

Математика

Тема урока: «Одночлены. Многочлены.»

Учитель
математики
ГБОУ СОШ № 619
г.Москвы
Рудьман Т.В.

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

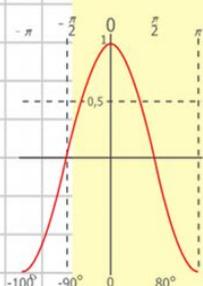
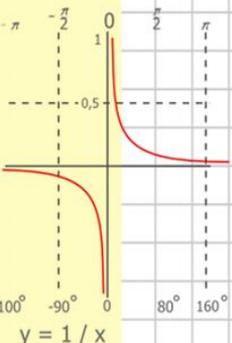
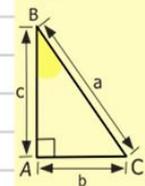
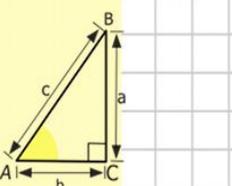
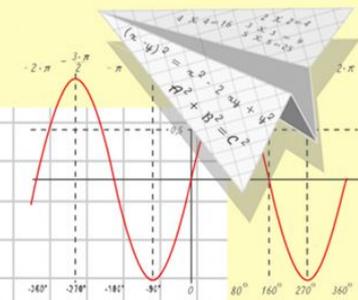
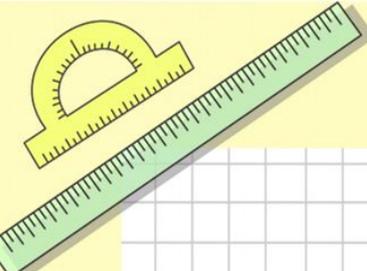
$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

$$\sin 90^\circ = 1$$

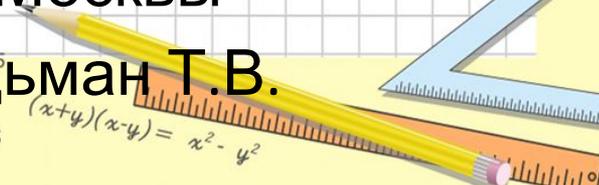
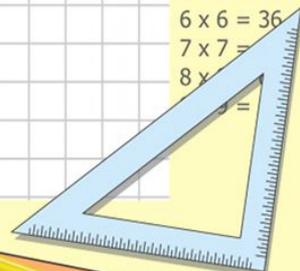
$$\begin{aligned} y &= \sin 90 \\ x &= 25y + 45 \\ y &= 1 \\ x &= 25 + 45 \\ x &= 70 \end{aligned}$$

$$(x+y)(x-y) = x^2 - y^2$$

$$\begin{aligned} 2 \times 2 &= 4 \\ 3 \times 3 &= 9 \\ 4 \times 4 &= 16 \\ 5 \times 5 &= 25 \\ 6 \times 6 &= 36 \\ 7 \times 7 &= 49 \\ 8 \times 8 &= 64 \end{aligned}$$



$$\begin{array}{r} 1 \\ 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$



Определение одночлена

Одночленом называется выражение, которое содержит числа, натуральные степени переменных и их произведения, и при этом не содержит никаких других действий с этими числами и переменными.

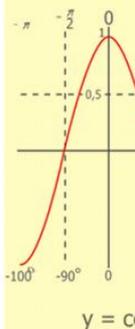
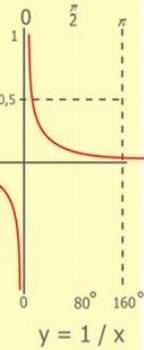
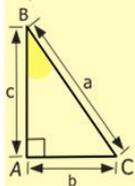
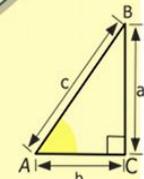
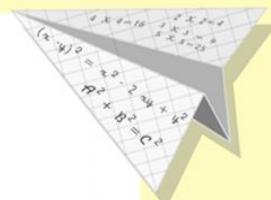
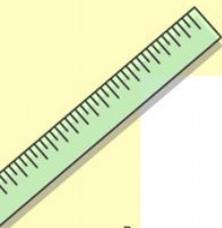
Среди перечисленных выражений на экране назовите одночлены:

$$4bc$$

$$a + b$$

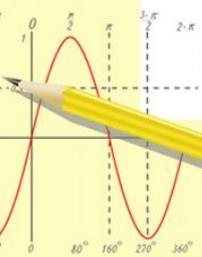
$$3c^2x^5$$

$$\frac{d}{a}$$



$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 2100 \\ + 840 \\ \hline 105000 \end{array}$$

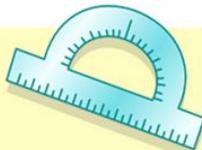
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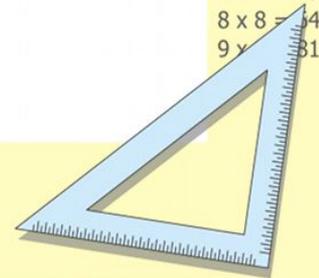
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

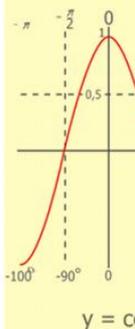
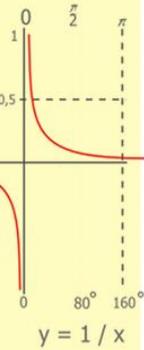
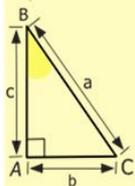
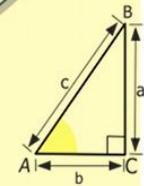
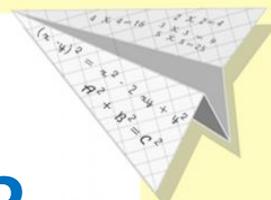
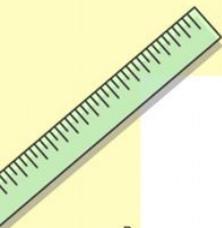
$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



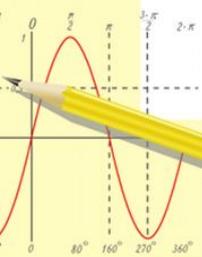
Какое определение неверное?

- ❖ В результате умножения одночлена на одночлен получается одночлен
- ❖ Одночленом называют сумму числовых и буквенных множителей
- ❖ Числовой множитель у одночлена стандартного вида называется коэффициентом одночлена



$$\begin{array}{r} 1 \\ \times 2500 \\ \hline 2500 \\ + 42 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$

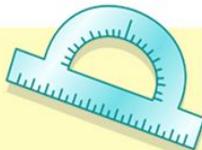
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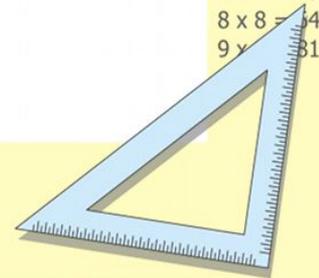
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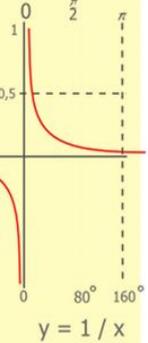
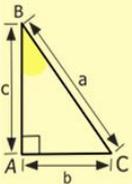
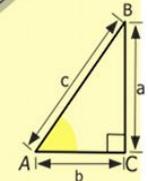
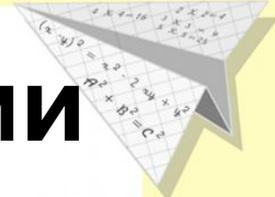
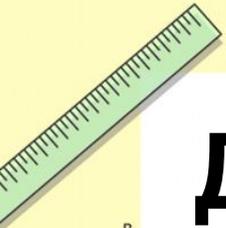
Действия над одночленами

Записать одночлен в стандартном виде.

$$3,2a \times 0,25ab$$

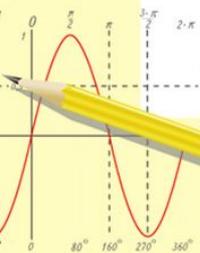
Проверяем

$$0,8a^2b$$



$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 2100 \\ + 8400 \\ \hline 105000 \end{array}$$

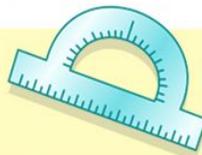
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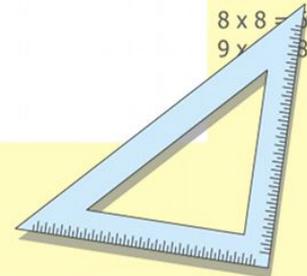
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

$$(x+y)(x-y) = x^2 - y^2$$



Найдите значение одночлена $2x^3x$
при $x = -3$

Проверяем

162

Выполнить умножение одночленов

$$2mn \times (-4m^2n^2)$$

Проверяем

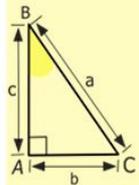
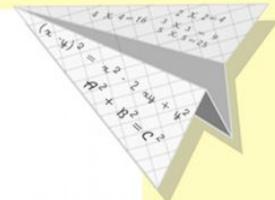
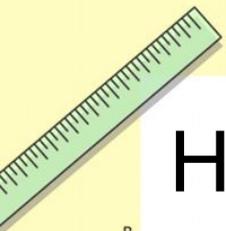
$$-8m^3n^3$$

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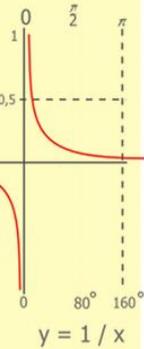
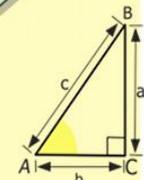
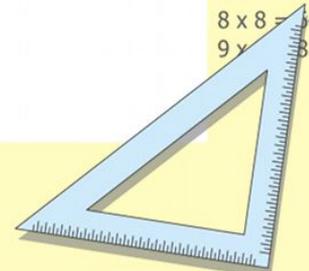
$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$

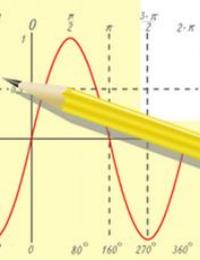


y = co

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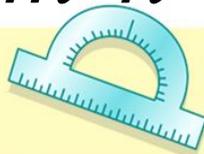
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$$\sin 90^\circ = 1$$



Возведите одночлен в степень $(10x^3y^2a^2)^3$

Проверяем

$$-10000x^9y^6a^6$$

Записать выражение в виде квадрата
одночлена $9a^6$

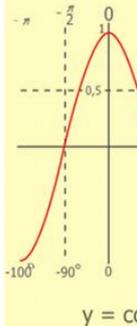
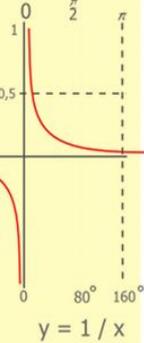
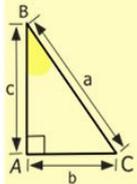
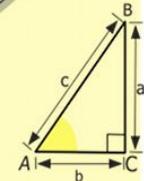
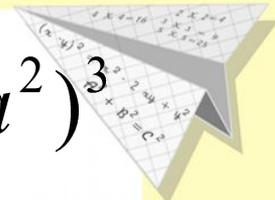
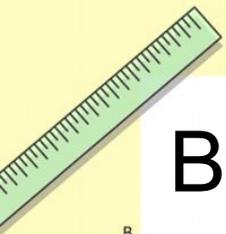
Проверяем

$$(3a^3)^2$$

$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

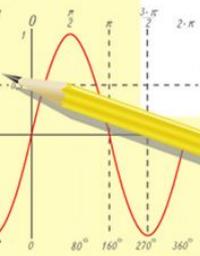
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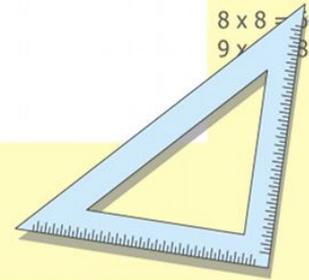
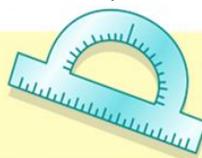
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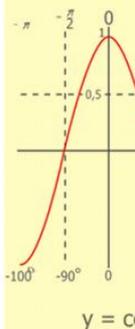
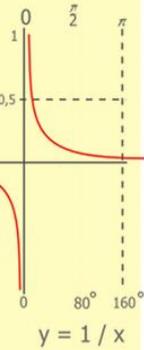
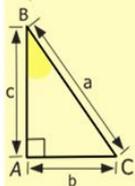
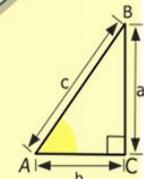
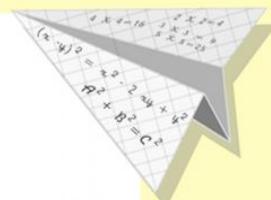
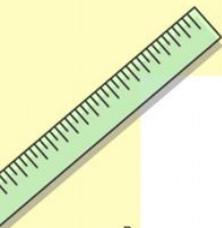


Определение многочлена

Многочленом называется сумма одночленов. Если все одночлены в многочлене приведены к стандартному виду, то говорят, что это многочлен стандартного вида.

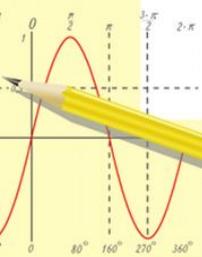
Среди перечисленных выражений на экране назовите многочлены:

$(2a^2)^3$ $4a^2 - 3fc^3$ $4ac^2$ $2a^2 - (2bc + 2c^2)^3$



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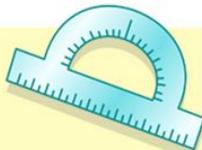
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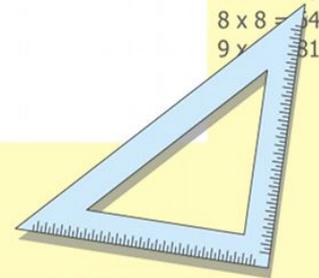
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$$(x+y)(x-y) = x^2 - y^2$$



Соединить линиями соответствующие части определений.

В результате умножения многочлена на многочлен

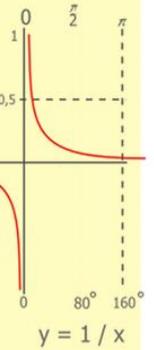
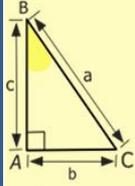
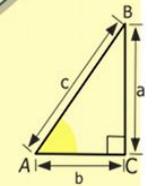
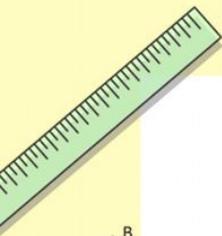
показатели степеней складываются

При умножении степеней с одинаковыми основаниями

отдельно ее числитель и знаменатель

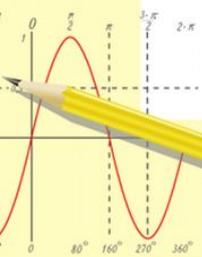
При возведении в степень дроби возводят в эту степень

получается многочлен



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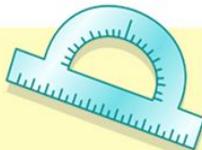
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$$\frac{a}{A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

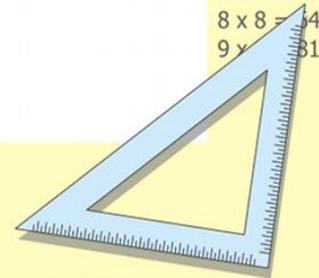
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

$$\begin{cases} y = 1 \\ x = 25 + 45 \\ \hline x = 70 \end{cases}$$

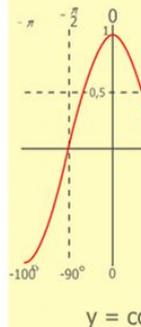
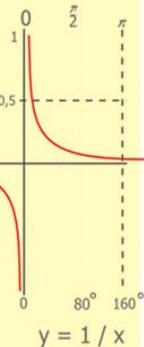
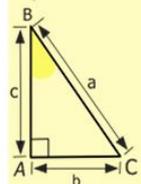
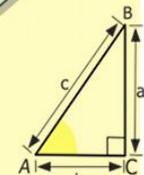
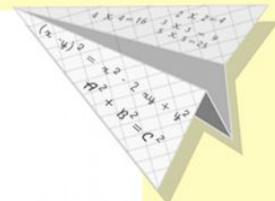
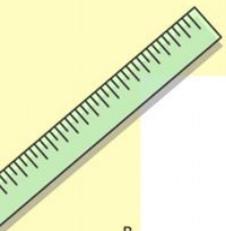
$$(x+y)(x-y) = x^2 - y^2$$



Действия над многочленами

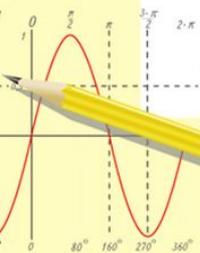
Преобразовать сумму и разность
многочленов в многочлен
стандартного вида – $(21x^2 - 4ax + 7x)$

Проверяем
 $-9x^2 - 4ax + x$



$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 2100 \\ + 840 \\ \hline 105000 \end{array}$$

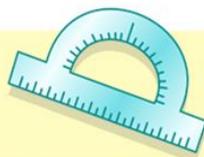
$$\begin{array}{l} 2 \times 2 = 4 \\ 3 \times 3 = 9 \\ 4 \times 4 = 16 \\ 5 \times 5 = 25 \\ 6 \times 6 = 36 \\ 7 \times 7 = 49 \\ 8 \times 8 = 64 \\ 9 \times 9 = 81 \end{array}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

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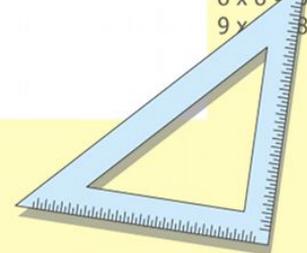
$$\sin 90^\circ = 1$$



$$\begin{cases} y = \sin 90 \\ x = 25y + 45 \end{cases}$$

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$$(x+y)(x-y) = x^2 - y^2$$



Умножить многочлен на одночлен,
 преобразовать $(-4by^2 - 3b^2y^2 - 4by^3 - 5y^3) \times (-4by)$

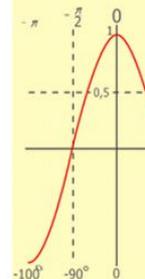
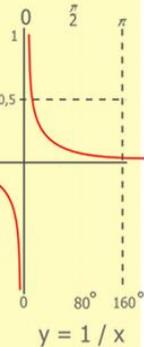
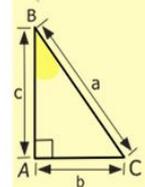
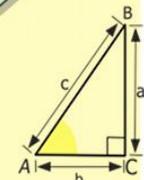
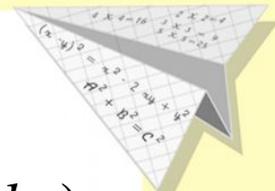
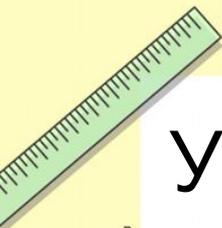
Проверяем

$$12b^3y^3 + 16b^2y^4 + 16b^2y^3 + 20by^4$$

Преобразовать выражение в многочлен
 стандартного вида $-3a^2 \times (-2a^3 + 9a) + (-7a^2 + 2) \times (-2a^3)$

Проверяем

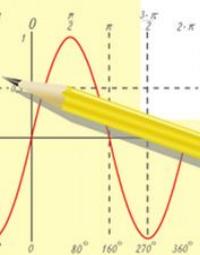
$$20a^5 - 31a^3$$



$$\begin{array}{r} 1 \\ \times 2500 \\ \hline 210 \\ + 84 \\ \hline 105000 \end{array}$$

y = cos

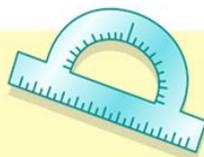
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$$\sin 90^\circ = 1$$

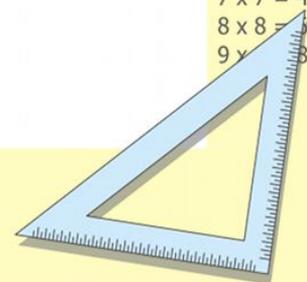


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$$x = 70$$

$$(x+y)(x-y) = x^2 - y^2$$



Вспоминаем формулы сокращенного умножения:

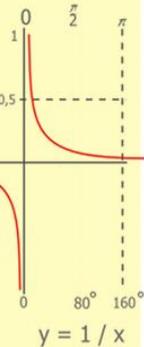
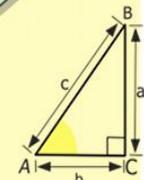
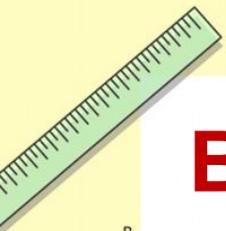
$$a^2 - b^2 = (a - b) \times (a + b)$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

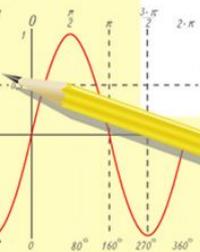
$$(a + b)^2 = a^2 + 2ab + b^2$$

$$a^3 + b^3 = (a + b) \times (a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b) \times (a^2 + ab + b^2)$$



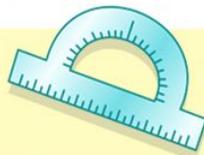
$$\begin{array}{r} 2500 \\ \times 42 \\ \hline 210 \\ + 84 \\ \hline 10500 \end{array}$$



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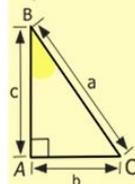
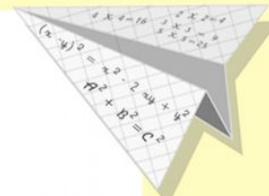
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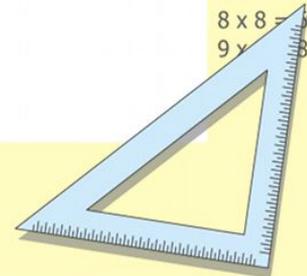
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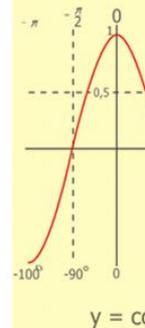
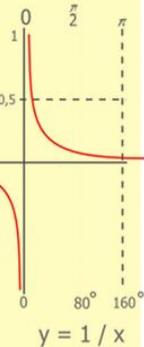
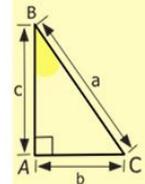
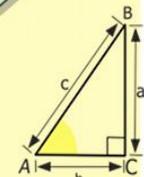
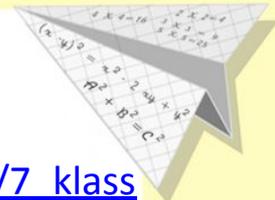
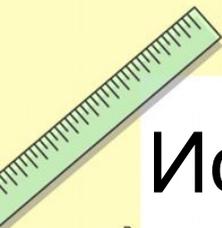


Используемые ресурсы:

http://ucheba-legko.ru/lections/viewlection/matematika/7_klass/mnogochlenyi/odnochlenyi

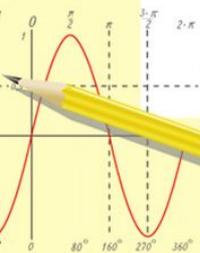
http://ucheba-legko.ru/lections/viewlection/matematika/7_klass/mnogochlenyi/lec_odnochl_enyi_i_mnogochlenyi-2

http://fizmat.by/math/polynomials/operations_monomials/test25



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