

Class 5

Optimization models

Demand function equation.

Revenue maximization.

Profit maximization.

BEPs.

Study materials:

Slides

Demand function

What shall we do with our selling Price, if:

$P_1 = \$1,000$, then $Q_1 = 400$ units, and $R_1 = \$400,000$

$P_2 = \$1,750$, then $Q_2 = 250$ units, and $R_2 = \$437,500$

To do:

- (a) increase the price, or
- (b) decrease the price, or
- (c) keep the price at \$1,750?

SOLUTION: The price that MAX the revenue shall be:

\$2,250,

\$2,000,

\$1,750,

\$1,500,

\$1,250?

Demand function

Correct answer:

The “best” price to MAX the revenue would be: \$1,500

$P_{\text{opt}} = \$1,500$, then $Q_{\text{opt}} = 300$ units, and $R_{\text{MAX}} = \$450,000$

To do:

(a) increase the price

(b) decrease the price

(c) keep the price at \$1,750

This can be solved through (1) finding the demand function equation, and (2) solving a revenue maximization problem.

Demand function

Can be found using the approaches:

Sales tests:

P1, Q1

P2, Q2

Quantity (u)	Price (\$)
250	1 750
350	1 250

NB: Demand function is not always linear.
P(MAX) and Q(MAX) are indicative.
Sales test not always linear.
Need to offset the effect of seasonality.

Demand Function Equation

$Y = a + b \cdot X$, basic linear equation

$P = a + b \cdot Q$, demand function equation

where:

$a = P(\text{MAX in the market}) = 3,000$

$b = \text{slope of the demand function line}$
 $= \Delta Y / \Delta X = -5$

$Q(\text{MAX}) = -a/b = 600 \text{ (units)}$

NB: Mind the negative value of the variable coefficient of the linear equation “b”.

Task: Revenue maximization

$$Q^*(\text{Revenue MAX}) = -a/2b = 300 \text{ (u)}$$

Substitute Q^* into the Demand function equation,
will find P^* (= the price at Q^* point)

$$P^* = 3,000 + (-5) \cdot 300 = \$1,500$$

$$R^* = P^* \times Q^* = 450,000$$

NB: R^* is highest revenue possible at the current demand.

Profit maximization

$$Q^{**} \text{ (Profit MAX)} = - (a - VC(u)) / 2b$$

P^{**} shall correspond to the value of Q^{**}

Data needed:

fixed and variable costs

$$FC = \$100,000$$

$$VC(u) = \$500$$

$$Q^{**} = 250(u), \text{ then}$$

$$P^{**} = 1,750, \text{ then}$$

$$R^{**} = 437,500, \text{ and}$$

$$Pr^{**} = R^{**} - FC - VC(u)Q^{**} = \$212,500$$

*Pr^{**} is highest operating profit possible at the current demand and total costs*

Summary

	Quantity (u)	Price (\$)	Revenue (\$)	Op Profit (\$)
Demand function	250	1,750	437,500	212,500
	350	1,250	437,500	162,500
Fixed Costs	100,000			
VC(u)	500			
b	-5			
a	3,000			
	Quantity (u)	Price (\$)	Revenue (\$)	Op Profit (\$)
Qmax	600	0	0	-400,000
Q*(Revenue)	300	1,500	450,000	200,000
Q**(Profit)	250	1,750	437,500	212,500
Discriminant	4,250,000	SqRoot	2,062	
	Quantity (u)	Price (\$)	Revenue (\$)	Op Profit (\$)
Q1	43.84	2,781	121,922	0
Q2	456.16	719	328,078	0
Nota bene:				
input cells				
results (u, \$)				