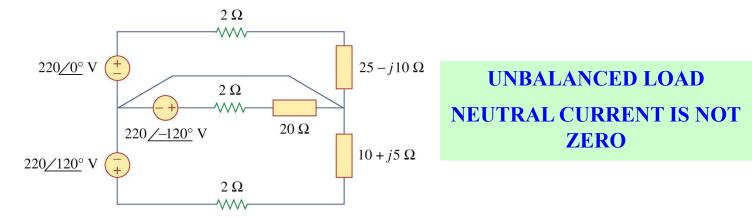
## **Problem 12.10** Determine the current in the neutral line.



## Chapter 12, Solution 10.

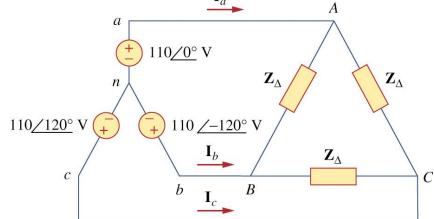
Since the neutral line is present, we can solve this problem on a per-phase basis.

For phase a,  $\mathbf{I}_{a} = \frac{\mathbf{V}_{an}}{\mathbf{Z}_{A} + 2} = \frac{220 \angle 0^{\circ}}{27 - j10} = \frac{220}{28.79 \angle -20.32^{\circ}} = 7.642 \angle 20.32^{\circ}$ For phase b,  $\mathbf{I}_{b} = \frac{\mathbf{V}_{bn}}{\mathbf{Z}_{B} + 2} = \frac{220 \angle -120^{\circ}}{22} = 10 \angle -120^{\circ}$ For phase c,  $\mathbf{I}_{c} = \frac{\mathbf{V}_{cn}}{\mathbf{Z}_{C} + 2} = \frac{220 \angle 120^{\circ}}{12 + j5} = \frac{220 \angle 120^{\circ}}{13 \angle 22.62^{\circ}} = 16.923 \angle 97.38^{\circ}$ 

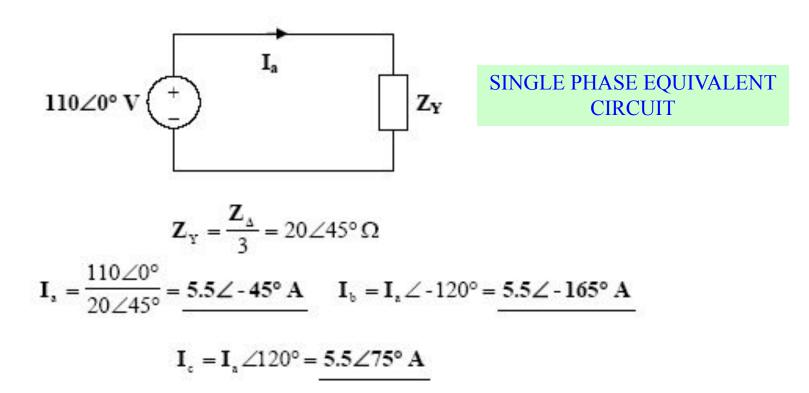
The current in the neutral line is  $I_n = -(I_a + I_b + I_c)$  or  $-I_n = I_a + I_b + I_c$ 

$$\mathbf{I}_{n} = (7.166 + j2.654) + (-5 - j8.667) + (-2.173 + j16.783)$$
$$\mathbf{I}_{n} = 0.007 - j10.77 = \underline{10.77 \angle 90^{\circ} \mathbf{A}}$$

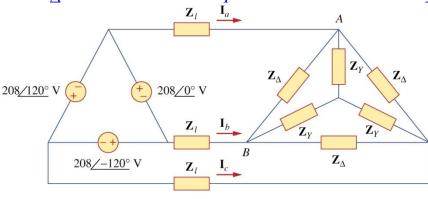
**Problem 12.12** Solve for the line currents in the Y- $\Delta$  circuit. Take  $Z_{\Delta} = 60 \angle 45^{\circ} \Omega$ .



Convert the delta-load to a Y-load and apply per-phase analysis.



**Problem 12.22** Find the line currents  $I_a$ ,  $I_b$ , and  $I_c$  in the three-phase network below. Take  $Z_A = 12 - j15\Omega$ ,  $Z_y = 4 + j6\Omega$ , and  $Z_y = 2\Omega$ .



ONE DELTA AND ONE Y CONNECTED LOAD IS CONNECTED

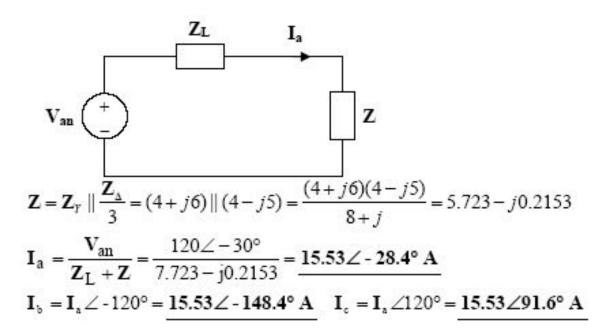
□ TWO Loads are parallel if they are converted to same type.

Delta connected load is converted to Y

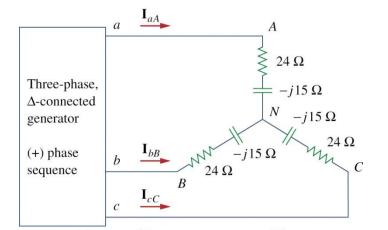
Convert the  $\Delta$ -connected source to a Y-connected connection.

$$\mathbf{V}_{aa} = \frac{\nabla_{p}}{\sqrt{3}} \angle -30^{\circ} = \frac{208}{\sqrt{3}} \angle -30^{\circ} = 120 \angle -30^{\circ}$$

Convert the  $\Delta$ -connected load to a Y-connected load.



**Problem 12.26** For the balanced circuit below,  $V_{ab} = 125 \angle 0^{\circ}$  V. Find the line currents  $I_{aA}$ ,  $I_{bB}$ , and  $I_{cC}$ .



## BALANCED Y CONNECTED LOAD.

Transform the source to its wye equivalent.

 $V_{an} = \frac{V_p}{\sqrt{3}} \angle -30^\circ = 72.17 \angle -30^\circ$  Source voltage given is line to line, obtain the line to neutral voltage.

Now, use the per-phase equivalent circuit.

$$I_{aA} = \frac{V_{au}}{Z}, \quad Z = 24 - j15 = 28.3 \angle -32^{\circ}$$
$$I_{aA} = \frac{72.17 \angle -30^{\circ}}{28.3 \angle -32^{\circ}} = 2.55 \angle 2^{\circ} A$$
$$I_{bB} = I_{aA} \angle -120^{\circ} = 2.55 \angle -118^{\circ} A$$
$$I_{cC} = I_{aA} \angle 120^{\circ} = 2.55 \angle 122^{\circ} A$$

**Problem 12.47** The following three parallel-connected three-phase loads are fed by a balanced three-phase source.

Load 1: 250 kVA, 0.8 pf lagging Load 2: 300 kVA, 0.95 pf leading Load 3: 450 kVA, unity pf If the line voltage is 13.8 kV, calculate the line current and the power factor of the source. Assume that the line impedance is zero.

pf = 0.8 (lagging) 
$$\longrightarrow \theta = \cos^{-1}(0.8) = 36.87^{\circ}$$
  
 $S_1 = 250 \angle 36.87^{\circ} = 200 + j150 \text{ kVA}$   
pf = 0.95 (leading)  $\longrightarrow \theta = \cos^{-1}(0.95) = -18.19^{\circ}$   
 $S_2 = 300 \angle -18.19^{\circ} = 285 - j93.65 \text{ kVA}$   
pf = 1.0  $\longrightarrow \theta = \cos^{-1}(1) = 0^{\circ}$   
 $S_3 = 450 \text{ kVA}$   $S_T = S_1 + S_2 + S_3 = 935 + j56.35 = 936.7 \angle 3.45^{\circ} \text{ kVA}$   
 $|S_T| = \sqrt{3} V_L I_L$   $I_L = \frac{936.7 \times 10^3}{\sqrt{3}(13.8 \times 10^3)} = 39.19 \text{ A rms}$ 

 $pf = cos\theta = cos(3.45^\circ) = 0.9982$  (lagging)

**Problem 12.81** A professional center is supplied by a balanced three-phase source. The center has four plants, each a balanced three-phase load as follows:

Load 1: 150 kVA at 0.8 pf leading Load 2: 100 kW at unity pf

Load 3: 200 kVA at 0.6 pf lagging Load 4: 80 kW and 95 kVAR (inductive)

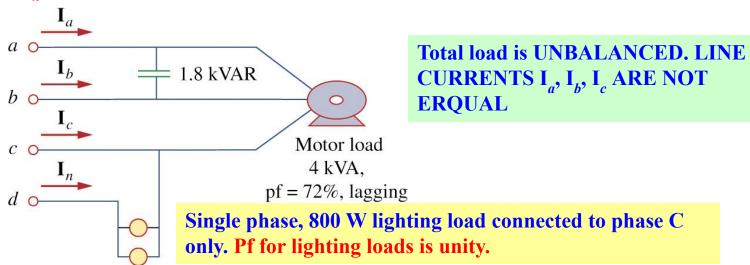
If the line impedance is  $0.02 + j0.05 \Omega$  per phase and the line voltage at the loads is 480 V, find the magnitude of the line voltage at the source.

For the line,

 $S_L = 3I_L^2 Z_L = (3)(542.7)^2(0.02 + j0.05)$   $S_L = 17.67 + j44.18 \text{ kVA}$ At the source,

$$S_T = S + S_L = 437.7 + j209.2$$
  $S_T = 485.1 \angle 25.55^\circ \text{ kVA}$   
 $V_T = \frac{S_T}{\sqrt{3} I_L} = \frac{485.1 \times 10^3}{\sqrt{3} \times 542.7} = \frac{516 \text{ V}}{1000}$ 

**Problem 12.84** The Figure displays a three-phase delta-connected motor load which is connected to a line voltage of 440 V and draws 4 kVA at a power factor of 72 percent lagging. In addition, a single 1.8 kVAR capacitor is connected between lines *a* and *b*, while a 800-W lighting load is connected between line *c* and neutral. Assuming the *abc* sequence and taking  $V_{an} = V_p \angle 0^\circ$ , find the magnitude and phase angle of currents  $I_a$ ,  $I_b$ ,  $I_c$ , and  $I_n$ .



We first find the magnitude of the various currents.

For the motor  $I_L = I_L I_1 = \frac{SS}{\sqrt{33}V_{LL}} = \frac{4000}{440\sqrt{3}} = 5.248 \text{ A}$ For the capacitor,  $I_c = \frac{Q_c}{V_L} = \frac{1800}{440} = 4.091 \text{ A}$ For the lighting,  $V_p = \frac{440}{\sqrt{3}} = 254 \text{ V}$   $I_{Li} = \frac{P_{Li}}{V_p} = \frac{800}{254} = 3.15 \text{ A}$ 

