PART 3-1 (THE DETERMINANT) OF A MATRIX)

Definition of the Determinant of a 2×2 Matrix

The **determinant** of the matrix

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

is given by

$$|A| = \begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{vmatrix} = a_{11}a_{22} - a_{21}a_{12}$$

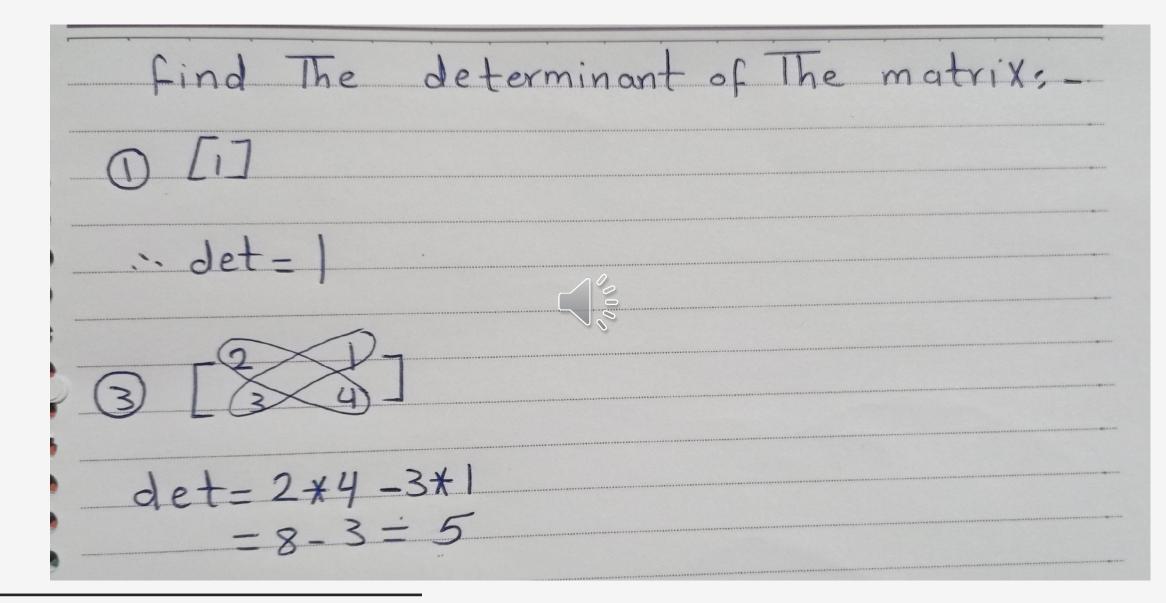
$$\det(A) = |A| = a_{11}a_{22} - a_{21}a_{12}.$$

Note

The determinant of a matrix of order 1 is defined simply as the entry of the matrix. For instance, if A = [-2], then

$$det(A) = -2.$$





DMI NOTE 9

$$det = 5 * 3 - (-6) * 2$$

= $15 + 12 = 27$

$$= \lambda^2 - 4\lambda + 3 = 8$$

$$= \lambda^2 - 4\lambda - 5$$

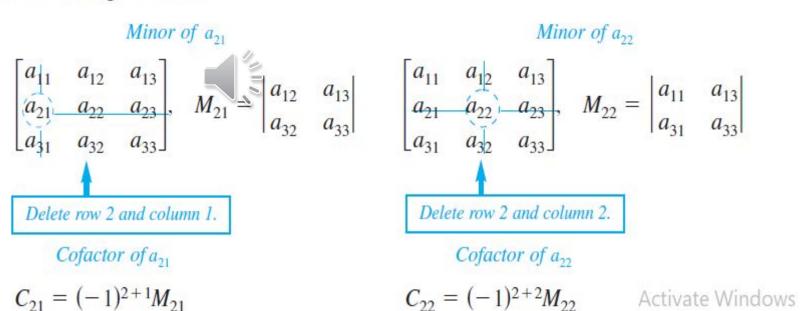
Definitions of Minors and Cofactors of a Matrix

If A is a square matrix, then the **minor** M_{ij} of the element a_{ij} is the determinant of the matrix obtained by deleting the ith row and jth column of A. The **cofactor** C_{ij} is given by

$$C_{ij} = (-1)^{i+j} M_{ij}.$$

 $= -M_{21}$

For example, if A is a 3×3 matrix, then the minors and cofactors of a_{21} and a_{22} are as shown in the diagram below.



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(3) find The minors and Cofactors of

The matrix [] 2]

$$m_{11} = \det L = 3$$
 $m_{12} = \det L = 3 = 3$
 $m_{12} = \det L = 3 = 3$
 $m_{12} = \det L = 3 = 3$
 $m_{12} = \det L = 3 = 3$

$$m21 = det [2] = 2 c (21 = (-1)^{2+1} * 2 = -2$$

$$\begin{bmatrix}
15 \\
4 \\
5 \\
2
-3
\end{bmatrix} = 5 \times 1 - (-3) \times 6$$

$$\begin{bmatrix}
-3 \\
-3
\end{bmatrix} = 5 \times 1 - (-3) \times 6$$

$$= 5 + 18 = 23$$

$$\begin{bmatrix}
-3 \\
-3
\end{bmatrix} = 5 + 18 = 23$$

$$\begin{bmatrix}
-3 \\
-3
\end{bmatrix} = -8 \times (-12 - (-1) + 2 - 8 - 8)$$

$$\begin{bmatrix}
-3 \\
-3
\end{bmatrix} = -8 \times (-12 - (-1) + 2 - 8 - 8)$$

$$\begin{bmatrix}
-3 \\
-3
\end{bmatrix} = -22 \times (-13 - (-1) + 3 - 22 - 22)$$

EDMI NOTE 9