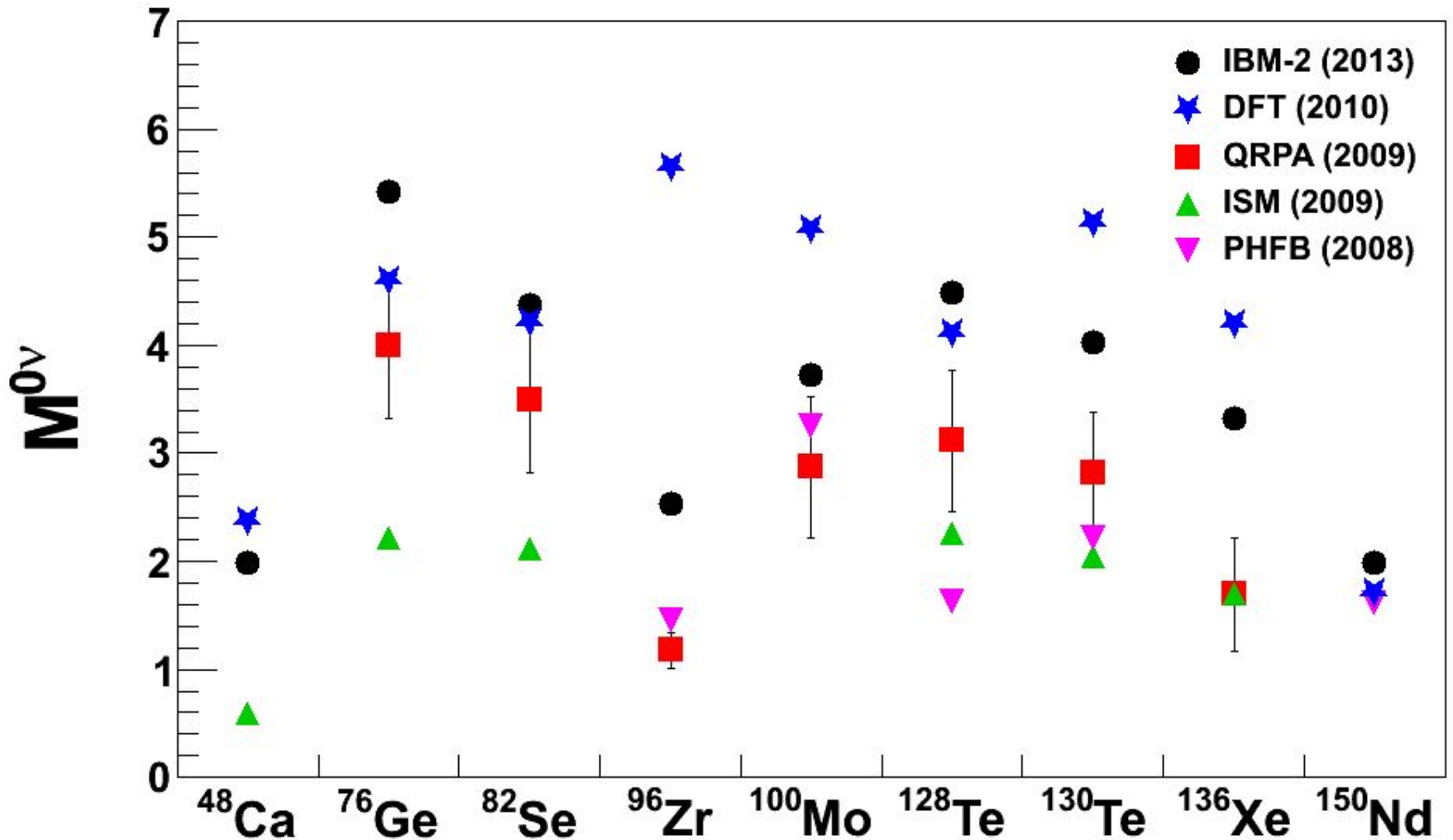
# $2\nu\beta\beta$ to Excited Final States



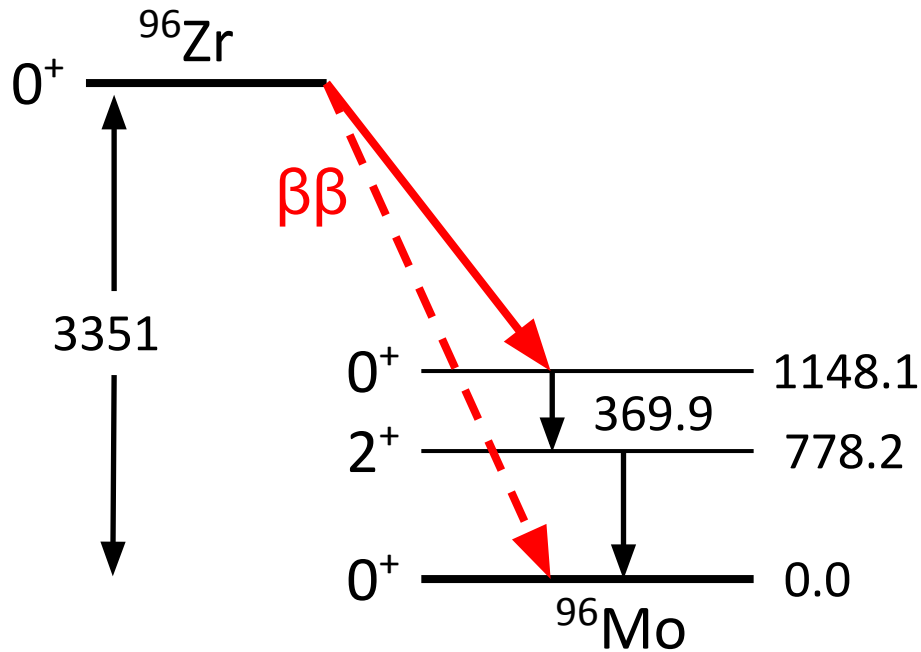
- $\lambda_{2\nu\beta\beta} = G_{2\nu} |M_{2\nu}|^2$
- $\lambda_{0\nu\beta\beta} = G_{0\nu} |M_{0\nu}|^2 \langle m_\nu \rangle^2$
- $0\nu\beta\beta$  matrix elements must be calculated
  - Tuned to reproduce  $2\nu\beta\beta$  matrix elements
  - Decays to excited final states provides an additional constraint



# Nuclear Matrix Elements

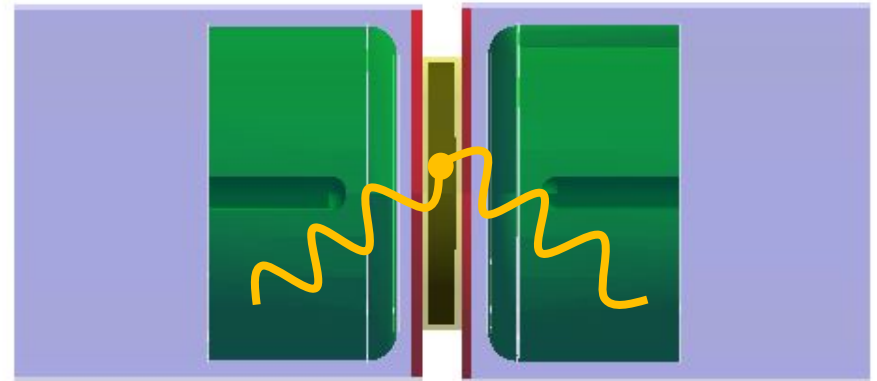


# Experimental Technique



An excited state decay  
with two coincident  $\gamma$ s

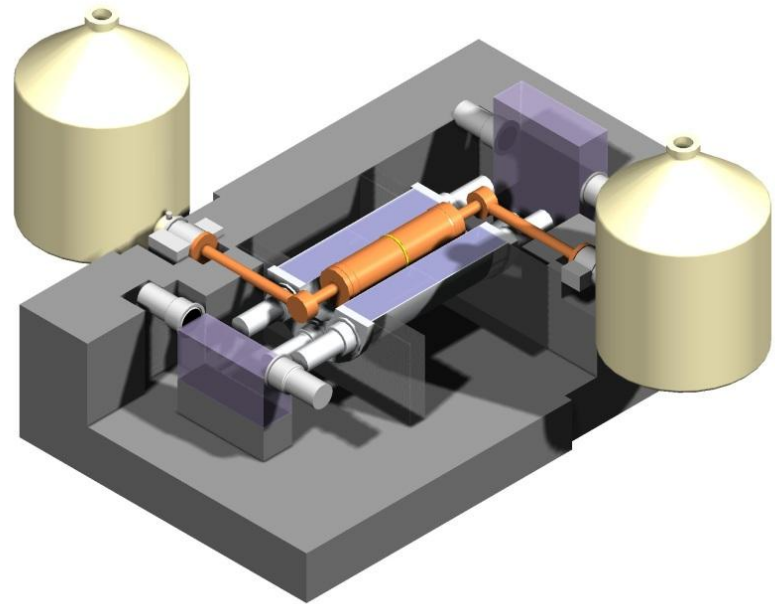
All energies in keV



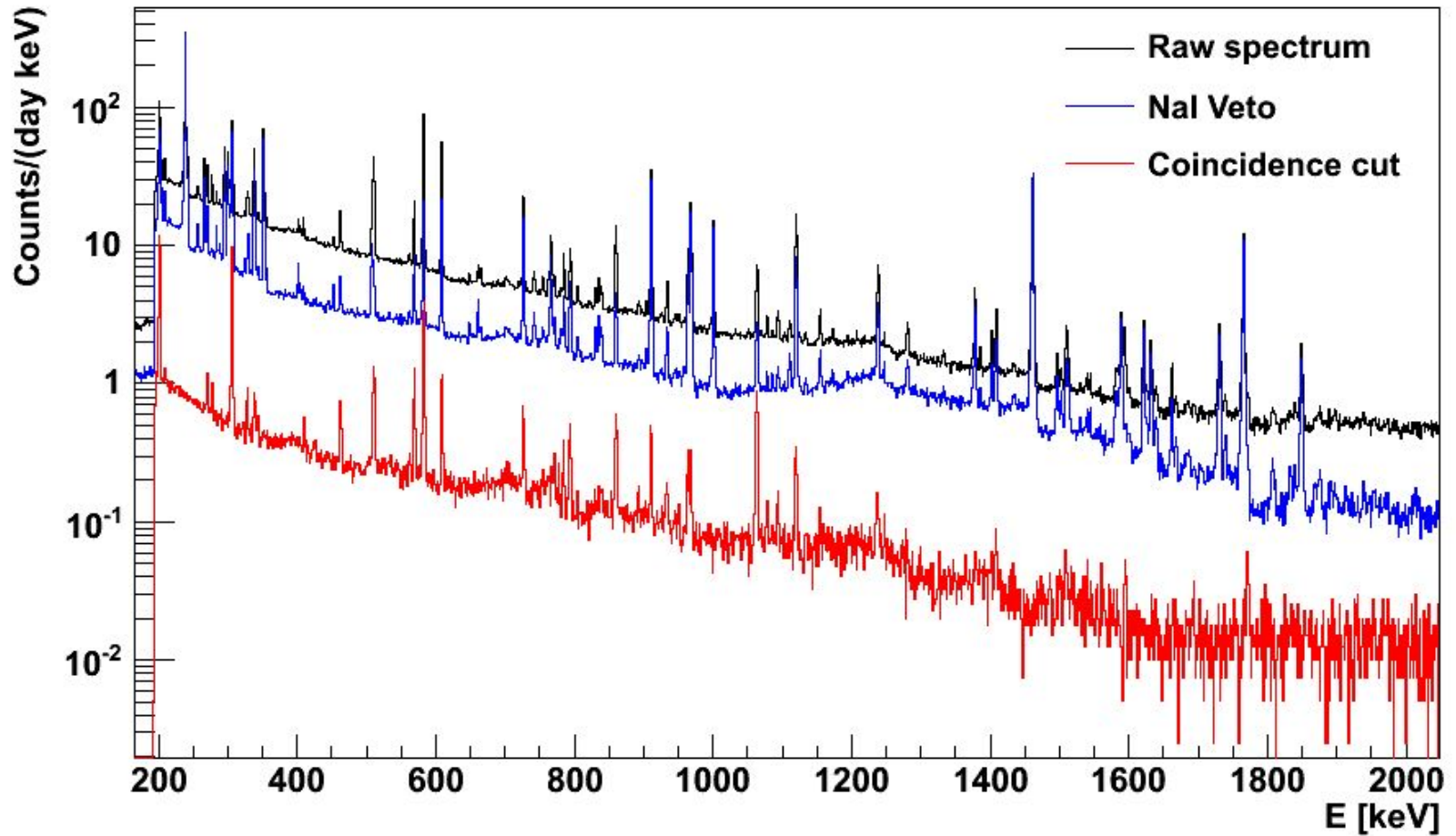
Sample between two  
coaxial-HPGe detectors

# Two-Coaxial HPGe Apparatus

- Two-coaxial HPGe detectors sandwich sample
- Active veto
  - NaI annulus for Compton suppression
  - Plastic end caps
- Passive shielding
  - $\frac{3}{4}$ " OFHC copper
  - 6" lead

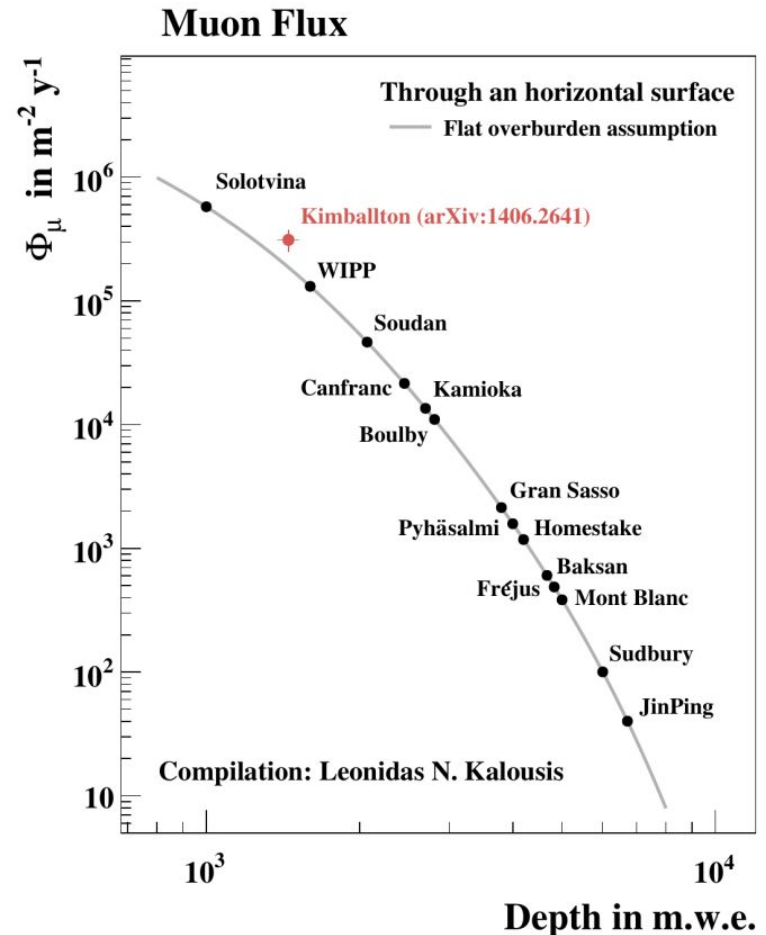


# HPGe Spectrum



# Kimballton Underground Research Facility (KURF)

- Active limestone mine
- Ripplemead, Va
  - 30 minutes from VT
  - 4 hours from Duke
- 1700 feet limestone overburden
- 1450 m.w.e. shielding from cosmic rays
- Internet access allows experiments to be controlled remotely





# KURF



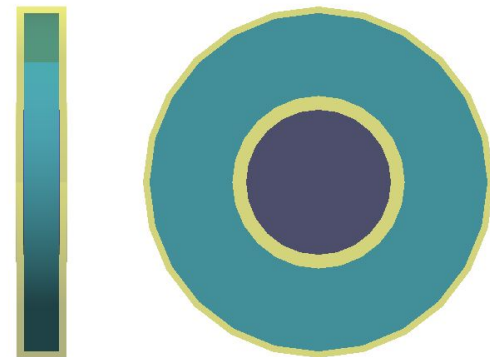
# KURF Lab



- A. micoLENS (VT)
- B. Neutron Spectroscopy (Maryland)
- C. Present experiment (Duke)
- D. Low background radioassays (UNC)
- E. MALBEK (UNC)
- F. Low activity Ar (Princeton)
- G. Watchboy (LLNL)

# $^{96}\text{Zr}$ Sample

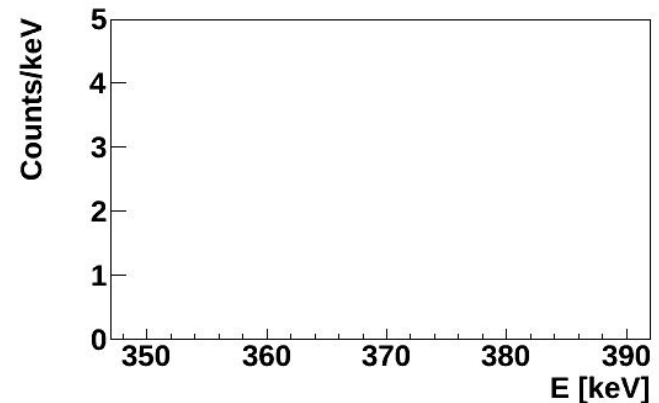
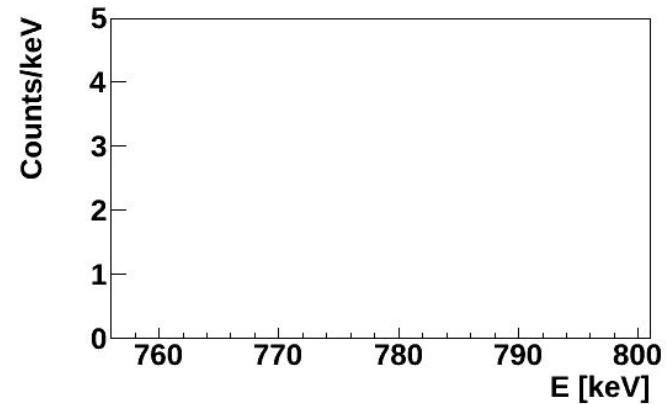
- $^{150}\text{Nd}$  and  $^{100}\text{Mo}$  are the only two nuclides where  $\beta\beta$  decay to an excited state has been observed
- $^{96}\text{Zr}$  as a  $\beta\beta$ -decay candidate
  - High  $Q$  Value (3347 keV)
  - Ground state decay measured by NEMO collaboration
    - $T_{1/2} = [2.35 \pm 0.14 \text{ (stat)} \pm 0.16 \text{ (syst)}] \times 10^{19} \text{ yr}$
  - 2.8% natural abundance
- $\text{ZrO}_2$  sample from ORNL:
  - 7.283 g enriched to 91.39%
  - 26.968 g enriched to 64.18%
  - Total of 17.914 g  $^{96}\text{Zr}$





# $^{96}\text{Zr}$ $2\nu\beta\beta$ Data

- $^{96}\text{Zr}$  source in place
  - 623.8 days (1.92 yr) of data
  - 4 events in  $\pm 3\sigma$  ROI
  - 2 events in  $\pm 2\sigma$  ROI
  - Consistent with background
- Backgrounds
  - $^{212}\text{Bi}$  ( $^{232}\text{Th}$  decay chain)
  - Compton scattering
  - Discriminate with energy resolution



# Limit Setting

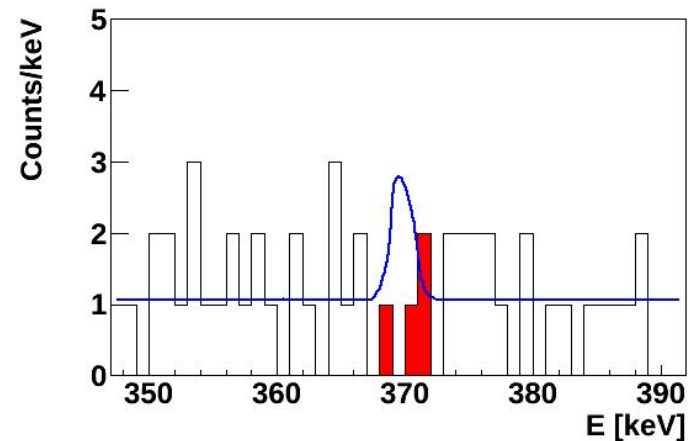
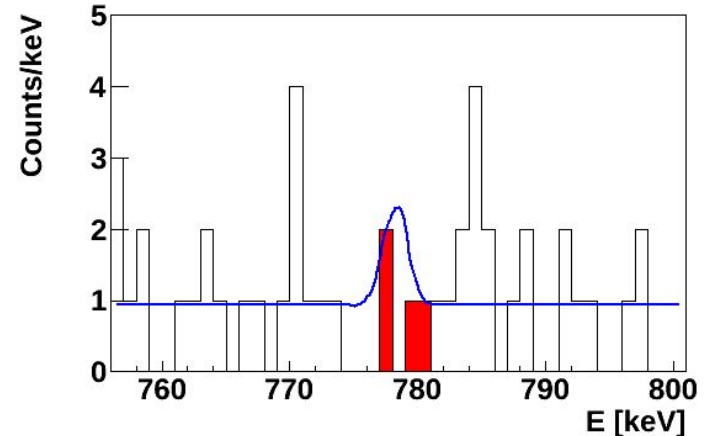
- $T_{1/2} > \frac{\ln(2)N_0 t f_b \epsilon}{N_d}$ 
  - $N_0$  Number of nuclei
  - $t$  Exposure time
  - $f_b$  Branching ratio
  - $\epsilon$  Efficiency
  - $N_d$  Statistical factor
- Method of Feldman-Cousins used for confidence intervals

## Limit versus sensitivity

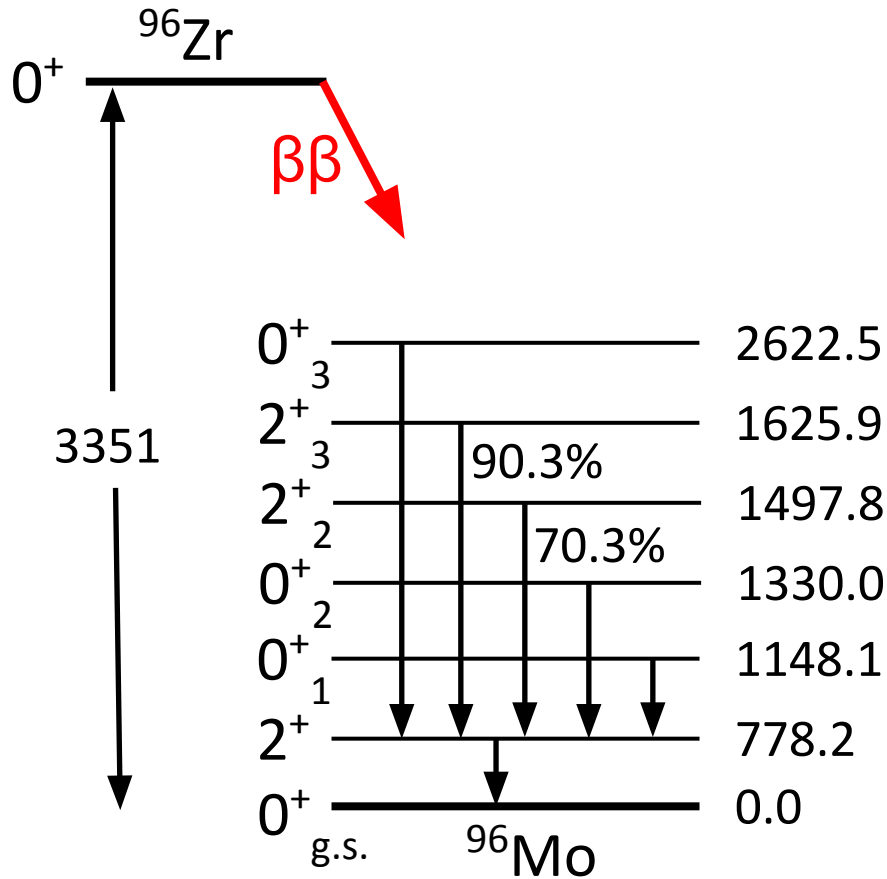
- Limit:  $N_d(N_{\text{obs}}, N_{\text{bkgd}})$
- Sensitivity:  $N_s(N_{\text{bkgd}})$ 
  - The mean limit  $N_d$  reported by an experiment with background  $N_{\text{bkgd}}$  and no signal

# New limits

- Limit at 90% C.L.
  - $T_{1/2} > 3.2 \times 10^{20}$  yr
  - Sensitivity:  
 $T_{1/2} > 2.8 \times 10^{20}$  yr
- Previous limit
  - $T_{1/2} > 6.8 \times 10^{19}$  yr
  - Used single well-type HPGe; no coincidence
  - Limited by high background and uncertainty from statistical fits



# To Higher Excited States

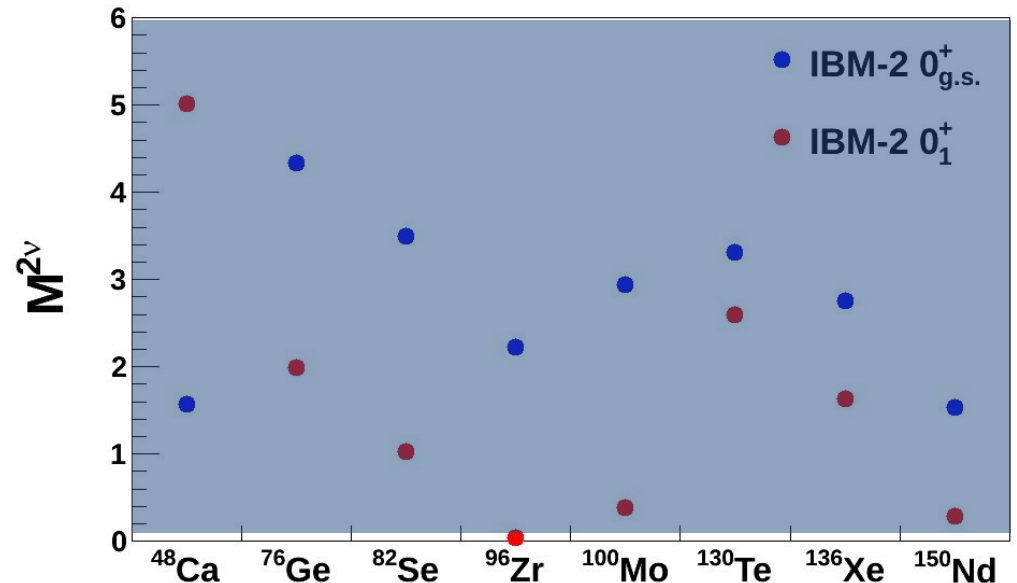


$J^\pi$	E [keV]	$T_{1/2}$ [yr] C.I.	$T_{1/2}$ [yr] Sensitivity
$0^+$ <sub>1</sub>	1148.1	$> 3.2 \times 10^{20}$	$> 2.8 \times 10^{20}$
$0^+$ <sub>2</sub>	1330.0	$> 1.4 \times 10^{20}$	-
$2^+$ <sub>2</sub>	1497.8	$> 1.0 \times 10^{20}$	-
$2^+$ <sub>3</sub>	1625.9	$> 1.2 \times 10^{20}$	-
$0^+$ <sub>3</sub>	2622.5	$> 1.1 \times 10^{20}$	$> 1.0 \times 10^{20}$

All energies in keV

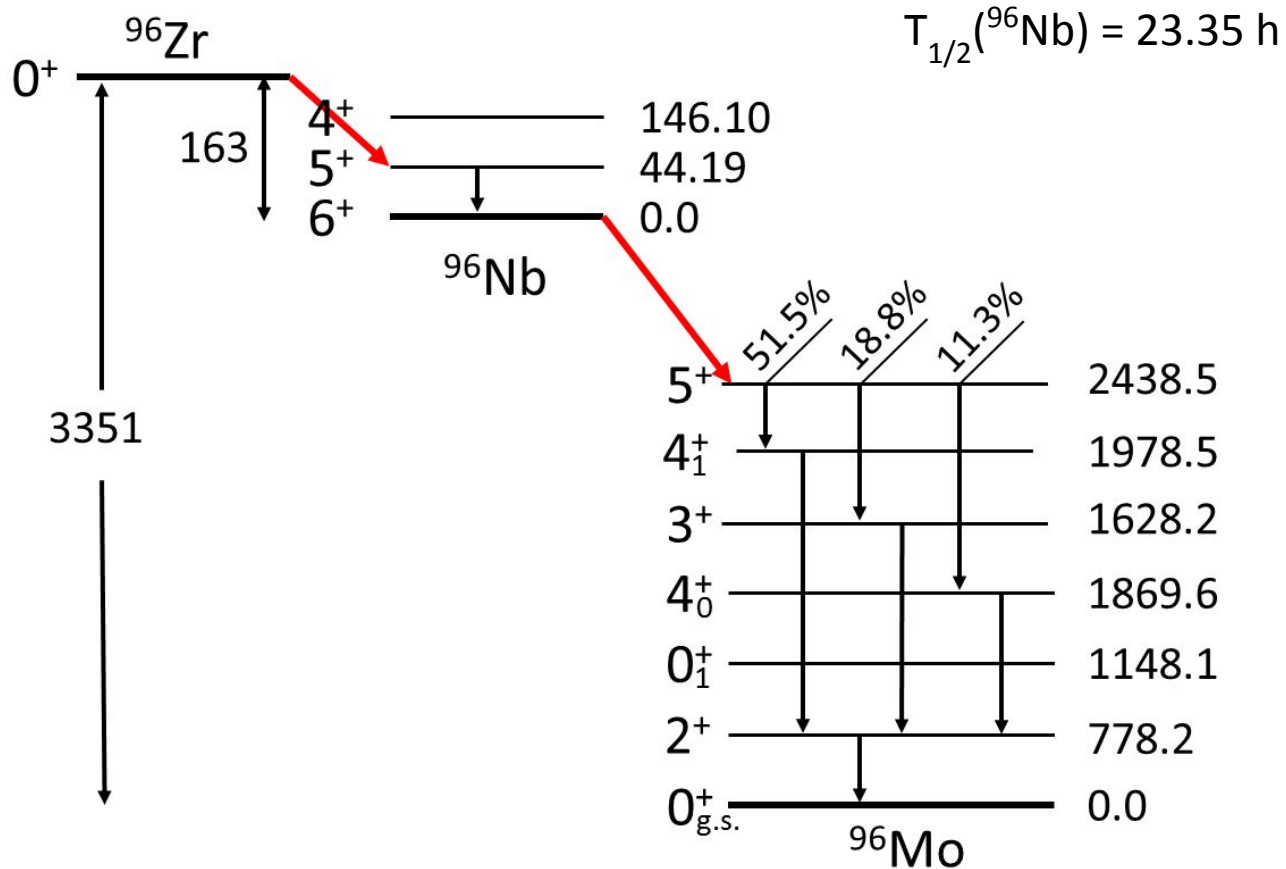
# Limits on NME

- $\lambda_{2\nu\beta\beta} = G_{2\nu\beta\beta} |M_{2\nu\beta\beta}|^2$
- Experiment:  
 $|M_{2\nu\beta\beta} (0_1^+)| < 0.11$
- IBM-2 theory<sup>1</sup>:  
 $|M_{2\nu\beta\beta} (0_1^+)| = 0.04$



<sup>1</sup> J. Barea, J. Kotila, and F. Iachello, Phys. Rev. C 87, 014315 (2013)

# Single- $\beta$ decay of $^{96}\text{Zr}$



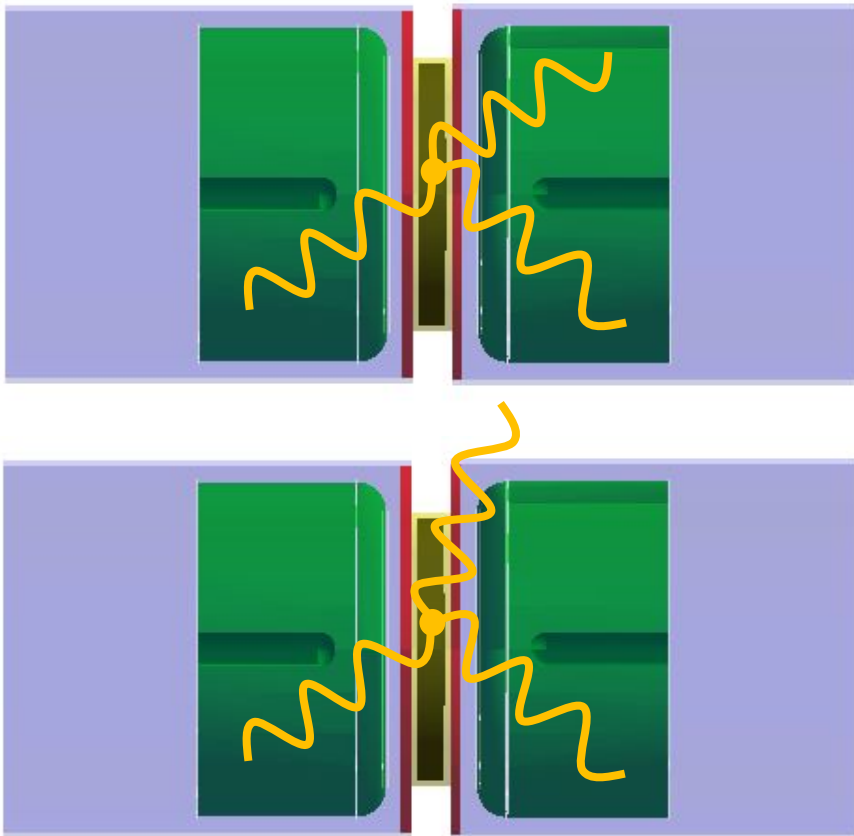
All energies in keV

# Experimental Motivation

- Help understand the nuclear structure of  $^{96}\text{Zr}$
- Possible background for experiments searching for  $0\nu\beta\beta$  in  $^{96}\text{Zr}$
- Previous experiments used a single HPGe detector
  - $\beta$  decay forms an irreducible background for excited state decays
- Using the coincidence technique in present work can unambiguously distinguish  $\beta$  decay and  $\beta\beta$  decay

# Limits on Single- $\beta$ decay of $^{96}\text{Zr}$

Three coincident  $\gamma$ s



- Present Experiment
  - Sum three most intense decay modes
    - Branching ratio 81.6%
  - 13 events in ROI , expect 11.1 events background
  - $T_{1/2} > 2.4 \times 10^{19}$  yr
- Previous measurement
  - $T_{1/2} > 3.8 \times 10^{19}$  yr
- Theory<sup>2</sup> (QRPA)
  - $T_{1/2} = 2.4 \times 10^{20}$  yr

<sup>2</sup> H. Heiskanen, M.T. Mustonen, and J. Suhonen, J. Phys. Rev. **G** 34, 837 (2007)



# Outline

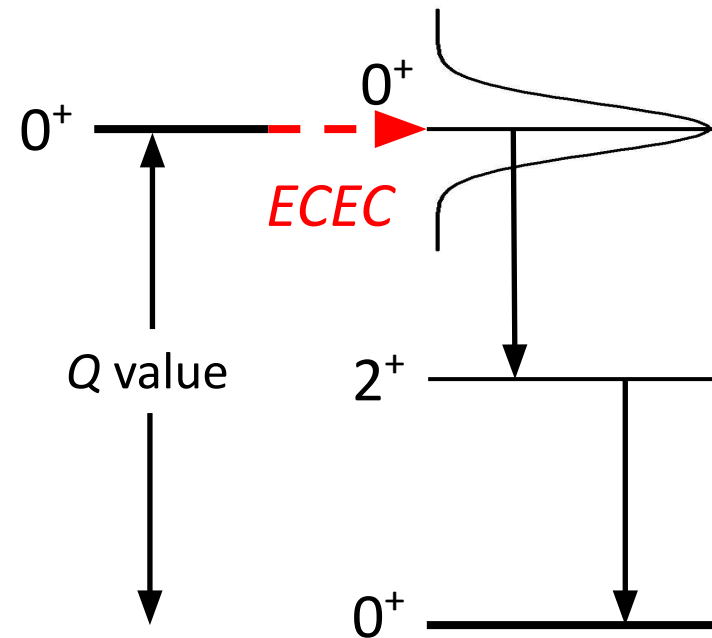
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# Resonant ECEC to Excited Final States

- Nucleus captures atomic electron
  - $p + e^- \rightarrow n + \nu_e$
- Second-order nuclear decay
  - $^{156}\text{Dy} + 2e^- \rightarrow ^{156}\text{Gd} + 2\nu_e$
- For Majorana neutrinos
  - $^{156}\text{Dy} + 2e^- \rightarrow ^{156}\text{Gd}^*$
  - Possible experimental alternative to  $0\nu\beta\beta$
- No outgoing particles
  - No method to dissipate excess energy
  - Requires “monumental coincidence” that an excited nuclear state in the daughter nucleus is degenerate with the  $Q$  value

# Resonant ECEC to Excited Final States

- Two neutrino mode strongly disfavored by phase space
- Observation would be evidence for Majorana neutrinos
- Rate enhancement if the  $Q$  value is degenerate with an energy level



# ECEC in $^{156}\text{Dy}$

$E_Y$ [keV]	$I^\pi$	Electron Orbitals	$(B_{XY})$ [keV]	$\Delta$ [keV]	$\Gamma_{XY}$ [eV]	EF	$ \Psi_x ^2 \Psi_y ^2$
1946.375	$1^-$	$KL_1$	58.822(8)	0.75(10)	26	$4.1 \times 10^6$	$1.23 \times 10^{10}$
1952.385	$0^-$	$KM_1$	52.192(8)	1.37(10)	35	$1.7 \times 10^6$	$2.68 \times 10^{10}$
1988.5	$0^+$	$L_1L_1$	16.914(8)	0.54(24)	8	$2.5 \times 10^6$	$1.65 \times 10^{10}$
2003.749	$2^+$	$M_1N_3$	2.160(24)	0.04(10)	15	$7.7 \times 10^8$	$1.52 \times 10^{11}$

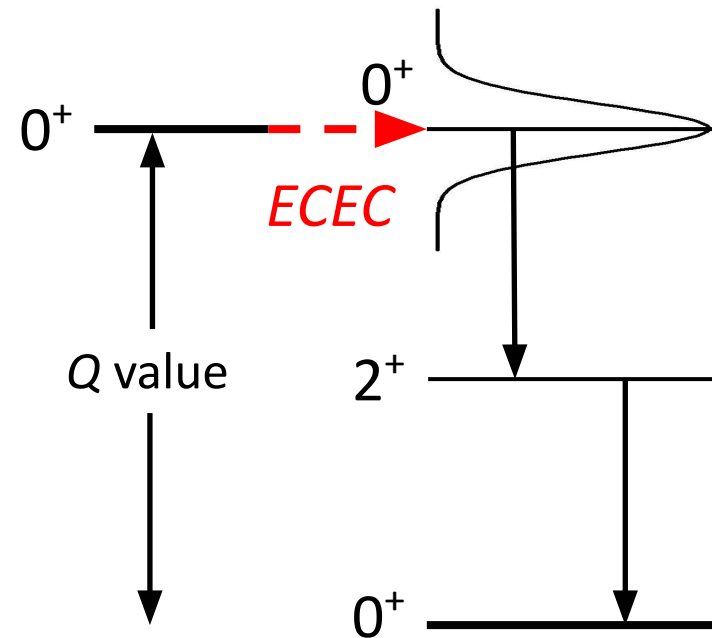
$$EF = \frac{\Gamma_{XY}}{\Delta^2 + \frac{1}{4}\Gamma_{XY}^2}$$

$$\lambda^{0vee} = G_{0vee} |M^{0vee}| \langle M_\nu \rangle^2 (EF)$$

<sup>3</sup> S. Eliseev *et al.*, Phys. Rev. C 84, 012501(R) (2011)

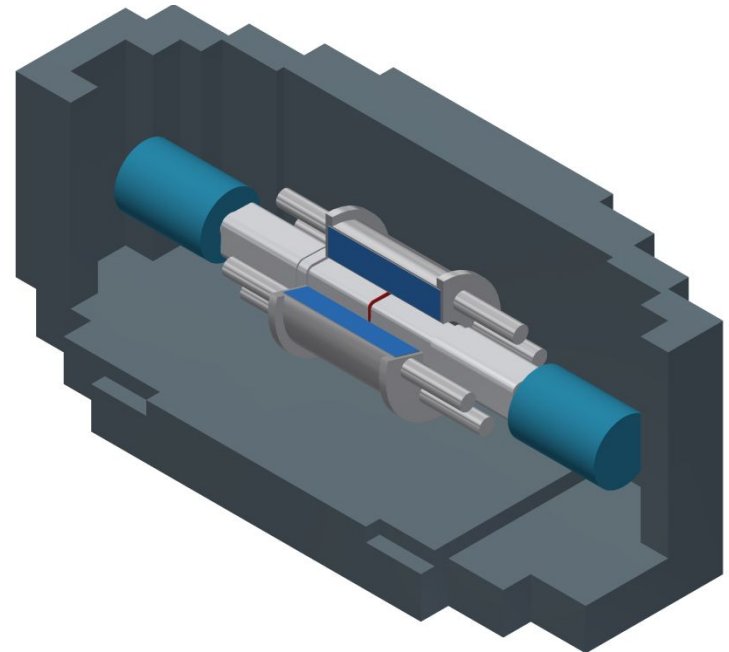
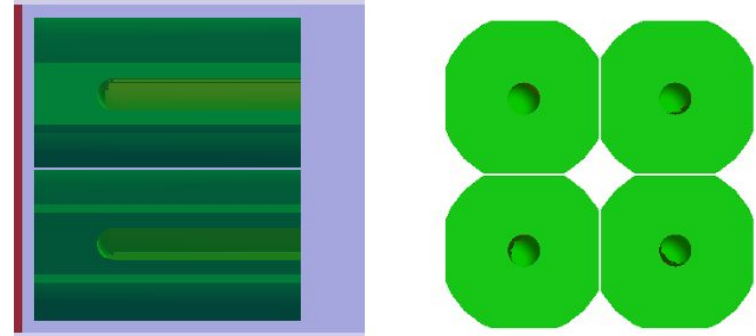
# Resonant ECEC in $^{156}\text{Dy}$

- $^{156}\text{Dy}$  is currently one of the most promising candidates
  - Extremely low natural abundance: 0.056%
- Enriched sample from ORNL
  - 1.15 grams
  - Enriched to 21%
  - Total = 213 mg
- Detectable only by  $\gamma$ -ray transitions in daughter



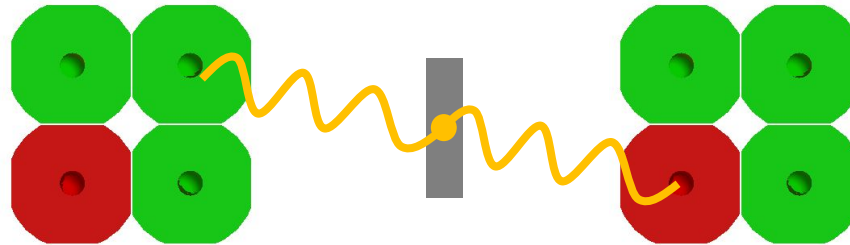
# New Two-Clover HPGe Apparatus

- Use two clover HPGe detectors
  - Segmented
  - Larger volume
- NaI annulus
- 6-8" Lead shielding
- Timeline
  - Built in 2010
  - Characterization and efficiency measurements 2010-2012
  - Moved to KURF Fall 2012
  - $^{156}\text{Dy}$  sample 2013-2014



# Coincidence and Addback

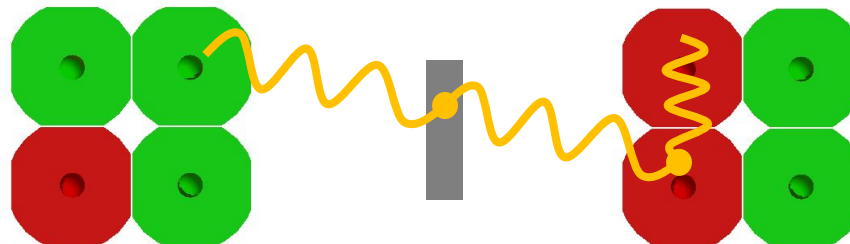
- External coincidences



- Internal coincidences



- Addback coincidences



# Previous Searches

## Belli *et al.*<sup>4</sup>

- 322 g natural Dy<sub>2</sub>O<sub>3</sub>
- 157 mg <sup>156</sup>Dy
- 104.7 days
- Single HPGe at LNGS

## This work

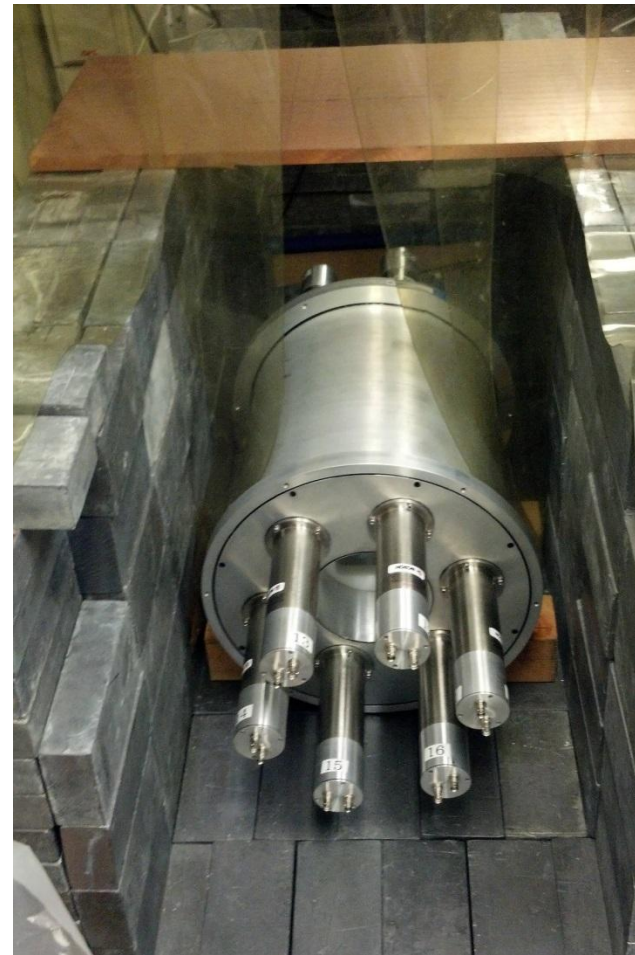
- Enriched sample
  - Reduce  $\gamma$ -ray attenuation by sample
- Cover a larger solid angle
- Ability to look at coincidence  $\gamma$ -rays from cascades
  - Reduce background

<sup>4</sup> P. Belli *et al.*, J. Phys. Conf. Ser. **375**, 042024 (2012)

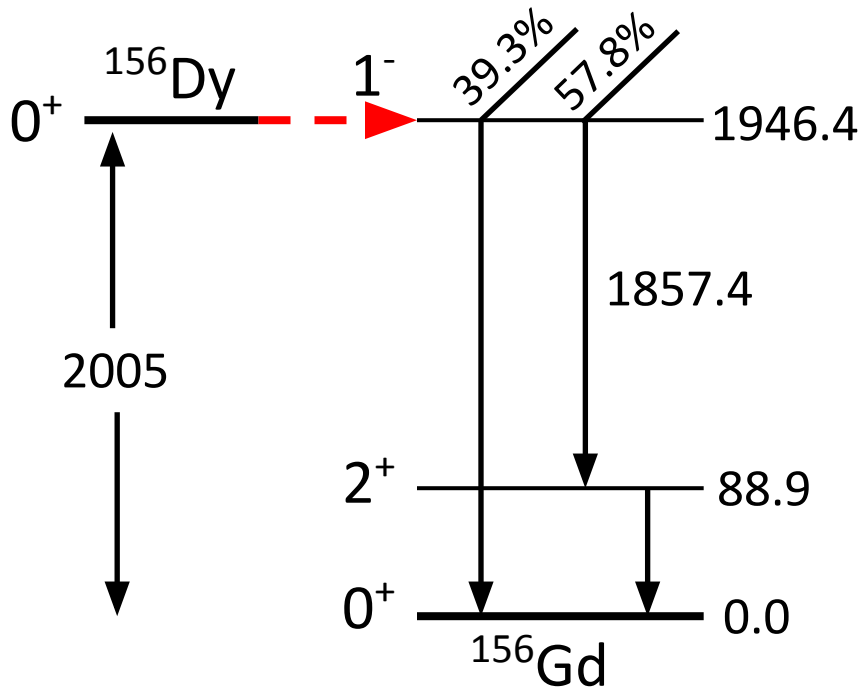


# $^{156}\text{Dy}$ Data Acquisition

- Run #1
  - 151.95 mg
  - 99.13 days
- Run #2
  - 213.57 mg
  - 132.82 days
- Presented results are the sum of both runs
  - 0.119 g·yr of exposure



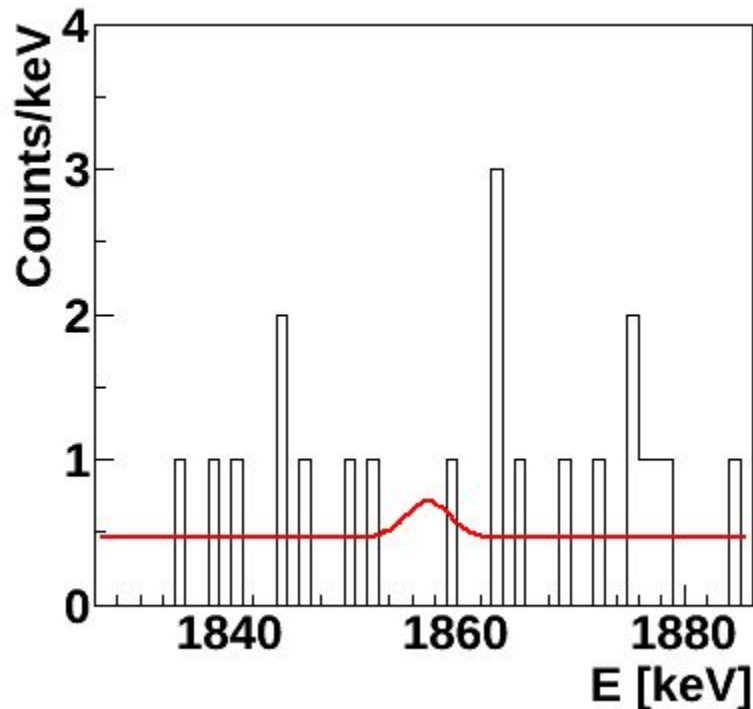
# Capture to the 1946 keV State



- Branching ratio 57.8%
- Gate on 88.9 keV  $\gamma$  ray in one clover segment
- Allow singles and addback on 1857 keV

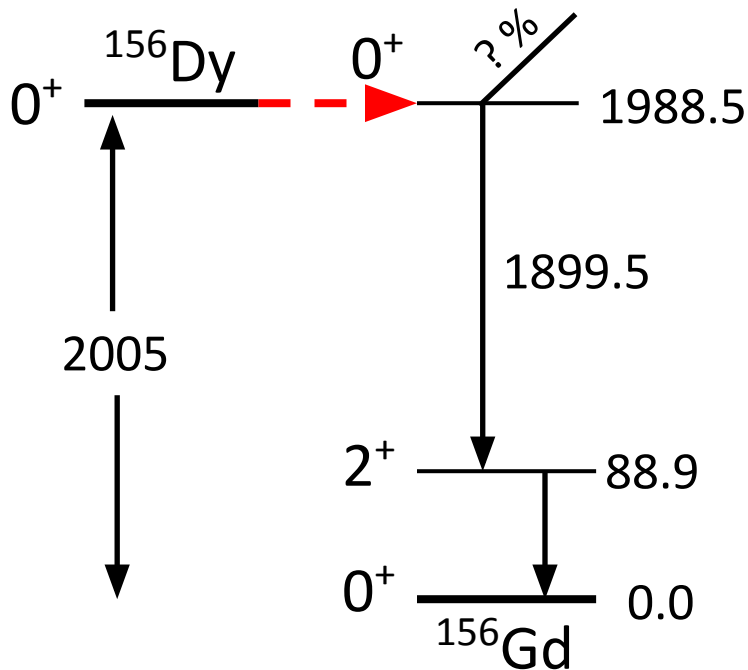
All energies in keV

# Capture to the 1946 keV State



- Branching ratio 57.8%
- Gate on 88.9 keV  $\gamma$  ray in one clover segment
- Allow singles and addback on 1857 keV
- 1 event in ROI, expected 4.12 events background
  - $N_d = 1.275$
  - $N_s = 4.86$

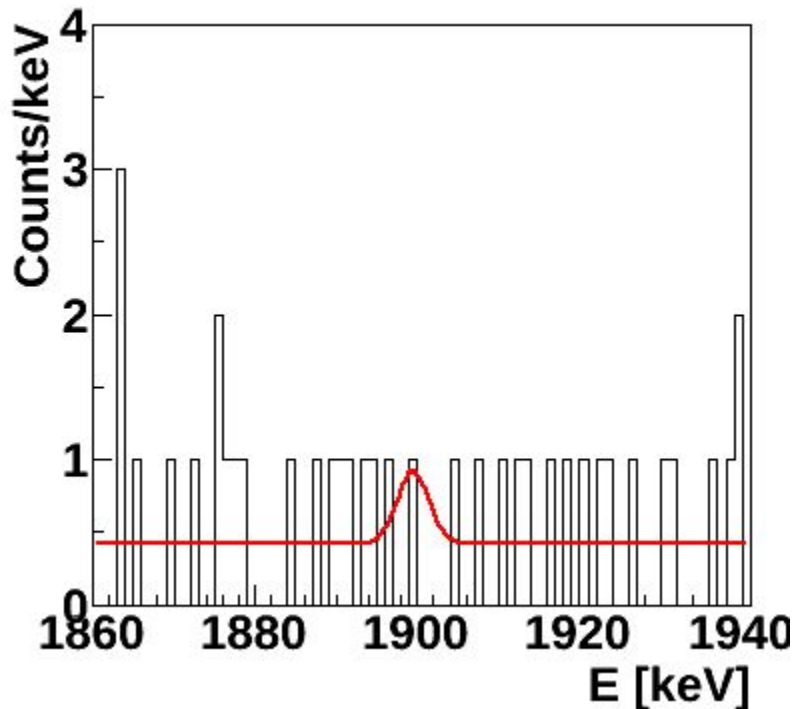
# Capture to the 1988 keV State



All energies in keV

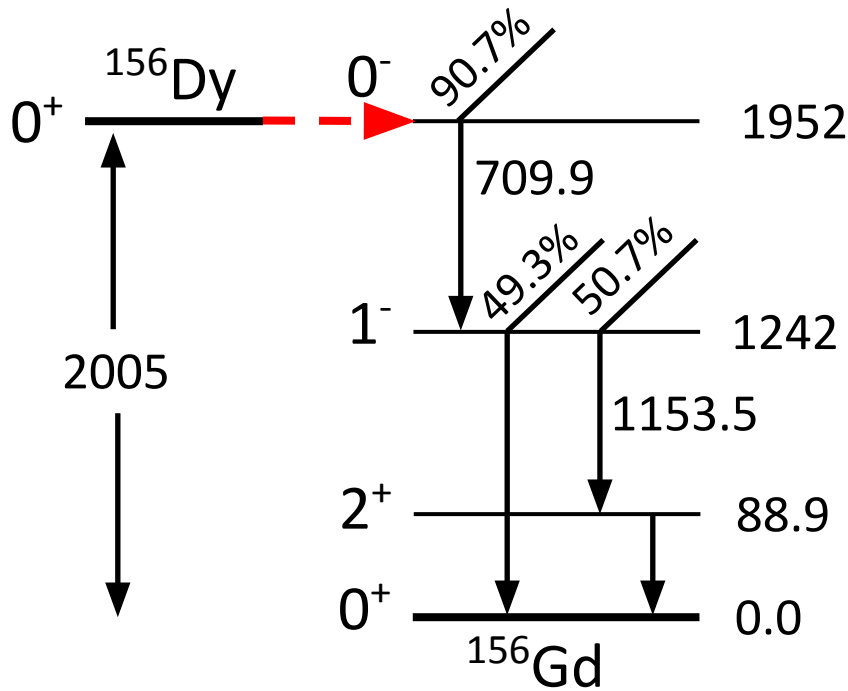
- No nuclear data available on state
- Assume a strong transition to the  $2^+$  state
  - Branching ratio = 100%
- Gate on 88.9 keV  $\gamma$  ray in one clover segment

# Capture to the 1988 keV State



- No nuclear data available on state
- Assume a strong transition to the  $2^+$  state
  - Branching ratio = 100%
- Gate on 88.9 keV  $\gamma$  ray in one clover segment
- 2 events in ROI, expected 3.76 events background

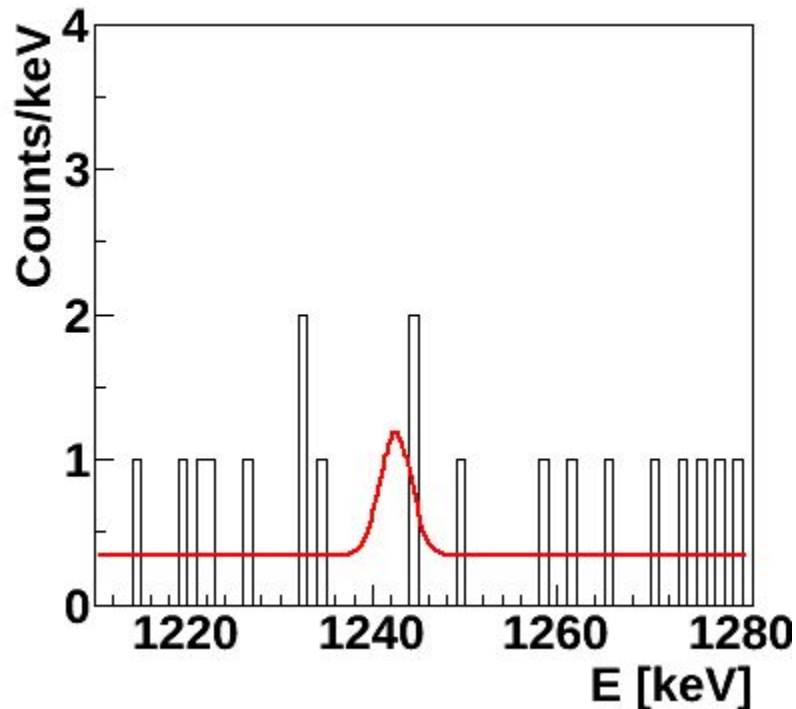
# Capture to the 1952 keV State



All energies in keV

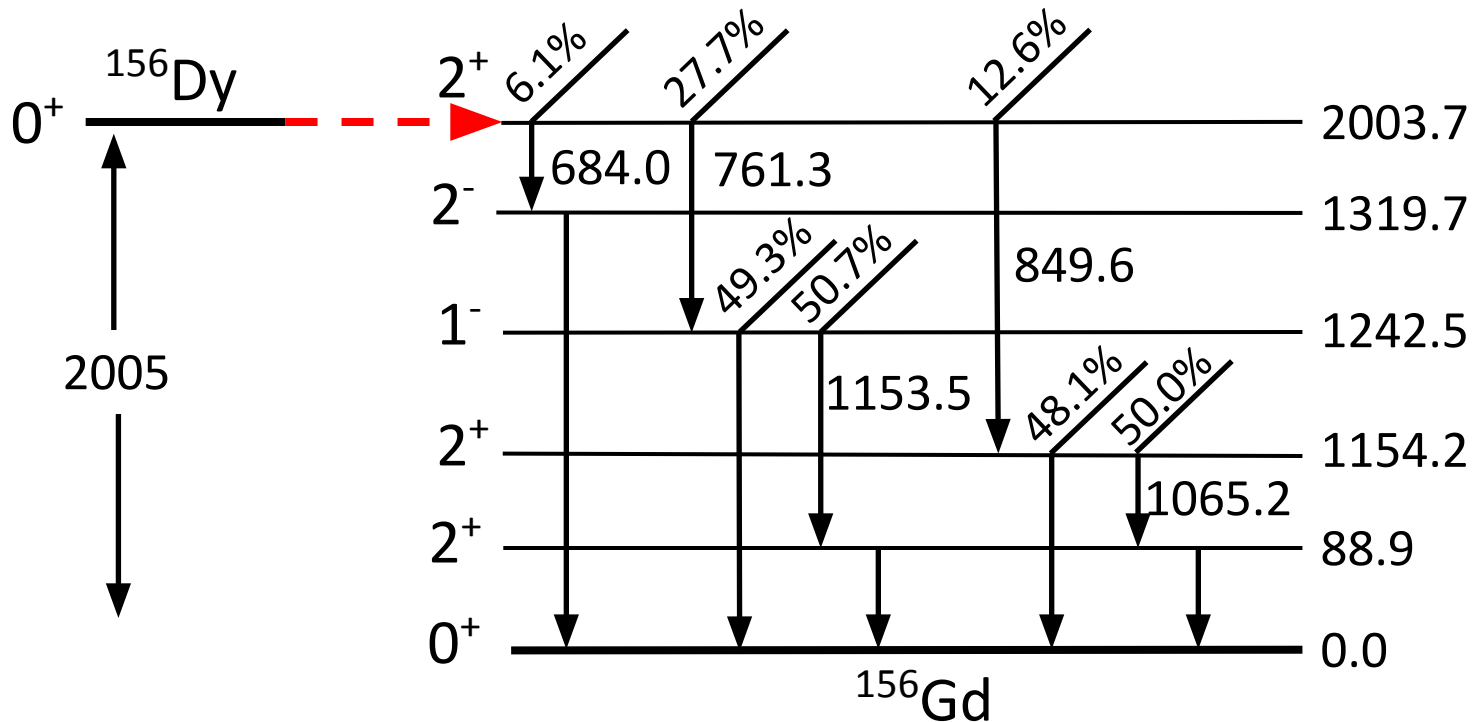
- Two  $\gamma$ -ray decay mode
  - Branching ratio 44%
- Allow addback on both  $\gamma$ s
- Three  $\gamma$ -ray decay mode may be reconstructed in addback
  - Additional 26.3% increase to sensitivity

# Capture to the 1952 keV State



- Two  $\gamma$ -ray decay mode
  - Branching ratio 44%
- Allow addback on both  $\gamma$ s
- Three  $\gamma$ -ray decay mode may be reconstructed in addback
  - Additional 26.3% increase to sensitivity
- Given 709.9 keV event
- 2 events in ROI, expected 2.38 events background

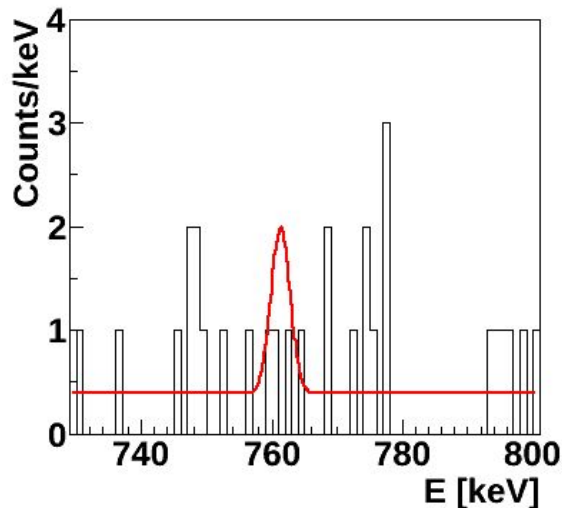
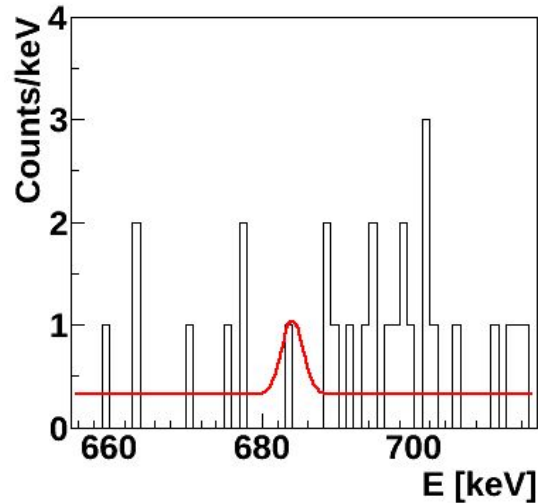
# Capture to the 2003.7 keV State



All energies in keV



# Capture to the 2003.7 keV State



- Two  $\gamma$ -ray decays
  - Branching ratio 25.8%
- Including contribution from ternary  $\gamma$ -ray decays
  - Increase sensitivity by 18%
- Top: in coincidence with 1319.7
- Bottom: in coincidence with 1242.5
- Sum all three decay modes
  - 6 events in ROI, expected 5.64 events background

# Summary of Results

$J^\pi$	E [keV]	$T_{1/2}$ [yr] This work C.I.	$T_{1/2}$ [yr] This work Sensitivity	$T_{1/2}$ [yr] Previous limit <sup>4</sup>
$1^-$	1946.4	$> 1.0 \times 10^{18}$	$> 2.8 \times 10^{17}$	$> 9.6 \times 10^{15}$
$0^-$	1952.4	$> 2.2 \times 10^{17}$	$> 1.9 \times 10^{17}$	$> 2.6 \times 10^{16}$
$0^+$	1988.5	$> 9.5 \times 10^{17}$	$> 5.0 \times 10^{17}$	$> 1.9 \times 10^{16}$
$2^+$	2003.7	$> 6.7 \times 10^{16}$	-	$> 3.0 \times 10^{14}$

<sup>4</sup> P. Belli *et al.*, J. Phys. Conf. Ser. **375**, 042024 (2012)

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- **Concluding remarks**

# The Future

- Many  $0\nu\beta\beta$  experiments are currently underway with more about to begin
  - Underway: EXO-200, GERDA, KamLAND-Zen
  - Near future: CUORE, Majorana, SNO+
- Collaborations are progressing towards 1-ton scale experiment
- Goals:
  - Illuminate the Dirac or Majorana nature of the neutrino
  - Set limits on the neutrino mass

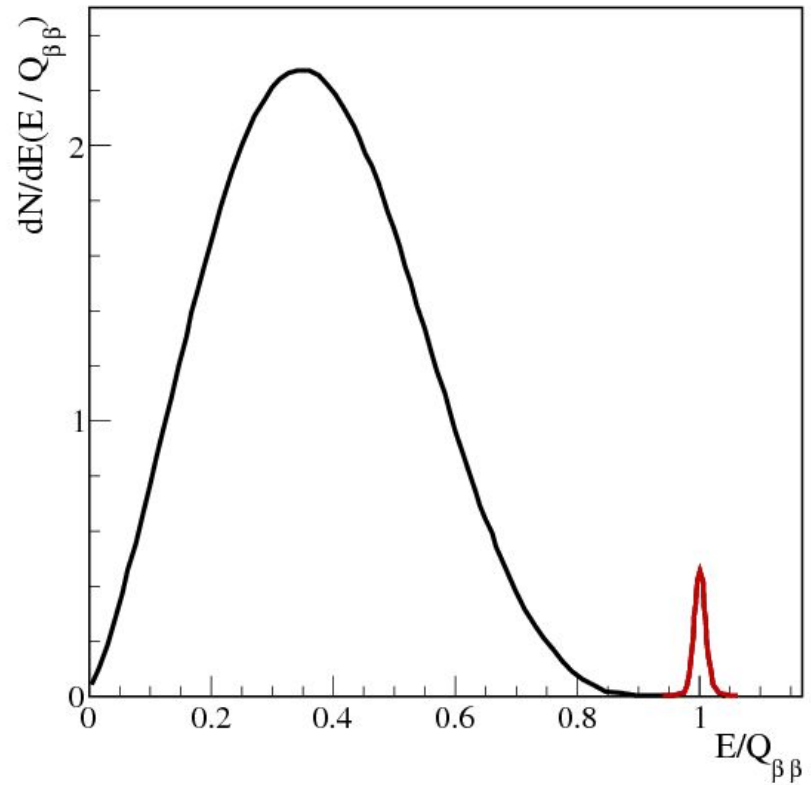
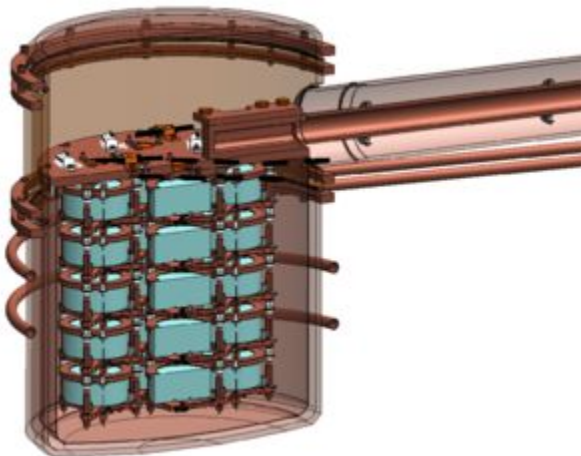
# Summary

- $\beta\beta$  of  $^{96}\text{Zr}$  to excited states
  - Improve theoretical understanding of NMEs
    - Reduce uncertainty
  - Excited state decay modes could help verify discovery
    - Decreased background by coincidence technique
  - $T_{1/2}(\beta\beta) > [1.0-3.2] \times 10^{20}$  yr
  - $T_{1/2}(\beta) > 2.4 \times 10^{19}$  yr
- $0\nu ECEC$  to excited states
  - Experimental alternative to  $0\nu\beta\beta$
  - Resonant enhancement could greatly increase experimental sensitivity
  - $T_{1/2} > [0.67-10] \times 10^{17}$  yr

Thank you

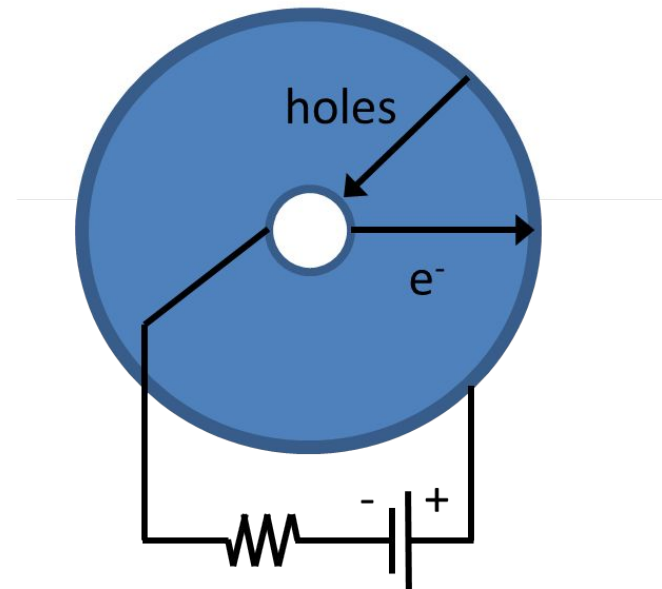
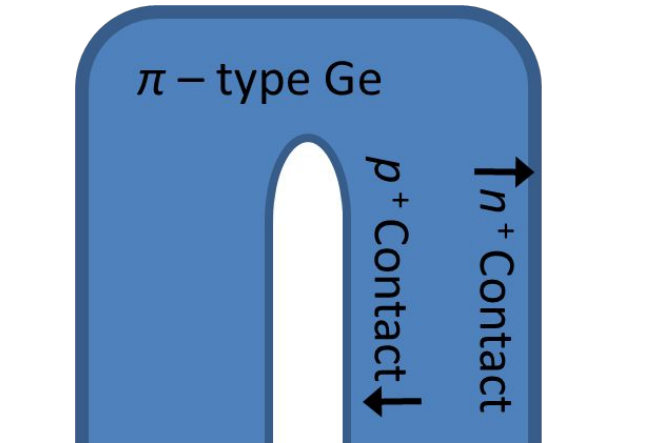
# How to Observe $0\nu\beta\beta$

- How to observe
  - Neutrinos escape
  - Electrons deposit energy in detector
- Majorana Experiment
  - $^{76}\text{Ge}$



# HPGe Detectors

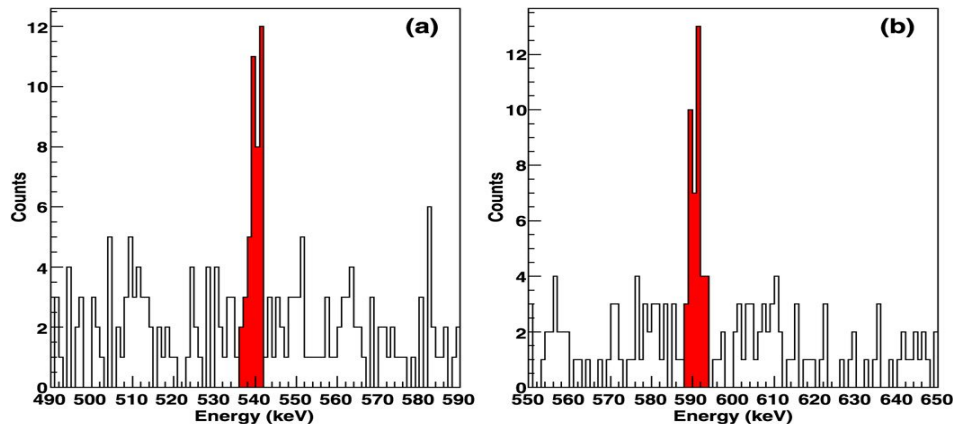
- Photoelectric effect
  - Low energies (<140 keV)
  - Full energy deposition
- Compton scattering
  - Median energies
  - Partial energy deposition
- Pair production
  - High energy
    - Requires 1.022 MeV
  - Dominates > 8 MeV





# Previous Data: $^{100}\text{Mo}$

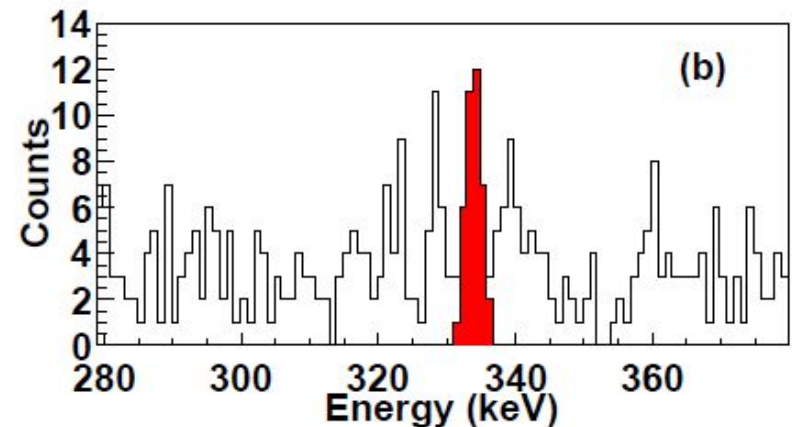
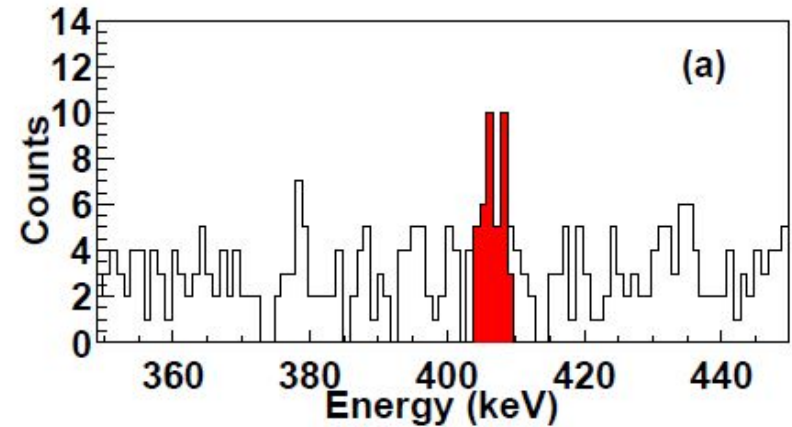
- 1.033 kg  $^{100}\text{Mo}$  (1.05 kg metal enriched to 98.4%)
- 905 days of data acquisition (at TUNL - ground level)
- $35.5 \pm 6.4$  events (539.51 + 590.79 keV)
- $T_{1/2} = [5.5^{+1.2}_{-0.8}$  (stat)  $\pm 0.3$  (syst) ]  $\times 10^{20}$  yr
- NME:  $0.144^{+0.029}_{-0.039}$



<sup>5</sup> M.F.Kidd, J.H. Esterline, and W. Tornow, Nuc. Phys. A 821, 251 (2009)

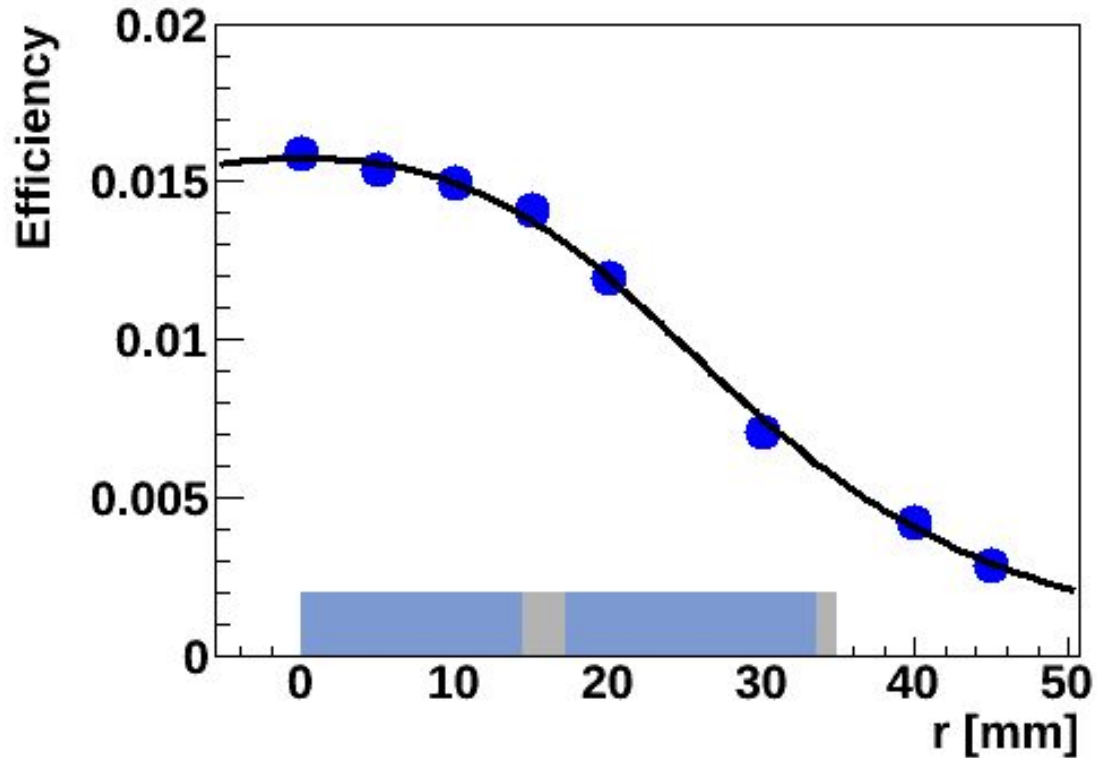
# Previous Data: $^{150}\text{Nd}$

- 40.13 g  $^{150}\text{Nd}$
- 642 days (1.75 y) of data at KURF
- 333.97 + 406.52 keV
- Net 21.6 events
- $T_{1/2} = [1.07^{+0.45}_{-0.25} \text{ (stat)} \pm 0.07 \text{ (syst)}] \times 10^{20} \text{ yr}$
- NME:  $0.0465^{+0.0098}_{-0.0054}$



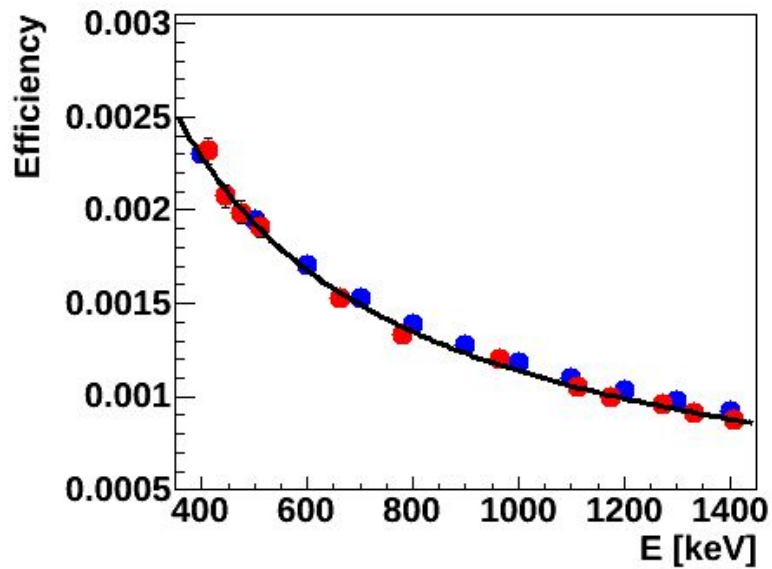
<sup>6</sup> M.F. Kidd, J.H. Esterline, S.W. Finch, and W. Tornow, Phys. Rev. C 90, 055501 (2014)

# Two-Coaxial Apparatus Efficiency

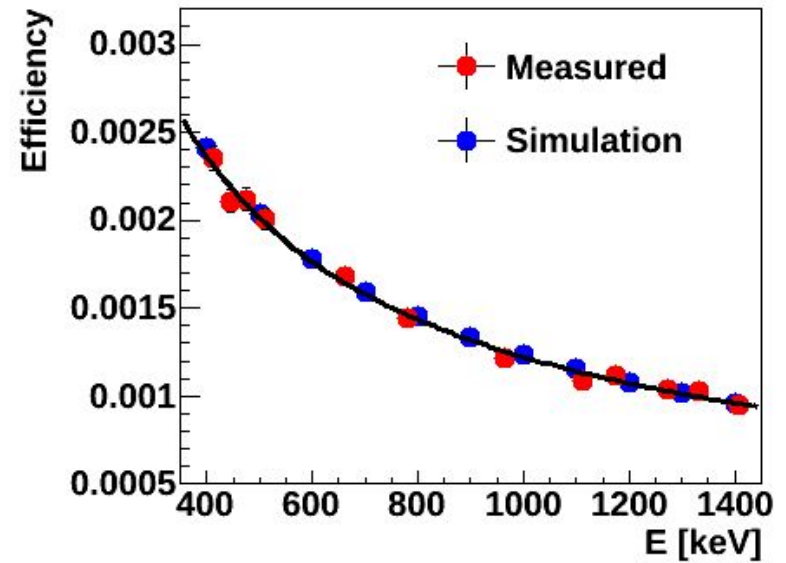


# Coaxial HPGe efficiency

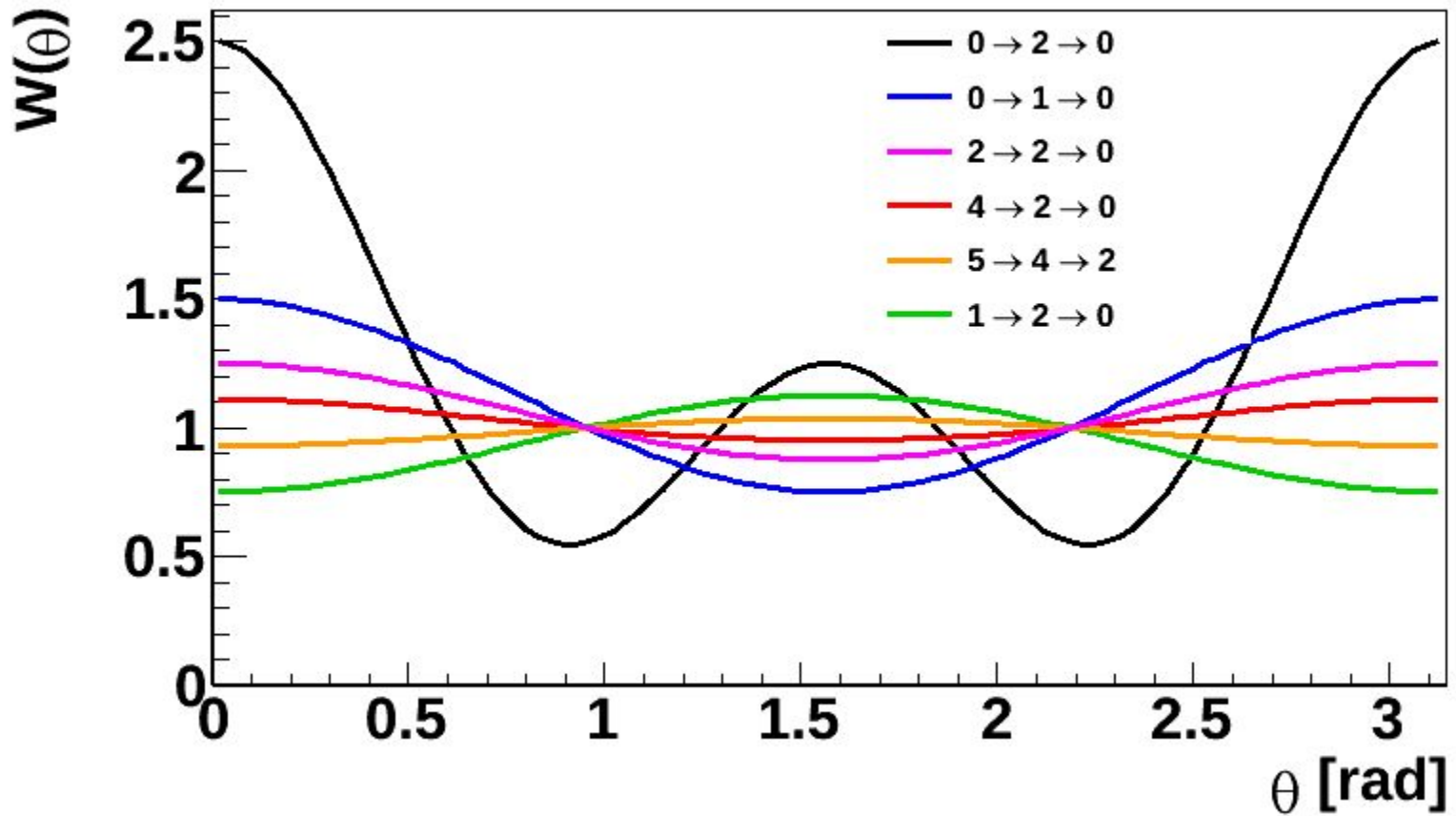
HPGe 1



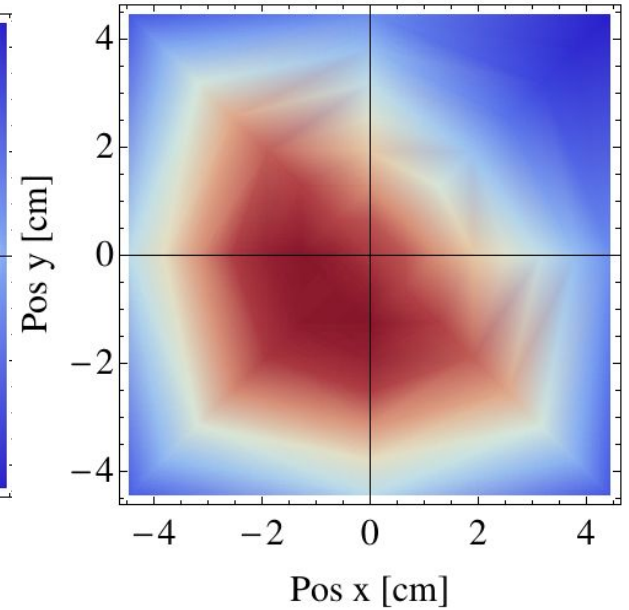
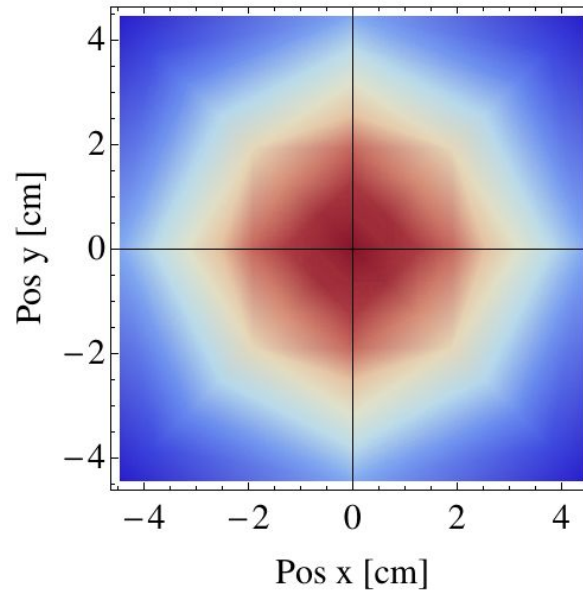
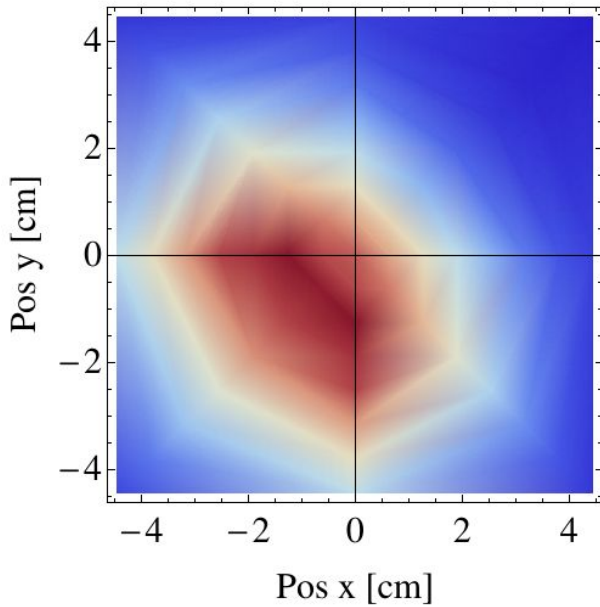
HPGe 2



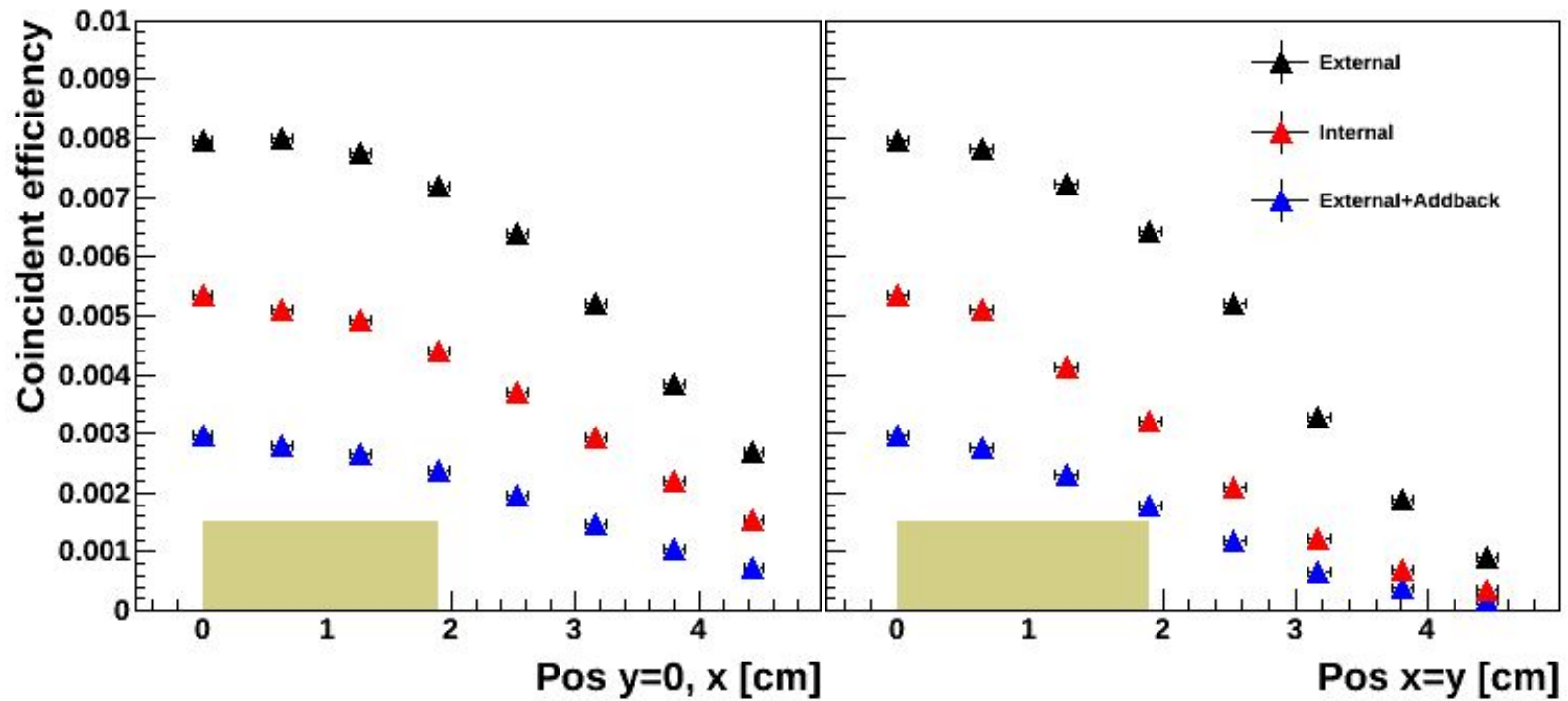
# Angular Distribution



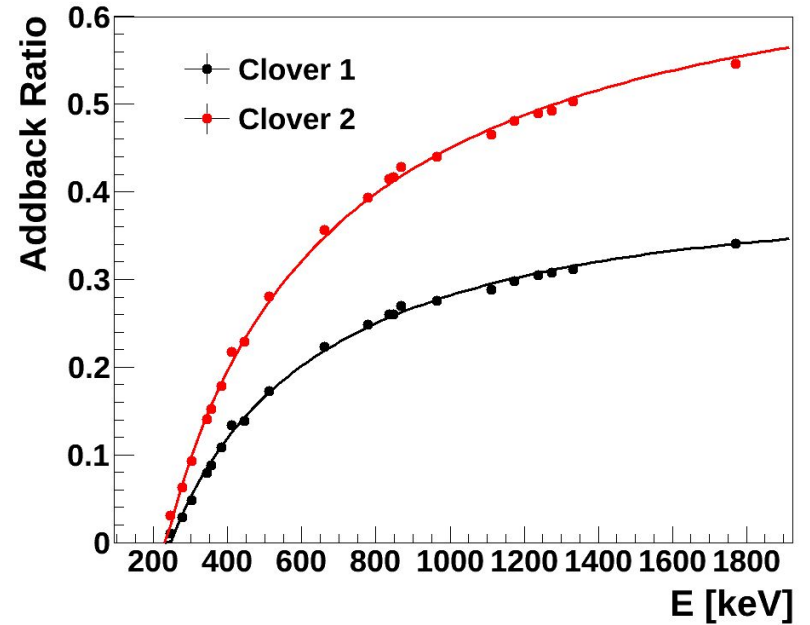
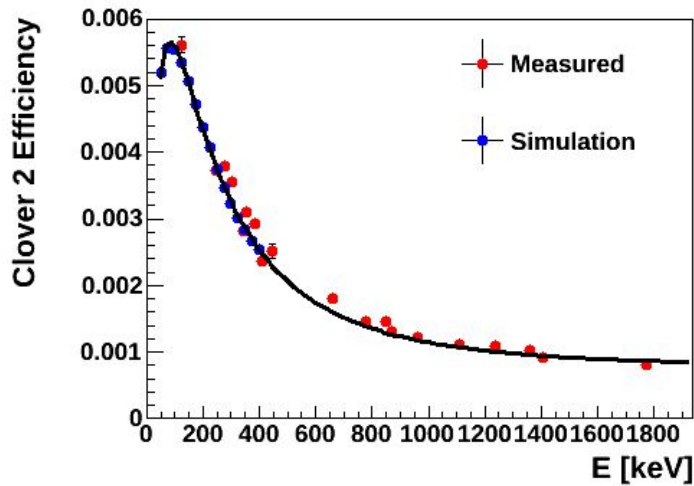
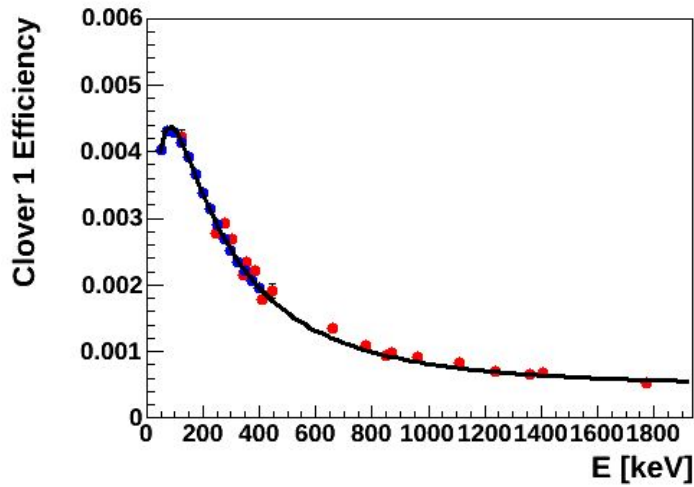
# Two-Clover Apparatus Efficiency



# Two-Clover Apparatus Efficiency



# Clover Efficiency





# Method of Feldman-Cousins

- Background = 3.0,  $\mu = 0.5$

- $P(n|\mu) = \frac{(\mu+b)^n}{n!} \exp[-(\mu + b)]$

- $R = P(n|\mu) / P(n|\mu_{best})$

- Add values of  $n$  in order of  $R$  until  $\sum_n P(n|\mu) > C.L.$

- Here,  $n = [0,6]$  at 90% C.L.

$n$	$P(n \mu)$	$\mu_{best}$	$P(n \mu_{best})$	$R$	rank
0	0.030	0	0.050	0.607	6
1	0.106	0	0.149	0.708	5
2	0.185	0	0.224	0.826	3
3	0.216	0	0.195	0.936	2
4	0.189	1	0.175	0.996	1
5	0.132	2	0.161	0.753	4
6	0.077	3	0.149	0.480	7

# Limits on NME

