## First practical work Topic: Direct geodetic problem (task)

## Purpose of the work:

Based on the known coordinates, it is necessary to determine the coordinates of the second point according to the known horizontal distance (line) and the known directional angle.

## Introduction

Computational processing of the results of measurements on the ground, carried out in the preparation of plans, the solution of a number of land management problems, the preparation of data for the removal of projects in nature are directly related to direct geodetic problems on coordinates.

## Direct geodetic problem.

The essence of this problem (pic. 1): according to the known coordinates of point $1\left(\mathrm{X}_{1}, \mathrm{Y}_{2}\right)$ of line $1-2$, the directional angle of this line $\alpha_{1-2}$ and its horizontal distance $\mathrm{D}_{1-2} \mathrm{~d} 1-2$, it is required to determine the coordinates of point 2 .


Pic. 1. Direct geodetic problem

Drawing through points 1 and 2 lines parallel to the coordinate axes, we get a right triangle 1-2'-2, in which the hypotenuse $D_{1-2}$ and the acute angle $r=\alpha_{1-2}$ are known.
The legs of this triangle are the increment of the $\Delta x$ and $\Delta y$ coordinates, which can be obtained by the formulas:
$\Delta x=D_{1-2} \cos \alpha_{1-2} ; \Delta y=D_{1-2} \sin \alpha_{1-2}$.
Examination:
$\mathrm{D}=\sqrt{\Delta X^{2}+\Delta Y^{2}}$

- It should be remembered that in the general case, the signs of the increments of coordinates depend on the quarter determined by the directional angle of the given direction (tabl. 1)

| Quarter and their name | The value of directional angles | Connection of rumbs (table corners) with directional angle | Coordinate increment signs |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\Delta \mathrm{X}$ | $\Delta \mathrm{y}$ |
| 1 quarter - NE, | $0^{\circ}-90^{\circ}$ |  | + | + |
| 2 quarter - SE | $90^{\circ}-180^{\circ}$ |  | - | + |
| 3 quarter - SW, | $180^{\circ}-270^{\circ}$ |  | - | - |
| 4 quarter - NW | $270^{\circ}-360^{\circ}$ |  | + | - |

Then the coordinates of the desired point 2 are determined by the formulas:

$$
\mathrm{X}_{2}=\mathrm{X}_{1}+\Delta \mathrm{X}
$$

$$
Y_{2}=Y_{1}+\Delta Y
$$

or

$$
\mathrm{X}_{2}=\mathrm{X}_{1}+\mathrm{D}_{1-2} \cos \alpha_{1-2} ; \quad Y_{2}=Y_{1}+\mathrm{D}_{1-2} \sin \alpha_{1-2}
$$

The increment of coordinates and the coordinates of the required point are calculated with an accuracy corresponding to the accuracy of measuring the horizontal length of the line.

