

Кварки, невылетание цвета, и суперкомпьютеры

М.И. Поликарпов (ИТЭФ, Москва)

- Введение: кварки и глюоны
- Невылетание цвета – задача тысячелетия
- Моделирование сильных взаимодействий на компьютерах и суперкомпьютерах
- Перемешивание сильных и электромагнитных взаимодействий
- Теория невылетания цвета

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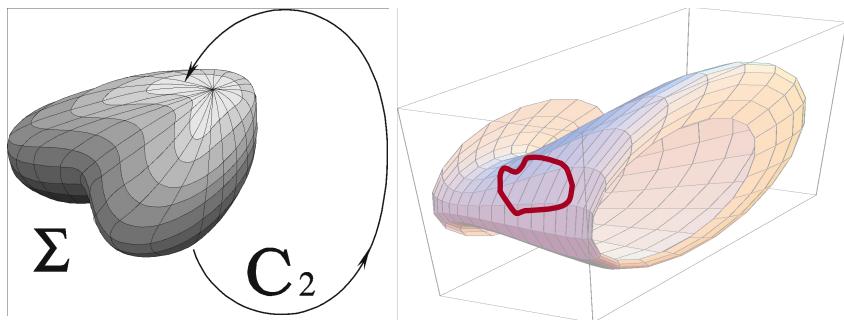
Experiment

LHC RHIC



Theory

$$L = -\frac{1}{g^2} \text{Tr } F_{\mu\nu}^2 + \sum_f \bar{\psi}_f (D + m) \psi_f$$



Supercalculations



Основные результаты получены в
сотрудничестве группы ИТЭФ с
ДЭЗИ (Германия),
Университет Каназава (Япония),
Национальная Лаборатория Брукхэвен (США)
Университет Сан Франциско (США)



F.V. Gubarev, A.V.Kovalenko, S.M. Morozov, MIP, S.V. Syritsyn, V.I. Zakharov, P.Yu Boyko,
P.V. Buividovich, M.N. Chernodub, V.G. Bornyakov , E.N. Luschevskaya, A.I.Veselov, A.A.
Slavnov

DESY, Gumboldt University, Germany

G.Schierholz, D.Pleiter, T.Streuer, H.Stuben, F. Weinberg, M. Mueller-Proysker, E.M. Ilgenfritz

Kanazawa University, Japan

H.Ichie, S.Kitahara, Y.Koma,Y.Mori, Y.Nakamura, T.Suzuki, A. Nakamura

BNL, San Francisco University, USA

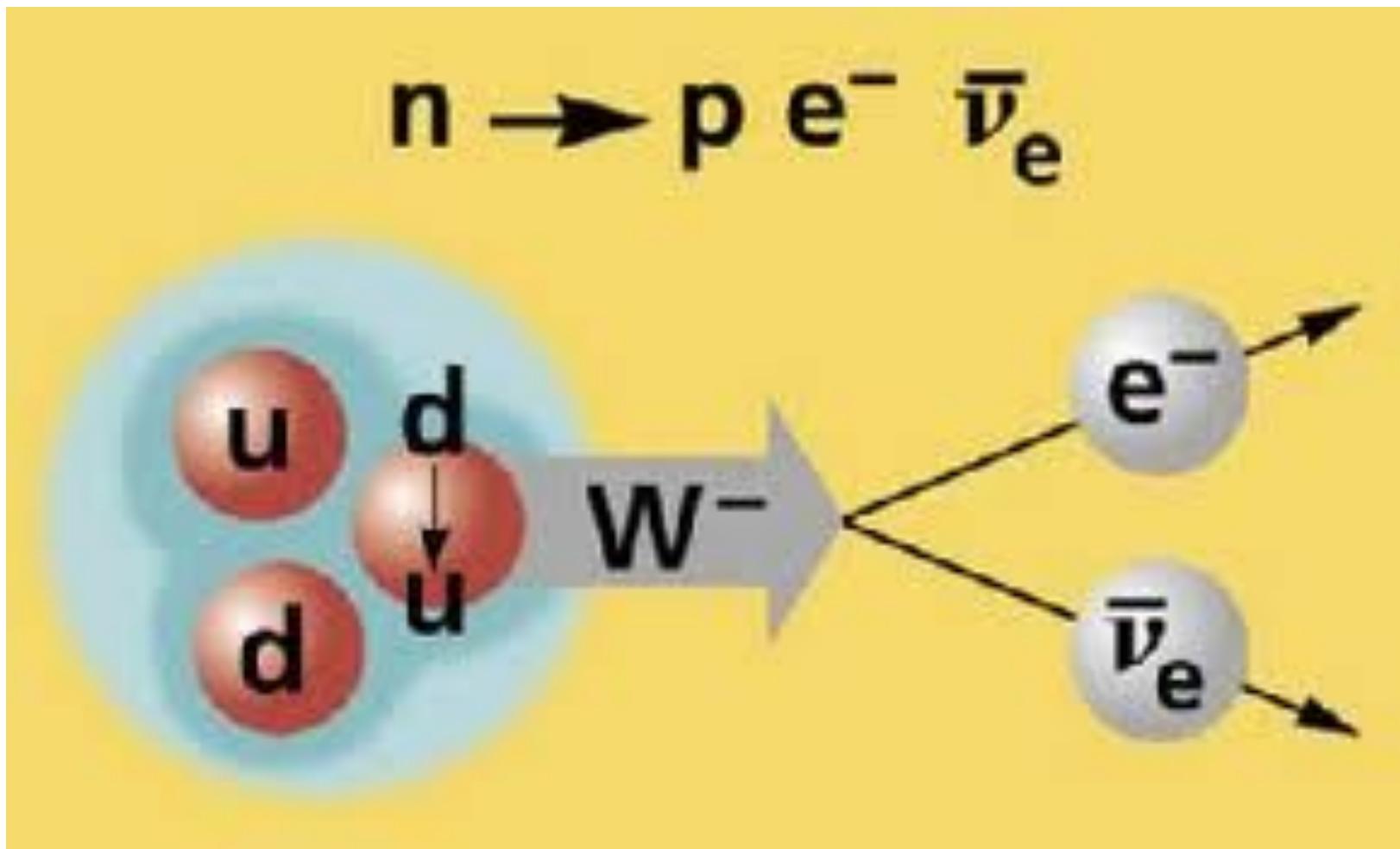
D. Kharzeev, J. Greensite, S. Olejnik (+ Bratislava University, Slovakia)

Взаимодействия – 1. Гравитационное

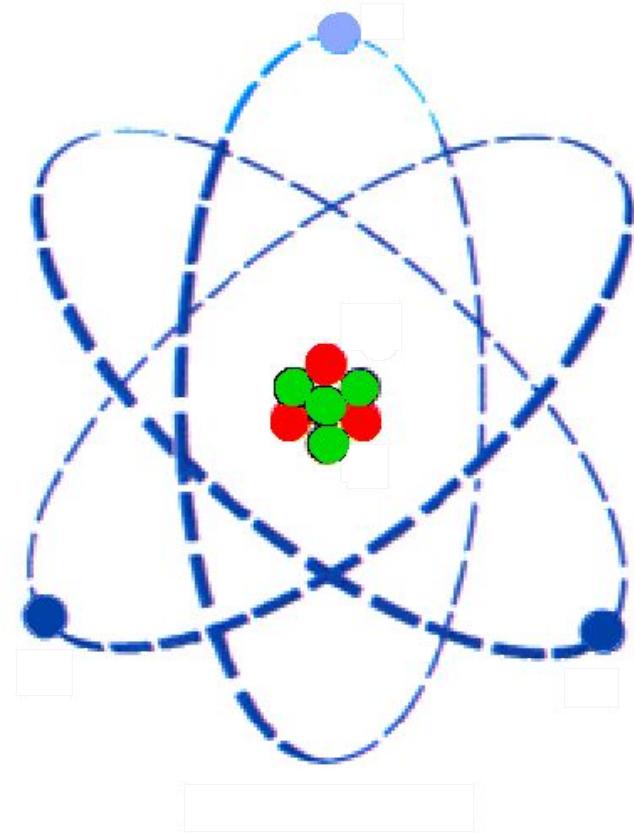
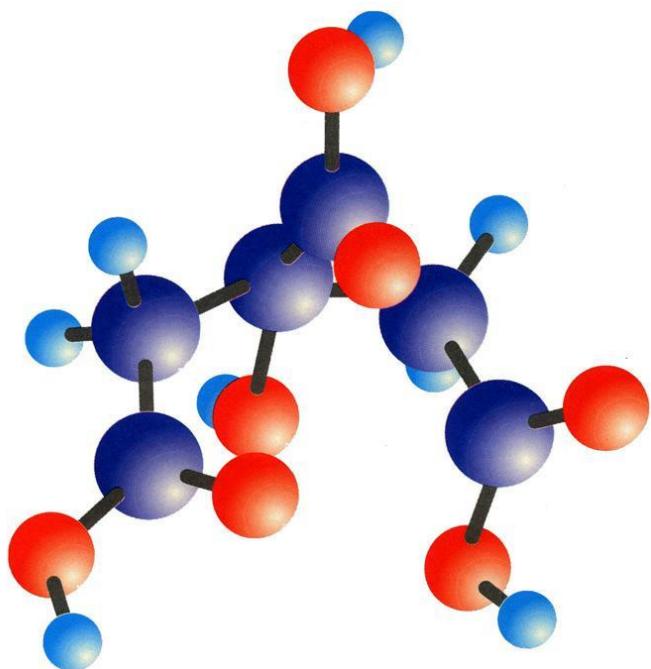


mg

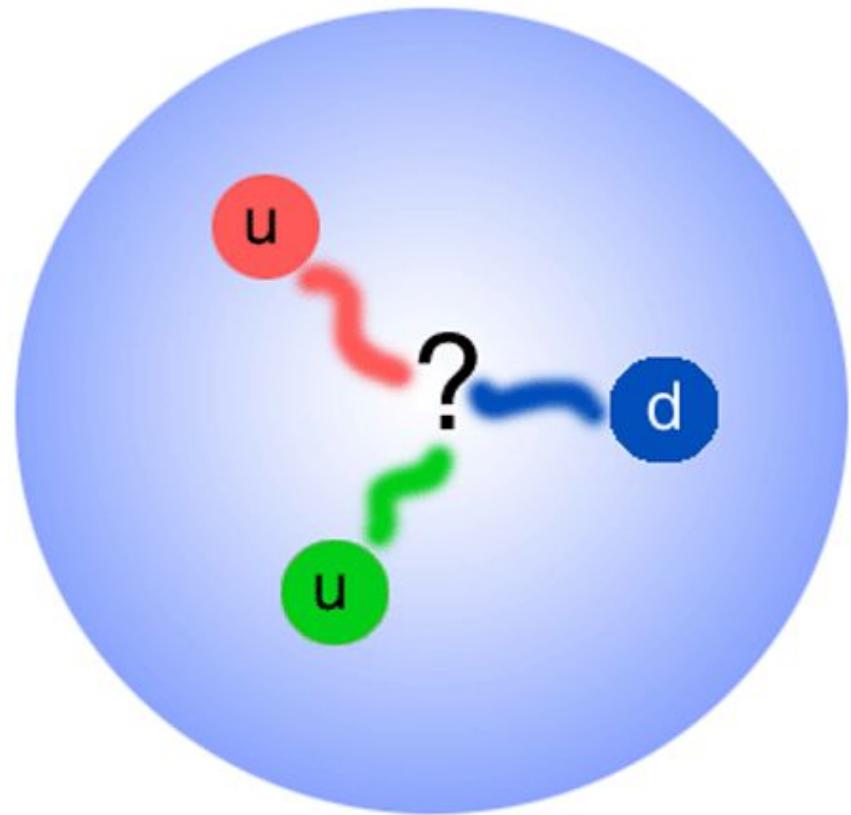
Взаимодействия – 2. Слабое



Взаимодействия – 3. Электромагнитное



Взаимодействия – 4. Сильное

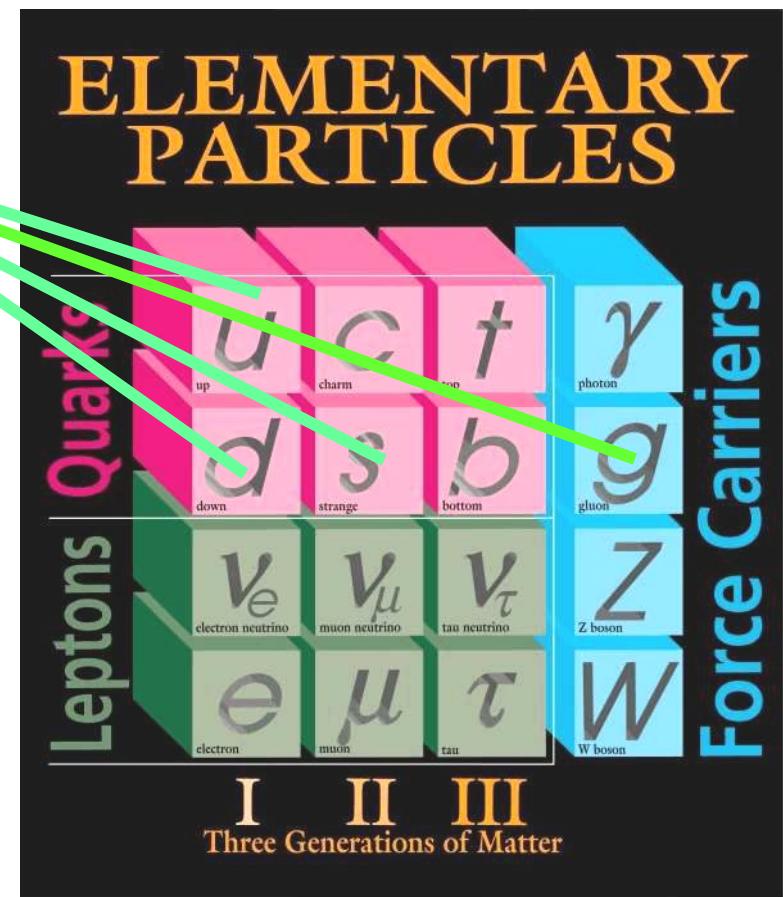
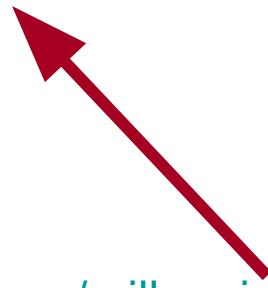


Основные задачи теории сильных взаимодействий

Стартуя с Лагранжиана КХД

$$L = -\frac{1}{g^2} \text{Tr } F_{\mu\nu}^2 + \sum_f \bar{\psi}_f (D + m) \psi_f$$

- 1) Получить спектр адронов,
- 2) Посчитать матричные элементы,
- (3) Описать фазовую диаграмму теории
- (4) Объяснить невылетание цвета

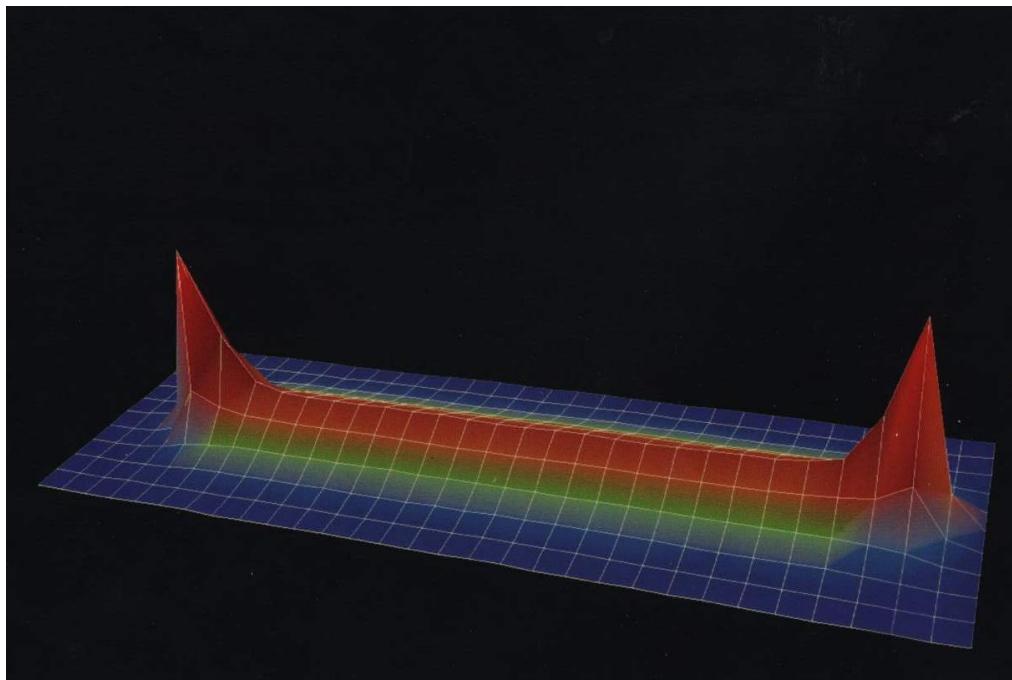


http://www.claymath.org/millennium/Yang-Mills_Theory/ (1 000 000 \$US)

Невылетание цвета

(почему мы не видим свободных夸克ов и глюонов?)

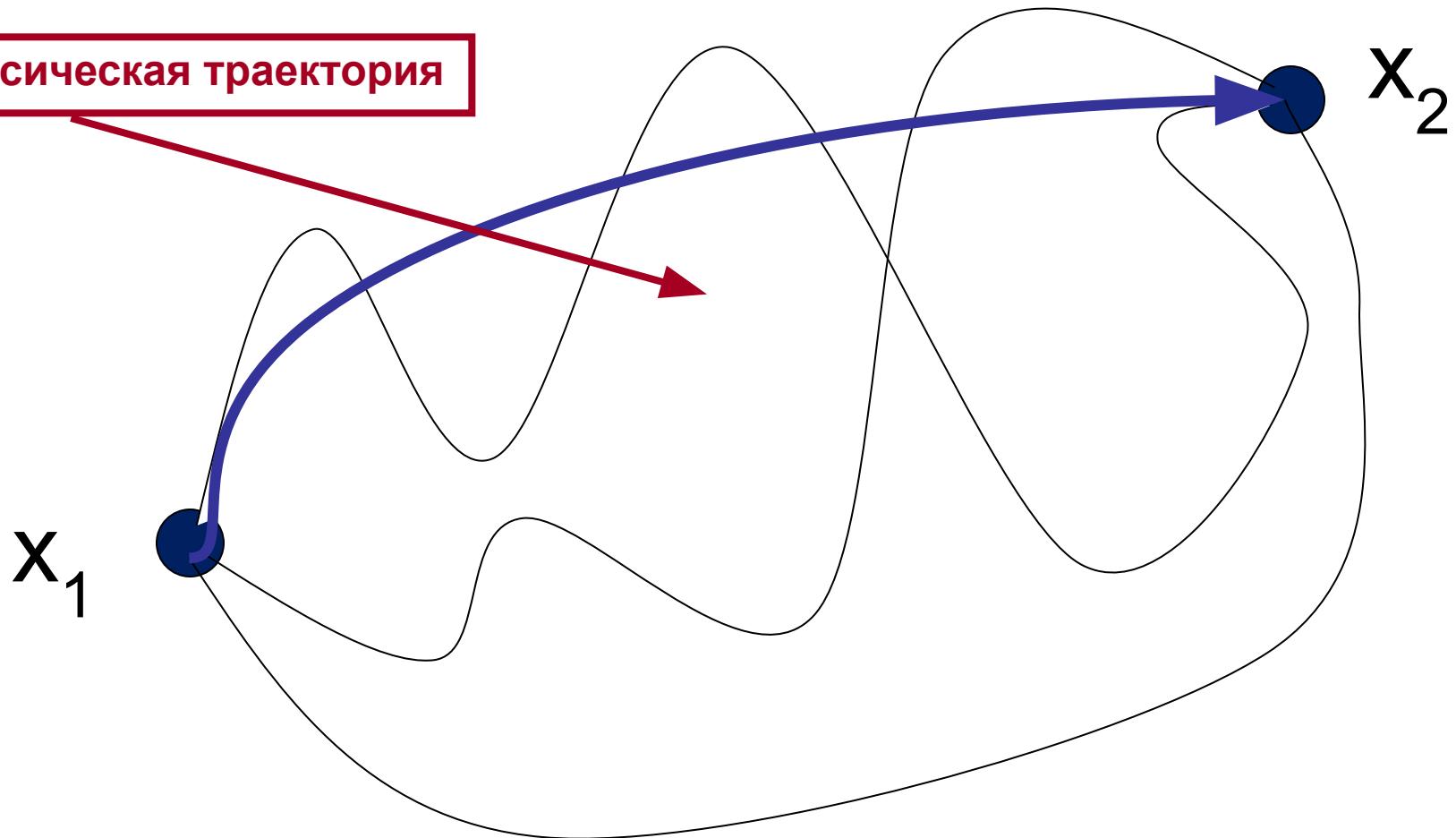
Основная сложность – отсутствие аналитических методов для описания теории сильных взаимодействий, но (супер)компьютеры могут многое предсказывать исходя из Лагранжиана КХД



**Сила между
кварком и
антикварком
12 тонн!!!**

Квантовая механика частицы

Классическая траектория



Вес каждой траектории

$$e^{iS}$$

Квантовая теория поля

$$A_\mu(x) = A_\mu(x, y, z, t)$$

$$-\infty < A_\mu(x) < +\infty$$

$$Z = \int \int \int \dots \int \int \int D A_\mu(x) e^{iS[A_\mu]}$$

Methods

- Imaginary time $t \rightarrow it$

$$Z = \int D\varphi \exp \{i S[\varphi]\} \rightarrow Z = \int D\varphi \exp \{-S[\varphi]\}$$

- Space-time discretization

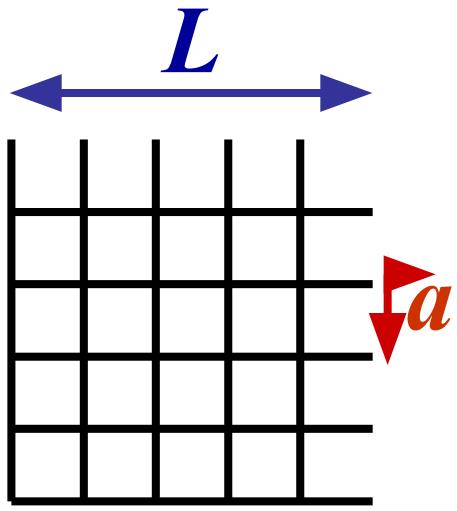
$$D\varphi(x) \Rightarrow \prod_x d\varphi_x$$

$$Z = \int \prod_x d\varphi_x \exp \{-S[\varphi]\}$$

- Thus we get from functional integral the partition function for statistical theory in four dimensions

INTRODUCTION

Three limits



Lattice spacing

Lattice size

Quark mass

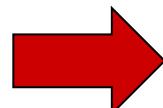
$$\begin{aligned} a &\rightarrow 0 \\ L &\rightarrow \infty \\ m_q &\rightarrow 0 \end{aligned}$$

Typical values

$$a \approx 0.1 \text{ fm}$$

$$L \approx 2 \div 4 \text{ fm}$$

$$m_q \approx 100 \text{ MeV}$$



Extrapolation

+

Chiral perturbation
theory

Типичная кратность интегралов

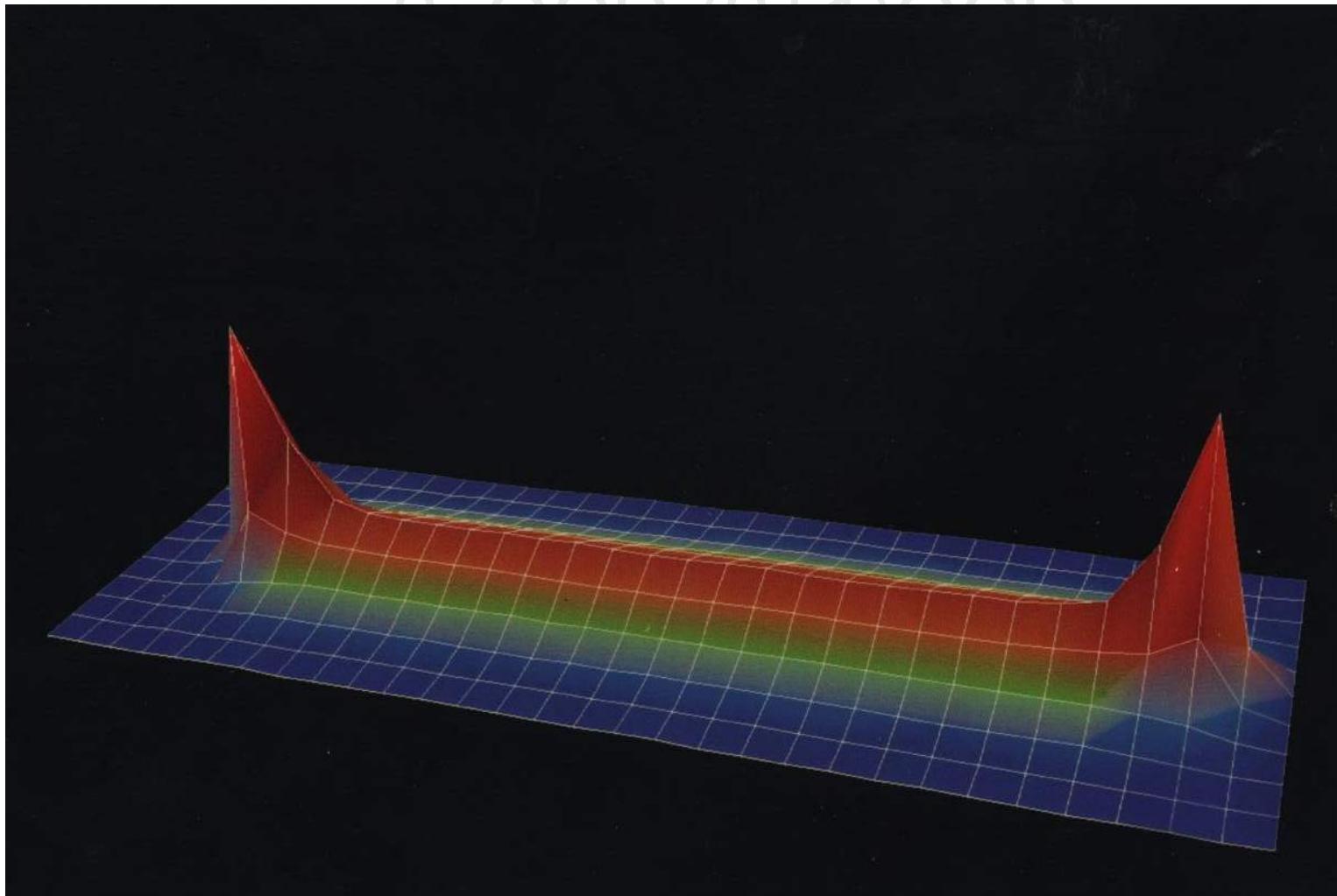
Для решетки L^4
 $(L=48, L^4=5,308,416)$

- Мы считаем интегралы кратности $32L^4$ ($L=48, 32L^4=169,869,312$)
- И работаем с матрицами $12L^4 \times 12L^4$
 $(L=48, 12L^4=63,700,992)$

$$\int d\psi \ d\bar{\psi} \ \exp \{ \bar{\psi} M \psi \} = \det M$$

SU(2) glue SU(3) glu

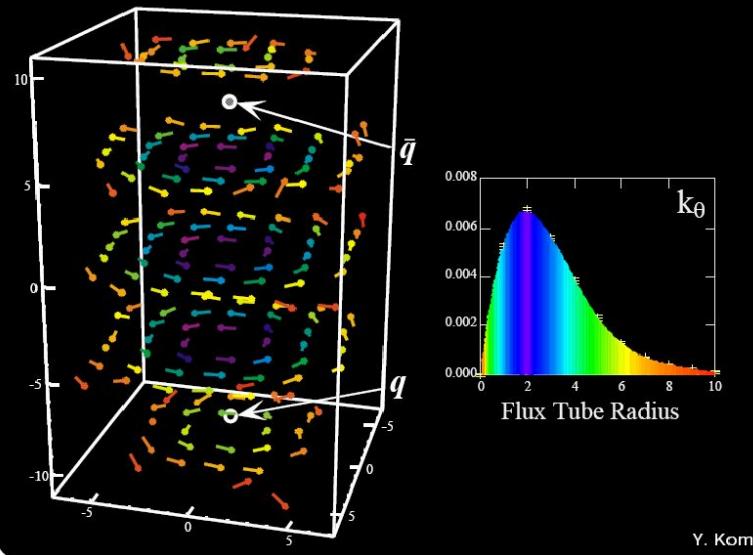
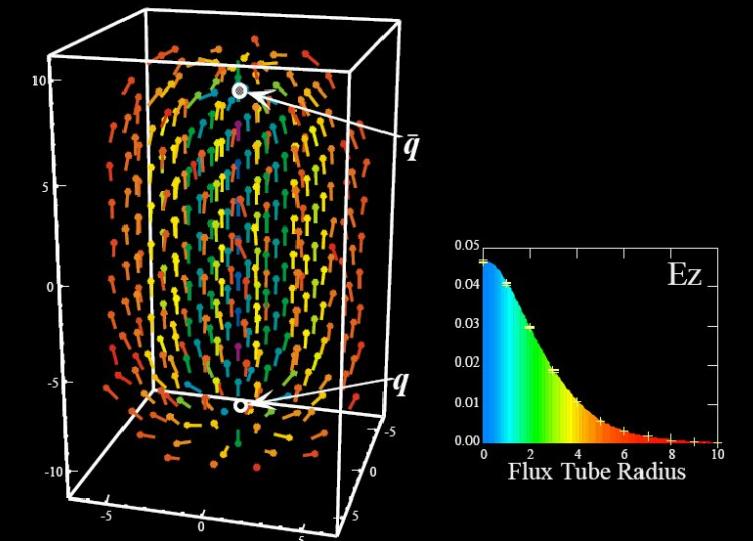
Сила между кварком и антакварком 12 тонн!!!



SU(2) glue

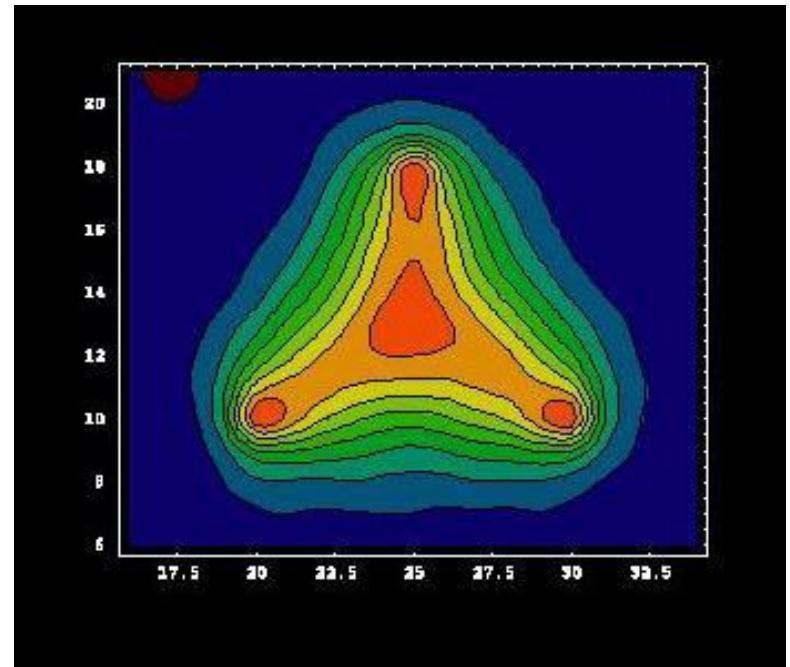
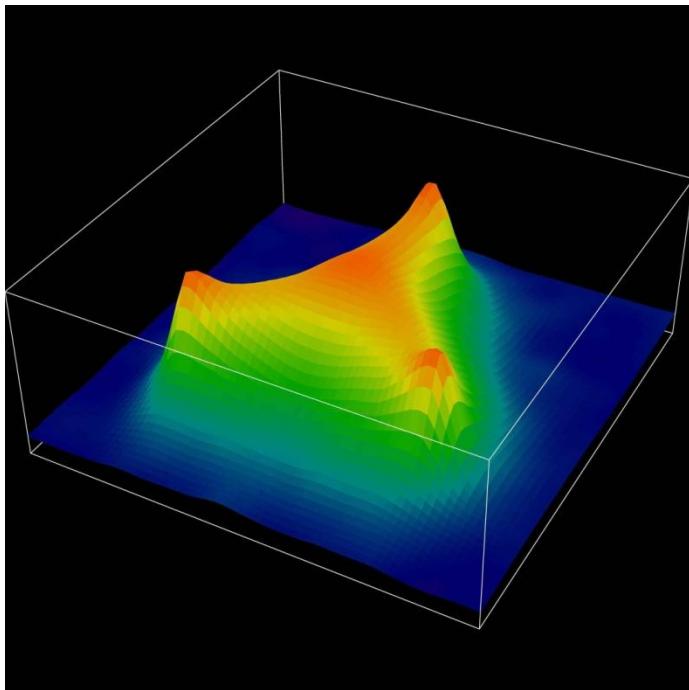
SU(3) glue 3dQCD (2+1)QCD

AP-SU(2) FLUX-TUBE PROFILE



Y. Koma

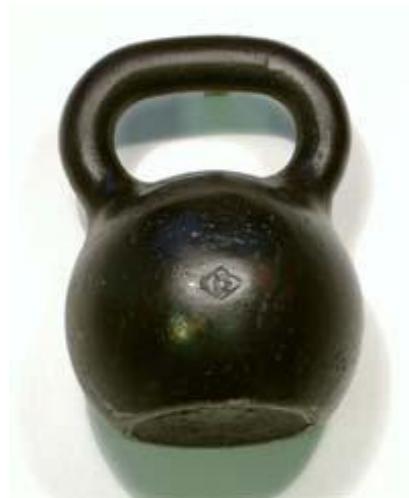
SU(2) glue **SU(3) glue** 2qQCD (2+1)QCD Three body forces!



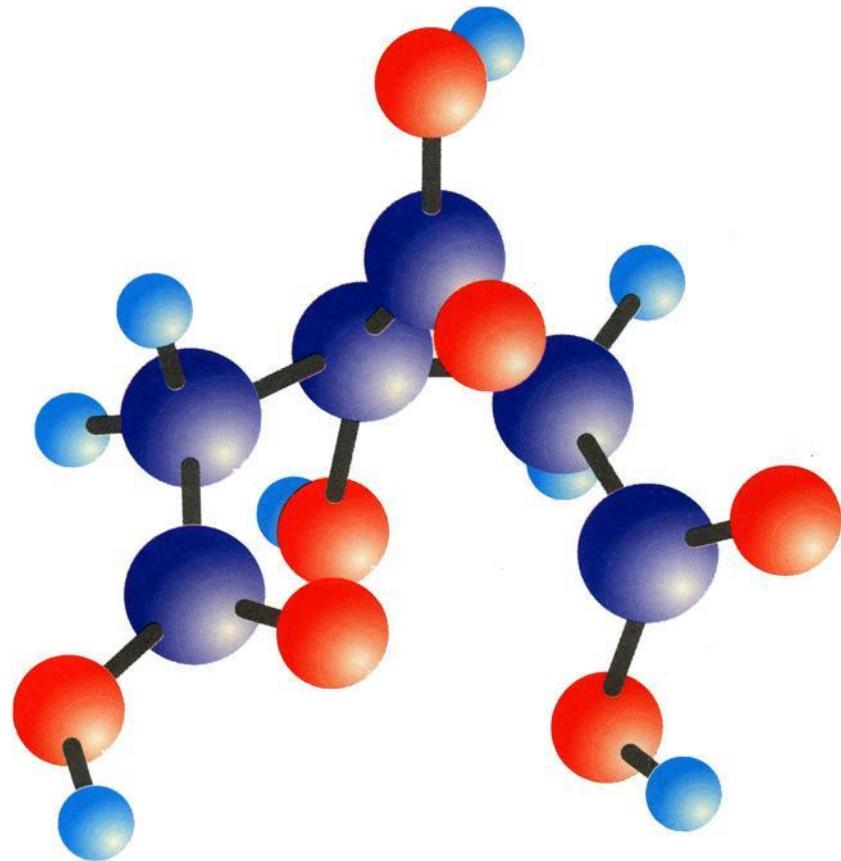
$$V(r_1, r_2, r_3) \neq V(r_1 - r_2) + V(r_2 - r_3) + V(r_3 - r_1)$$

← 1 М →

Происхождение массы



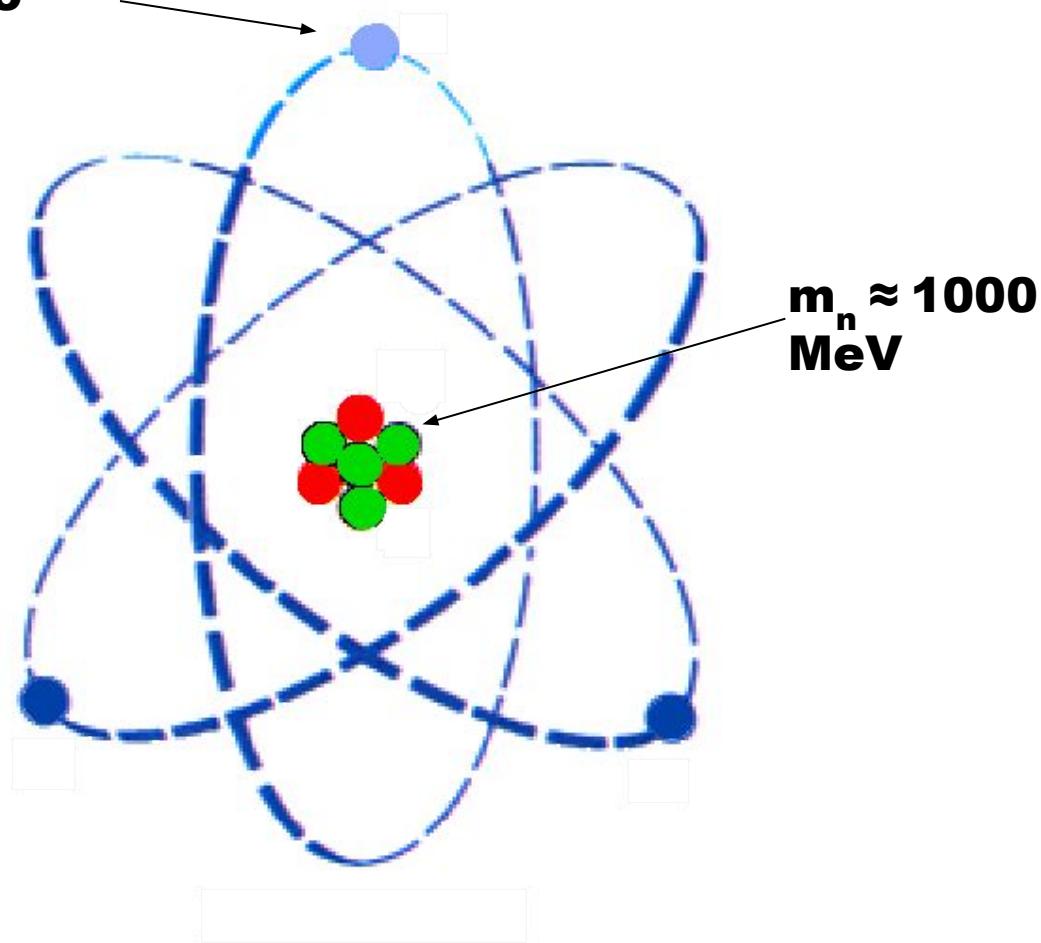
$10^{-8..10} \text{ M}$



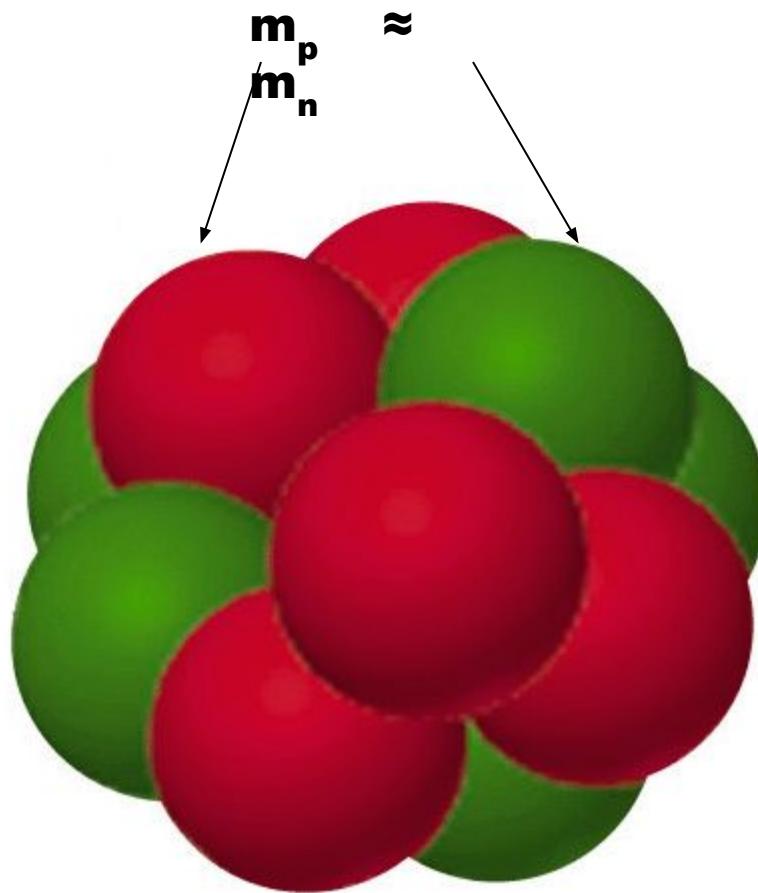
$10^{-10} M$

$m_e \approx 0.5$
MeV

$m_n \approx 1000$
MeV



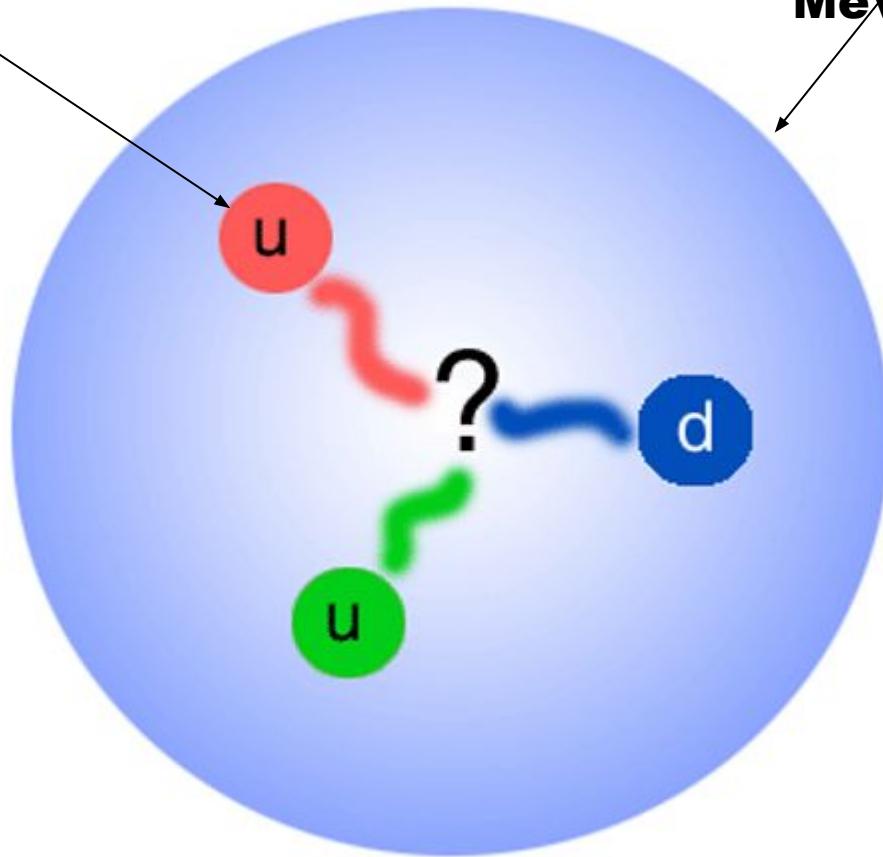
$10^{-14..15} M$



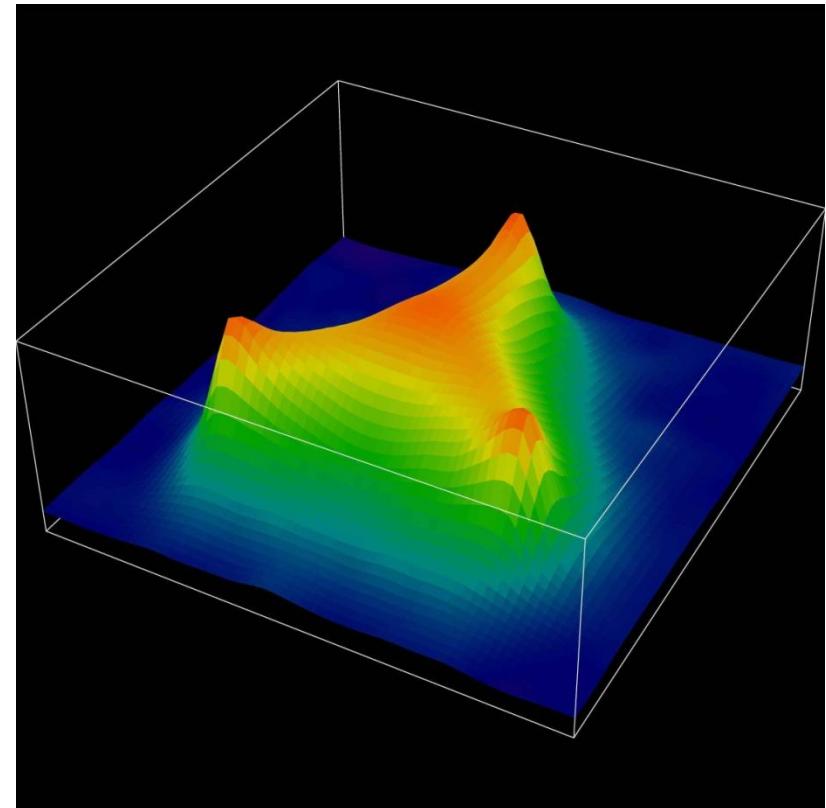
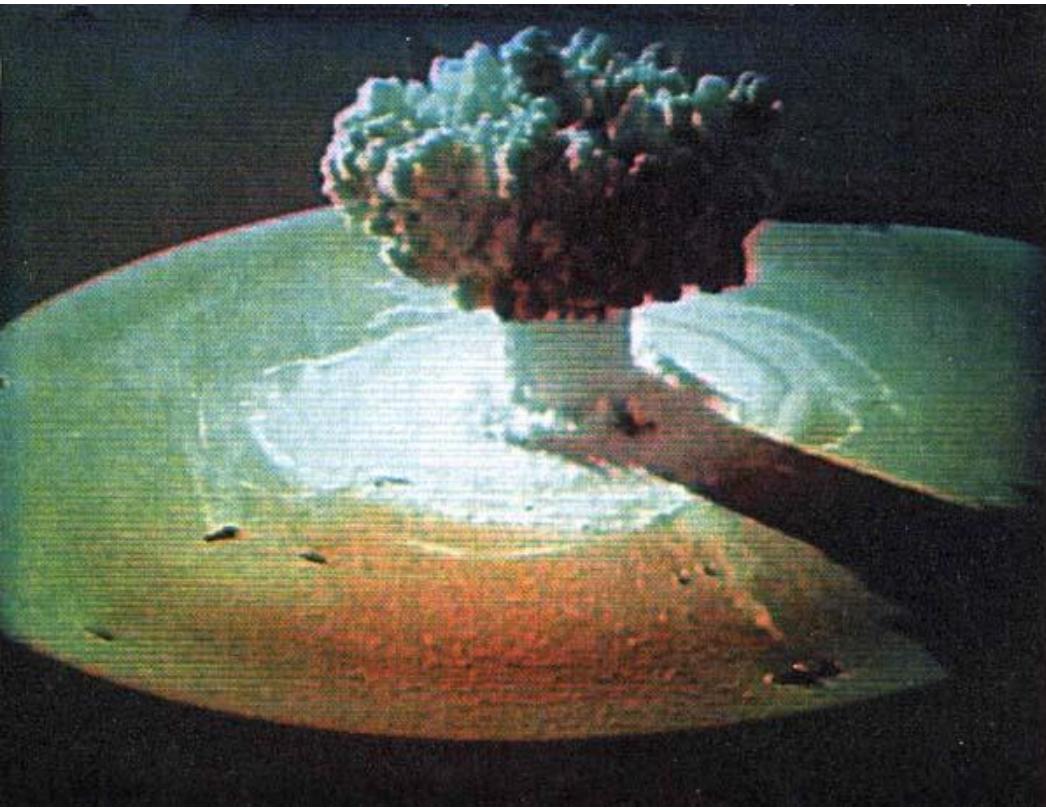
$10^{-15} M$

$m_{u,d} \approx 3..5$ MeV

$m_p \approx 1000$ MeV



Masses of material objects is due to gluon fields inside baryon



$$E = m_0 c^2$$

$$3m_q / m_{baryon} \approx 1/100$$

$$m_0 = \frac{E}{c^2}$$

Three body forces!

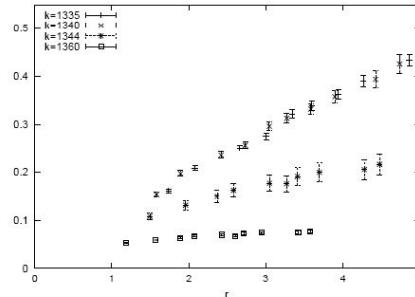
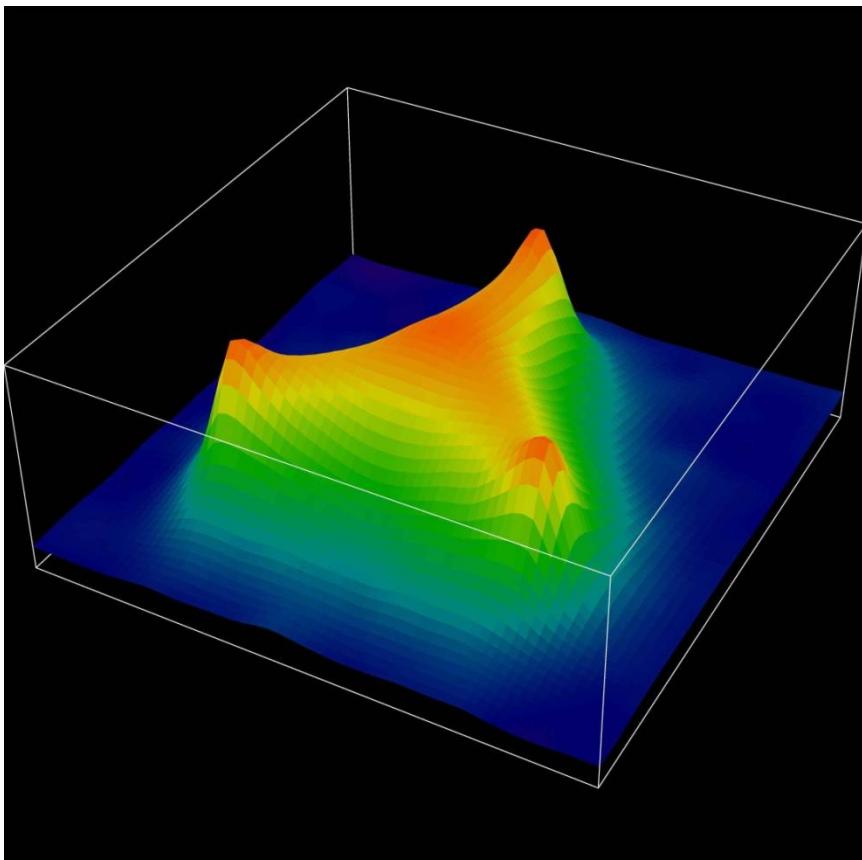


Figure 9: The monopole part of the baryon potential at finite temperature in full QCD as a function of L_Y ($T < T_c$) and L_Δ ($T > T_c$), respectively, in units of *God knows what*.

In Fig. 9 we show the baryon potential on the $16^3 8$ lattice at $\beta = 5.2$ for several values of κ . At this β value

$$T \propto \exp(-2.81/\kappa). \quad (4.1)$$

Increasing κ thus increases the temperature. We cross the finite temperature phase transition at $\kappa = 0.1344$ [14]. We see that the potential flattens off while we approach the transition point. However, the distances we were able to probe are not large enough to make any statement about string breaking.

To compute the action density ρ_A^{3Q} and the electric field and monopole correlators E_i^{3Q} and k^{3Q} , respectively, we need to reduce the statistical noise. Note that the Polyakov loops span an area of $\approx 16 \times 8$ lattice spacings. We do that by using extended operators

$$\begin{aligned} \rho_A^{3Q}(s) \rightarrow & \frac{1}{8} \{ \rho_A^{3Q}(s) + \rho_A^{3Q}(s - \hat{x} - \hat{y} - \hat{z}) + \rho_A^{3Q}(s - \hat{x} - \hat{y}) \\ & + \rho_A^{3Q}(s - \hat{x} - \hat{z}) + \rho_A^{3Q}(s - \hat{y} - \hat{z}) + \rho_A^{3Q}(s - \hat{x}) \\ & + \rho_A^{3Q}(s - \hat{y}) + \rho_A^{3Q}(s - \hat{z}) \}, \end{aligned} \quad (4.2)$$

$$\begin{aligned} E_i^{3Q}(s) \rightarrow & \frac{1}{4} \{ E_i^{3Q}(s) + E_i^{3Q}(s - \hat{x} - \hat{t}) \\ & + E_i^{3Q}(s - \hat{x}) + E_i^{3Q}(s - \hat{t}) \}, \end{aligned} \quad (4.3)$$

$$k^{3Q}(*s, \mu) \rightarrow \frac{1}{2} \{ k^{3Q}(*s, \mu) + k^{3Q}(*s - \hat{z}, \mu) \}, \quad (4.4)$$

where (again) we have assumed that the quarks lie in the (x, y) plane, and we call the direction of the Polyakov lines the t direction.

SU(2) glue SU(3) glue 2qQCD (2+1)QCD

Usually the teams are rather big, 5 - 10 -15 people

arXiv:hep-lat/0401026v1

arXiv:hep-lat/0401026v2

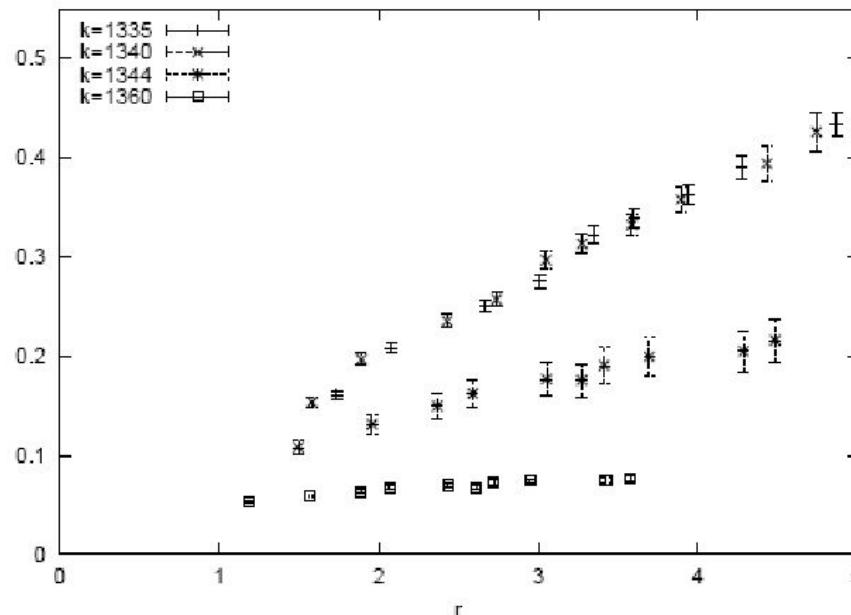
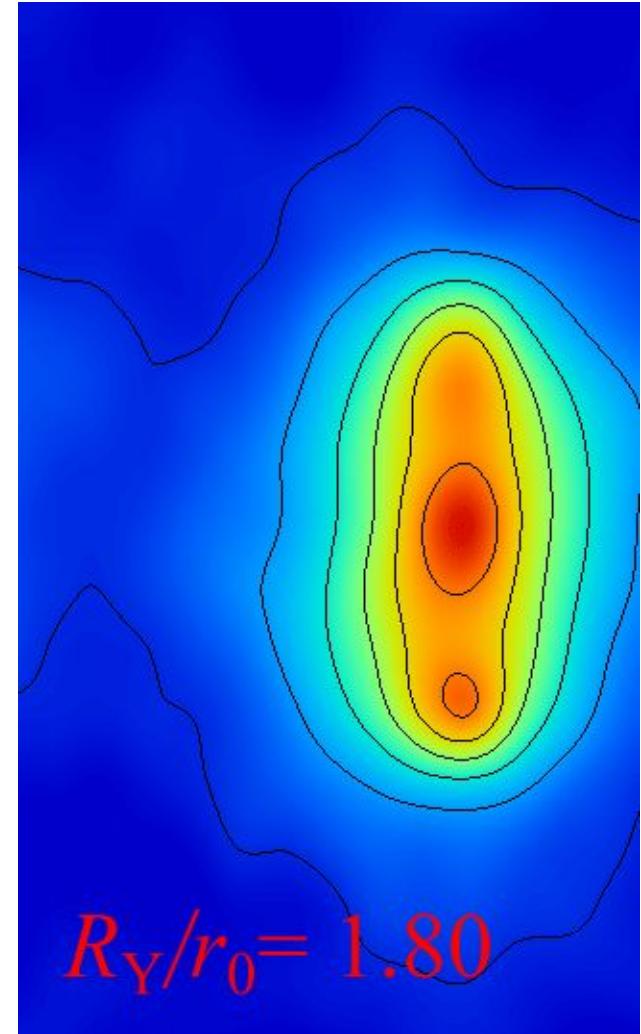
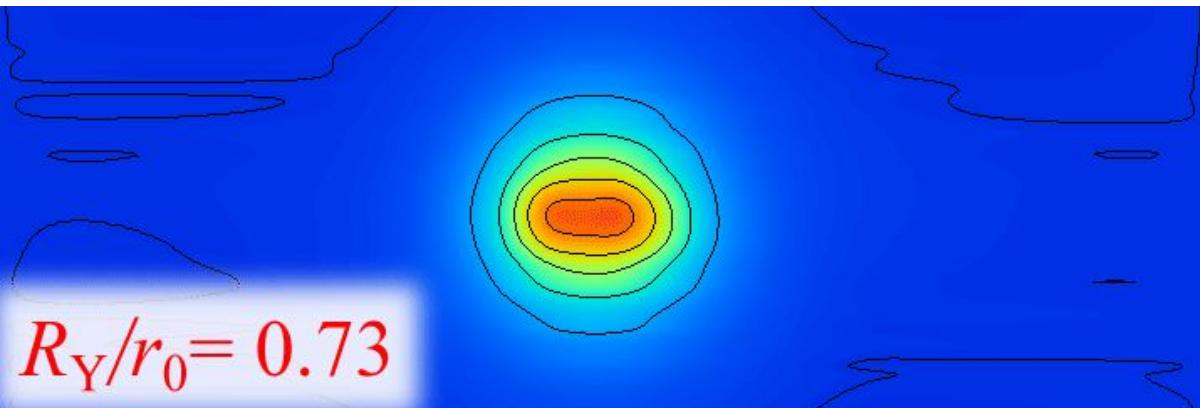


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In Fig. 9 we show the baryon potential on the $16^3 \times 8$ lattice at $\beta = 5.2$ for several values of κ . At this β value

SU(2) glue SU(3) glue 2qQCD (2+1)QCD String Breaking (DIK collaboration)



SU(2) glue SU(3) glue 2qQCD (2+1)QCD

Hadron Mass Spectrum

SU(2) glue SU(3) glue 2qQCD (2+1)QCD

Meson Summary Table

See also the table of suggested $q\bar{q}$ quark-model assignments in the Quark Model section.

• Indicates particles that appear in the preceding Meson Summary Table. We do not regard the other entries as being established.

† Indicates that the value of J given is preferred, but needs confirmation.

LIGHT UNFLAVORED ($S = C \neq B = 0$)		STRANGE ($S = \pm 1, C = B = 0$)		BOTTOM ($B = \pm 1$)	
$J^G(J^P)$	$J^G(J^P)$	$J^G(J^P)$	$J^G(J^P)$	$J^G(J^P)$	$J^G(J^P)$
• π^\pm	1 ⁻ (0 ⁻)	• $\pi_2(1670)$	1 ⁻ (2 ⁻)	• B^\pm	1/2(0 ⁻)
• π^0	1 ⁻ (0 ⁻ +)	• $\phi(1680)$	0 ⁻ (1 ⁻)	• B^0	1/2(0 ⁻)
• η	0 ⁺ (0 ⁻ +)	• $\rho_3(1690)$	1 ⁺ (3 ⁻)	• B_s^0/B^0 ADMIXTURE	
• $f_0(600)$	0 ⁺ (0 ⁺ +)	• $\rho(1700)$	1 ⁺ (1 ⁻)	• $B_s^+/B^0/b$ -baryon AD- MIXTURE _E	
• $\rho(770)$	1 ⁺ (1 ⁻ -)	• $a_2(1700)$	1 ⁺ (2 ⁺)	• V_{cb} and V_{ub} CKM Matrix Elements	
• $\omega(782)$	0 ⁻ (1 ⁻ -)	• $f_0(1710)$	0 ^{+(0⁺ +)}	• $K_0(800)$	1/2(0 ⁺)
• $\eta'(958)$	0 ^{+(0⁻ +)}	• $\eta(1760)$	0 ^{+(0⁻ +)}	• $K^*(892)$	1/2(1 ⁻)
• $f_0(980)$	0 ^{+(0⁺ +)}	• $\pi(1800)$	1 ^{-(0⁻ +)}	• $K_1(1270)$	1/2(1 ⁺)
• $a_0(980)$	1 ^{-(0⁻ +)}	• $f_2(1810)$	0 ^{+(2⁺ +)}	• $K_1(1400)$	1/2(1 ⁺)
• $\phi(1020)$	0 ^{-(1⁻ -)}	• $X(1835)$? ^{?(? -)}	• $K^*(1410)$	1/2(1 ⁻)
• $h_1(1170)$	0 ^{-(1⁻ +)}	• $\phi_3(1850)$	0 ^{-(3⁻ -)}	• $K_0^*(1430)$	1/2(0 ⁺)
• $b_1(1235)$	1 ^{+(1⁻ +)}	• $\eta_2(1870)$	0 ^{+(2⁺ -)}	• $K_2^*(1430)$	1/2(2 ⁺)
• $a_1(1260)$	1 ^{-(1⁻ +)}	• $\rho(1900)$	1 ^{+(1⁻ -)}	• $K(1460)$	1/2(0 ⁻)
• $f_2(1270)$	0 ^{+(2⁻ +)}	• $f_2(1910)$	0 ^{+(2⁺ +)}	• $K_2(1580)$	1/2(2 ⁻)
• $f_1(1285)$	0 ^{+(1⁻ +)}	• $f_2(1950)$	0 ^{+(2⁺ +)}	• $K(1630)$	1/2(? [?])
• $\eta(1295)$	0 ^{+(0⁻ +)}	• $\rho_3(1990)$	1 ^{+(3⁻ -)}	• $K_1(1650)$	1/2(1 ⁺)
• $\pi(1300)$	1 ^{-(0⁻ +)}	• $f_2(2010)$	0 ^{+(2⁺ +)}	• $K^*(1680)$	1/2(1 ⁻)
• $a_2(1320)$	1 ^{-(2⁻ +)}	• $f_0(2020)$	0 ^{+(0⁺ +)}	• $K_2(1770)$	1/2(2 ⁻)
• $f_0(1370)$	0 ^{+(0⁻ +)}	• $a_4(2040)$	1 ^{-(4⁻ +)}	• $K_3^*(1780)$	1/2(3 ⁻)
• $h_1(1380)$? ^{-(1⁻ -)}	• $f_4(2050)$	0 ^{+(4⁻ +)}	• $K_2(1820)$	1/2(2 ⁻)
• $\pi_1(1400)$	1 ^{-(1⁻ +)}	• $\pi_2(2100)$	1 ^{-(2⁻ +)}	• $K(1830)$	1/2(0 ⁻)
• $\eta(1405)$	0 ^{+(0⁻ +)}	• $f_0(2100)$	0 ^{+(0⁺ +)}	• $K_0^*(1950)$	1/2(0 ⁺)
• $f_1(1420)$	0 ^{+(1⁻ +)}	• $f_2(2150)$	0 ^{+(2⁺ +)}	• $K_2^*(1980)$	1/2(2 ⁺)
• $\omega(1420)$	0 ^{-(1⁻ -)}	• $\rho(2150)$	1 ^{+(1⁻ -)}	• $K_4(2045)$	1/2(4 ⁺)
• $f_2(1430)$	0 ^{+(2⁻ +)}	• $f_0(2200)$	0 ^{+(0⁺ +)}	• $K_2(2250)$	1/2(2 ⁻)
• $a_0(1450)$	1 ^{-(0⁻ +)}	• $f_j(2220)$	0 ^{+(2 or 4⁻ +)}	• $K_3(2320)$	1/2(3 ⁺)
• $\rho(1450)$	1 ^{+(1⁻ -)}	• $\eta(2225)$	0 ^{+(0⁻ +)}	• $K_5^*(2380)$	1/2(5 ⁻)
• $\eta(1475)$	0 ^{+(0⁻ +)}	• $\rho_3(2250)$	1 ^{+(3⁻ -)}	• $K_4(2500)$	1/2(4 ⁻)
• $f_0(1495)$	0 ^{+(0⁻ +)}	• $f_2(2300)$	0 ^{+(2⁺ +)}	• $K(2500)$	1/2(4 ⁻)
• $f_0(1500)$	0 ^{+(0⁻ +)}	• $f_2(2300)$	0 ^{+(2⁺ +)}	• $K(3100)$? ^{?(? ?)}
• $f_1(1510)$	0 ^{+(1⁻ +)}				
• $f_2'(1525)$	0 ^{+(2⁻ +)}	• $f_2(2340)$	0 ^{+(2⁺ +)}		
• $f_2(1565)$	0 ^{+(2⁻ +)}				
• $\eta_5(1595)$	0 ^{-(1⁻ +)}	• $\rho_5(2350)$	1 ^{+(5⁻ -)}		
• $\pi_1(1600)$	1 ^{-(1⁻ +)}	• $a_6(2450)$	1 ^{-(6⁻ +)}		
• $a_1(1640)$	1 ^{-(1⁻ +)}	• $f_0(2510)$	0 ^{+(6⁻ +)}		
• $\eta_2(1645)$	0 ^{+(2⁻ +)}				
• $\omega(1650)$	0 ^{-(1⁻ -)}				
• $\omega_3(1670)$	0 ^{-(3⁻ -)}				
OTHER LIGHT					
Further States					
$b\bar{b}$					
$D_s^0(2400)^{\pm}$					
$D_1(2420)^0$					
$D_1(2420)^{\pm}$					
$D_1(2430)^0$					
$D_s^*(2460)^0$					
$D_s^*(2460)^{\pm}$					
$D_s^*(2460)^{\pm}$					
$D^*(2640)^{\pm}$					
CHARMED, STRANGE ($C = S = \pm 1$)					
D_s^{\pm}					
$D_s^{*\pm}$					
$D_s^{*\pm}(2317)^{\pm}$					
$D_{s1}^*(2460)^{\pm}$					
$D_{s1}^*(2536)^{\pm}$					
$D_{s2}^*(2573)^{\pm}$					
NON- qq CANDIDATES					

159

130

**** Existence is certain, and properties are at least fairly well explored.

*** Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

** Evidence of existence is only fair.

* Evidence of existence is poor.

Baryon Summary Table

This short table gives the name, the quantum numbers (where known), and the status of baryons in the Review. Only the baryons with 3-star or 4-star status are included in the main Baryon Summary Table. Due to insufficient data or uncertain interpretation, the other entries in the short table are not established as baryons. The names with masses are of baryons that decay strongly. For N , Δ , and Ξ resonances, the partial wave is indicated by the symbol $L_{2J,2J}$, where L is the orbital angular momentum (S , P , D , ...), I is the isospin, and J is the total angular momentum. For Λ and Σ resonances, the symbol is $L_{1,2J}$.

p	P_{11}	****	$\Delta(1232)$	P_{33}	****	Λ	P_{01}	****	Σ^+	P_{11}	****	Ξ^0	P_{11}	****
n	P_{11}	****	$\Delta(1600)$	P_{33}	***	$\Lambda(1405)$	S_{01}	****	Σ^0	P_{11}	****	Ξ^-	P_{11}	****
$N(1440)$	P_{11}	****	$\Delta(1620)$	S_{31}	****	$\Lambda(1520)$	D_{03}	****	Σ^-	P_{11}	****	$\Xi(1530)$	P_{13}	***
$N(1520)$	D_{13}	****	$\Delta(1700)$	D_{33}	****	$\Lambda(1600)$	P_{01}	***	$\Sigma(1385)$	P_{13}	****	$\Xi(1620)$	*	
$N(1535)$	S_{11}	****	$\Delta(1750)$	P_{31}	*	$\Lambda(1670)$	S_{01}	****	$\Sigma(1480)$	*		$\Xi(1690)$		***
$N(1650)$	S_{11}	***	$\Delta(1900)$	S_{31}	**	$\Lambda(1690)$	D_{03}	****	$\Sigma(1560)$	*		$\Xi(1820)$	D_{13}	***
$N(1675)$	D_{15}	****	$\Delta(1905)$	F_{35}	****	$\Lambda(1800)$	S_{01}	***	$\Sigma(1580)$	D_{13}	*	$\Xi(1950)$		***
$N(1680)$	F_{15}	****	$\Delta(1910)$	P_{31}	****	$\Lambda(1810)$	P_{01}	***	$\Sigma(1620)$	S_{11}	**	$\Xi(2030)$		***
$N(1700)$	D_{13}	***	$\Delta(1920)$	P_{33}	***	$\Lambda(1820)$	F_{05}	****	$\Sigma(1660)$	P_{11}	***	$\Xi(2120)$	*	
$N(1710)$	P_{11}	***	$\Delta(1930)$	D_{35}	***	$\Lambda(1830)$	D_{05}	****	$\Sigma(1670)$	D_{13}	***	$\Xi(2250)$		**
$N(1720)$	P_{13}	****	$\Delta(1940)$	D_{33}	*	$\Lambda(1890)$	P_{03}	****	$\Sigma(1690)$	*		$\Xi(2370)$		**
$N(1900)$	P_{17}	**	$\Delta(1950)$	F_{37}	****	$\Lambda(2000)$	F_{07}	*	$\Sigma(1770)$	P_{11}	*			
$N(2000)$	F_{15}	**	$\Delta(2150)$	S_{31}	*	$\Lambda(2100)$	G_{07}	****	$\Sigma(1775)$	D_{15}	****	Ω^-		****
$N(2080)$	D_{13}	**	$\Delta(2200)$	G_{37}	*	$\Lambda(2110)$	F_{05}	***	$\Sigma(1840)$	P_{13}	*	$\Omega(2250)$		***
$N(2090)$	S_{11}	*	$\Delta(2300)$	H_{39}	**	$\Lambda(2325)$	D_{03}	*	$\Sigma(1880)$	P_{11}	**	$\Omega(2380)$		**
$N(2100)$	P_{11}	*	$\Delta(2350)$	D_{35}	*	$\Lambda(2350)$	H_{09}	***	$\Sigma(1915)$	F_{15}	***	$\Omega(2470)$		**
$N(2190)$	G_{17}	****	$\Delta(2390)$	F_{37}	*	$\Lambda(2395)$	D_{13}	***	$\Sigma(1940)$	D_{13}	***			
$N(2200)$	D_{15}	**	$\Delta(2400)$	G_{39}	**				$\Sigma(2000)$	S_{11}	*	Λ_c^+		****
$N(2220)$	H_{19}	****	$\Delta(2420)$	$H_{3,11}$	****				$\Sigma(2030)$	F_{17}	****	$\Lambda_c(2593)^+$		***
$N(2250)$	G_{19}	****	$\Delta(2750)$	$I_{3,13}$	**				$\Sigma(2070)$	F_{15}	*	$\Lambda_c(2625)^+$		***
$N(2600)$	$I_{1,11}$	***	$\Delta(2950)$	$K_{3,15}$	**				$\Sigma(2080)$	P_{13}	**	$\Lambda_c(2765)$		*
$N(2700)$	$K_{1,13}$	**							$\Sigma(2100)$	G_{17}	*	$\Lambda_c(2880)^+$		**
			$\Theta(1540)^+$		*				$\Sigma(2250)$		***	$\Sigma_c(2455)$		****
									$\Sigma(2455)$		**	$\Sigma_c(2520)$		***
									$\Sigma(2620)$		**	$\Sigma_c(2800)$		***
									$\Sigma(3000)$	*		Ξ_c^+		***
									$\Sigma(3170)$	*		Ξ_c^0		***
												Ξ_c^+		***
												$\Xi_c(2645)$		***
												$\Xi_c(2790)$		***
												$\Xi_c(2815)$		***
												Ω_c^0		***
														*

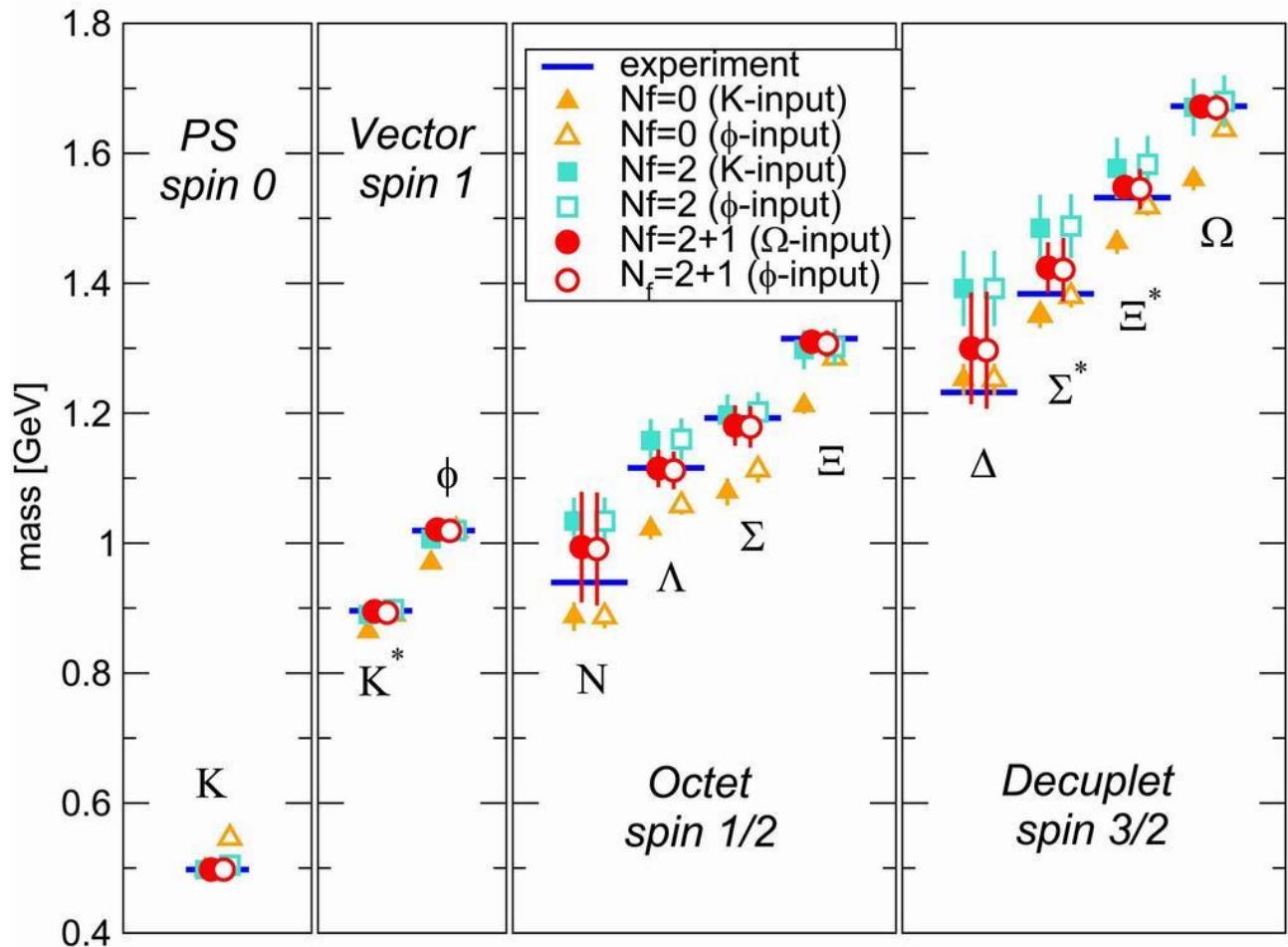
												Λ_b^0		***
												Ξ_b^0	Ξ_b^-	*

SU(2) glue SU(3) glue 2qQCD (2+1)QCD

Wilson non-perturbatively improved Fermions
“WORKING HORSE” of lattice QCD calculations

Y. Kuramashi Lattice 2007

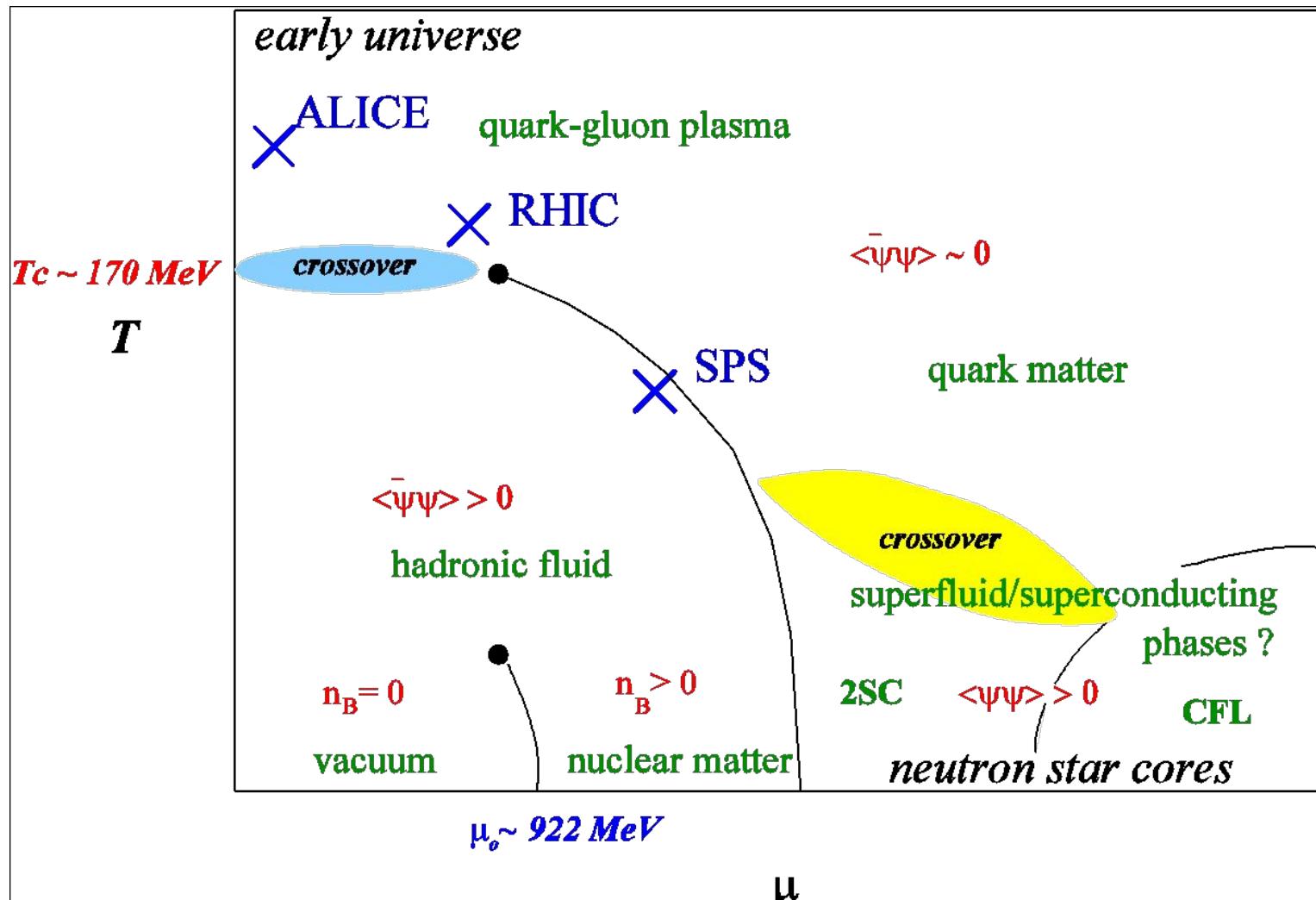
Iwasaki gauge action +
clover quarks
 $a^{-1} = 2.2\text{GeV}$,
lattice size: $32^3 \times 64$



SU(2) glue SU(3) glue 2qQCD (2+1)QCD

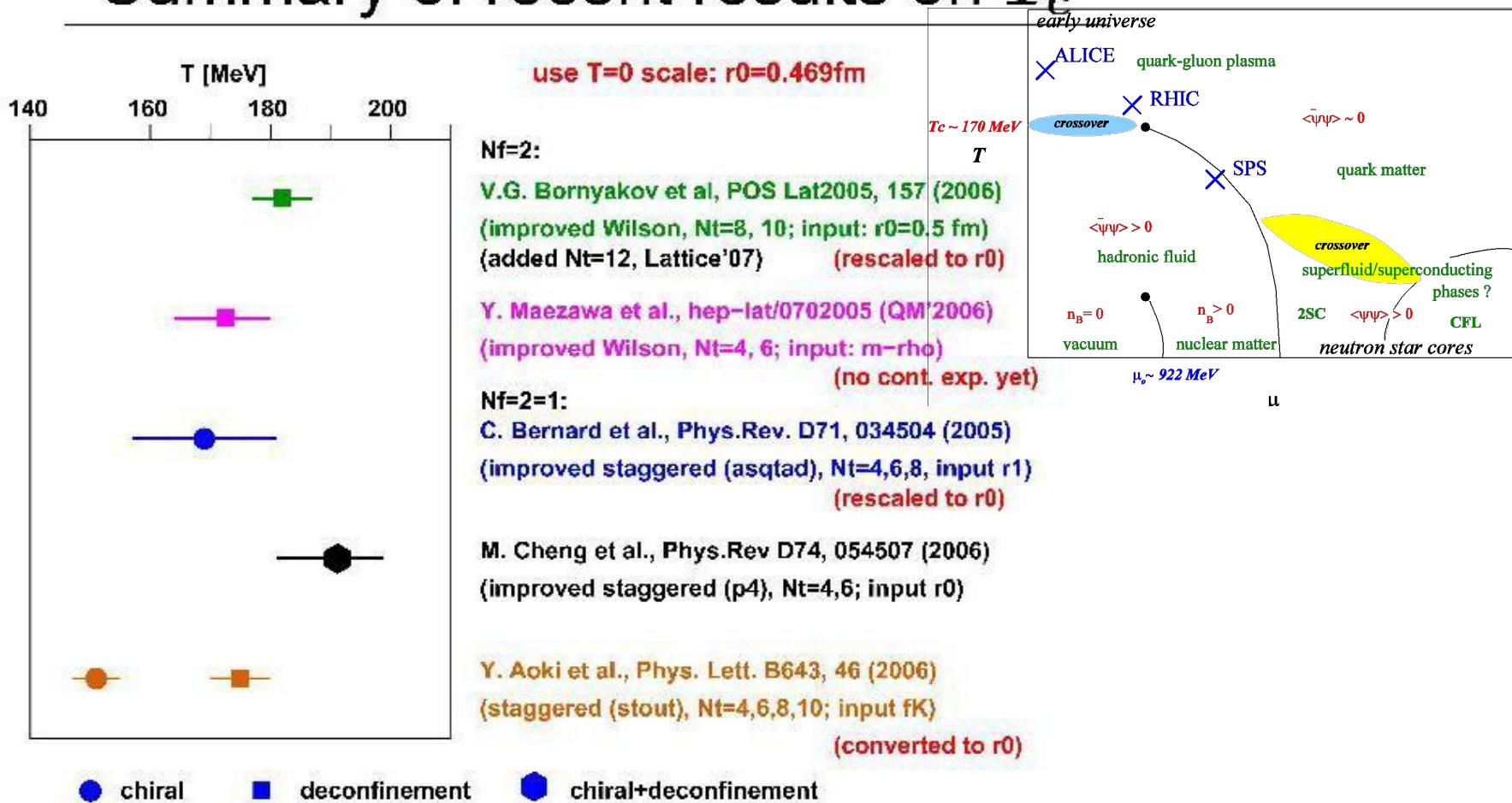
Finite Temperature

Фазовая Диаграмма КХД



Фазовая Диаграмма КХД

Summary of recent results on T_c



Моделирование К-Г плазмы в США

Proceedings of the DPF-2009 Conference, Detroit, MI, July 27-31, 2009

1

Equation of State and the Finite Temperature Transition in QCD

Rajan Gupta [HotQCD Collaboration]
Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA

This talk provides a summary of the results obtained by the HotQCD collaboration on the equation of state and the crossover transition in 2+1 flavor QCD. We investigate bulk thermodynamic quantities - energy density, pressure, entropy density, and the speed of sound over the temperature range $140 < T < 540$ MeV. These results have been obtained on lattices of temporal size $N_t = 6$ and 8 and with two improved staggered fermion actions, asqcd and p4. Our most extensive results are with masses of the two degenerate light quarks set at $m_l = 0.1m_s$ corresponding to the Goldstone pion mass m_π between 230 – 260 MeV. In these simulations, the strange quark mass is tuned to its physical value and constant values of m_l/m_s define lines of constant physics. We also summarize the current state of results on observables sensitive to the chiral and deconfining physics – the light and strange quark number susceptibilities, the chiral condensate and its susceptibility, and the renormalized Polyakov loop. Our results indicate that the deconfinement and chiral symmetry restoration occur in the same narrow temperature interval.

arXiv:0912.1374v1 [hep-lat] 7 Dec 2009

1. Introduction

Ongoing experiments at RHIC and proposed experiments at LHC aim to understand the properties of hot dense nuclear matter created in the collision of two relativistic nuclei. At sufficiently high temperatures and densities RHIC data support the creation of a quark-gluon plasma in the central region that undergoes a transition back to hadronic matter as it expands and cools. The goal is to explain the creation and evolution of this medium. Hydrodynamic descriptions used to model this evolution provide a good fit to the data and are thus the phenomenological tool of choice. First principle calculations using lattice QCD yield a number of properties of QCD as a function of temperature that are essential inputs in these hydrodynamical analyses. These properties include the nature of the transition (with respect to both confinement and chiral symmetry breaking) between the quark-gluon plasma and hadronic matter, the transition temperature, the equation of state of QCD and transport coefficients as a function of temperature in the range 140 – 700 MeV.

HotQCD is a US wide collaboration engaged in the study of QCD at finite temperature and density using lattice QCD¹. It brought together members of the MILC and RBC-Bielefeld collaborations to carry out large scale simulations on IBM BlueGene/L supercomputers at the Lawrence Livermore National Lab and on the NYSBlue at the New York Center for Computational Sciences at BNL.

Our goals are to perform detailed simulations of

2+1 flavor QCD using staggered fermions at the physical values of the strange and light quark masses. Most of the results presented here are for $m_l = 0.1m_s$, about a factor of two heavier than the mean physical u and d quark mass, $m_s \approx 0.03m_u$. Improvements in algorithms and computer resources are being used to incrementally approach the physical up and down quark masses and the continuum limit, thus providing high precision results. Also, in the current simulations the up and down quark masses are taken to be degenerate.

The physical quantities we are calculating include:

- The Equation of State (EoS) of QCD over the temperature range 140 – 700 MeV that is being probed by relativistic heavy ion experiments at Brookhaven and will be studied in more detail in the future at the LHC.
- The nature of the deconfinement transition between the hadronic phase at low temperature and the quark-gluon plasma at high temperatures. All simulations with staggered fermions show a rapid crossover rather than a genuine phase transition for physical values of the light quark masses. In the absence of a phase transition, there is *a priori* no unique transition temperature as it can depend on the probe. Thus, the temperature at which this transition takes place remains a subject of investigation. The status of current estimates is discussed at the end of this paper.
- The restoration of chiral symmetry at high temperature and whether this chiral transition is coincident with the deconfining transition.
- A detailed understanding of the physics in the transition region and the approach of thermodynamics quantities such as pressure, entropy, energy density and the speed of sound, to the Stefan-Boltzmann limit.

¹HotQCD Collaboration members are: A. Bazavov, T. Bhattacharya, M. Cheng, N.E. Christ, C. DeTar, S. Ejiri, S. Gottlieb, R. Gupta, U.M. Heller, K. Hebeler, C. Jung, F. Karsch, E. Laermann, L. Levkova, C. Michael, R.D. Mawhinney, P. Petreczky, C. Schmidt, R.A. Soltz, W. Soeldner, R. Sugar, D. Toussaint and P. Vranas

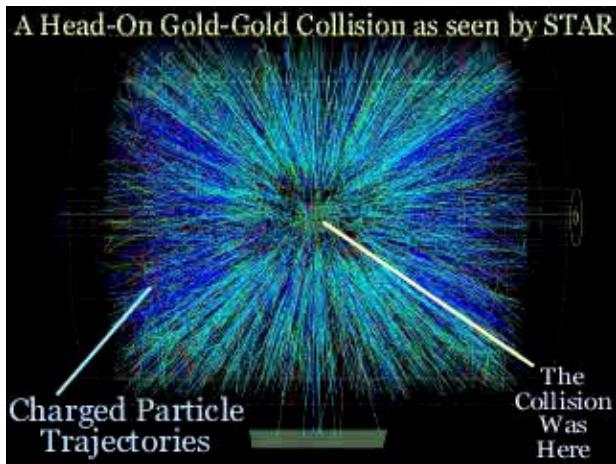
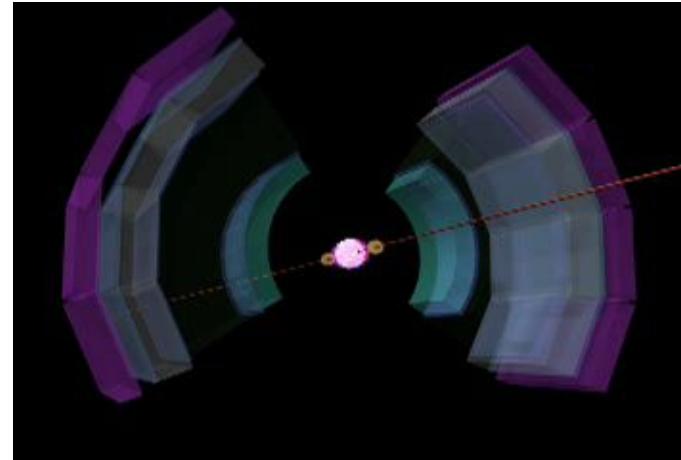
Моделирование К-Г плазмы в США

HotQCD is a US wide collaboration engaged in the study of QCD at finite temperature and density using lattice QCD ¹. It brought together members of the MILC and RBC-Bielefeld collaborations to carry out large scale simulations on IBM Bluegene/L supercomputers at the Lawrence Livermore National Lab and on the NYBlue at the New York Center for Computational Sciences at BNL.



SU(2) glue SU(3) glue

2qQCD(2+1)QCD



early universe

ALICE quark-gluon plasma

RHIC crossover

$T_c \sim 170 \text{ MeV}$

T

$\langle \bar{\psi} \psi \rangle > 0$

hadronic fluid

$n_B = 0$

vacuum

$n_B > 0$

nuclear matter

$\mu_e \sim 922 \text{ MeV}$

μ

$\langle \bar{\psi} \psi \rangle \sim 0$

quark matter

crossover

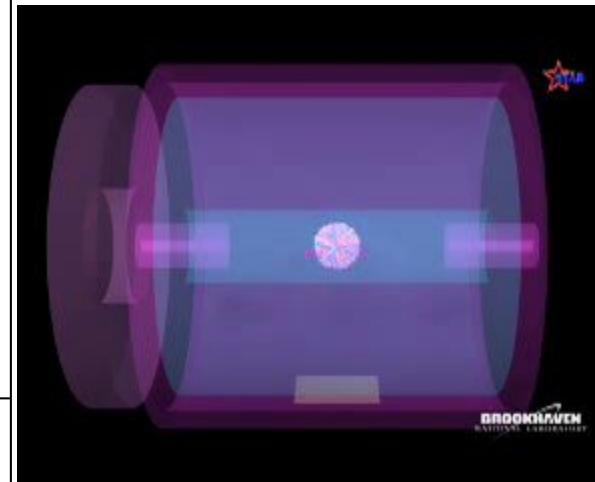
superfluid/superconducting phases ?

2SC

$\langle \bar{\psi} \psi \rangle > 0$

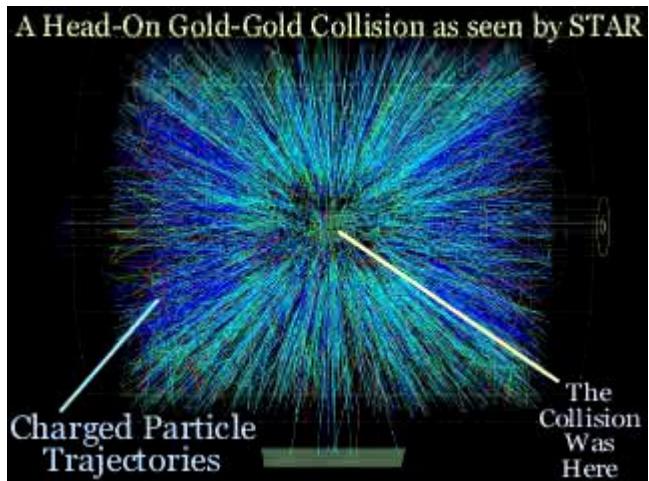
CFL

neutron star cores

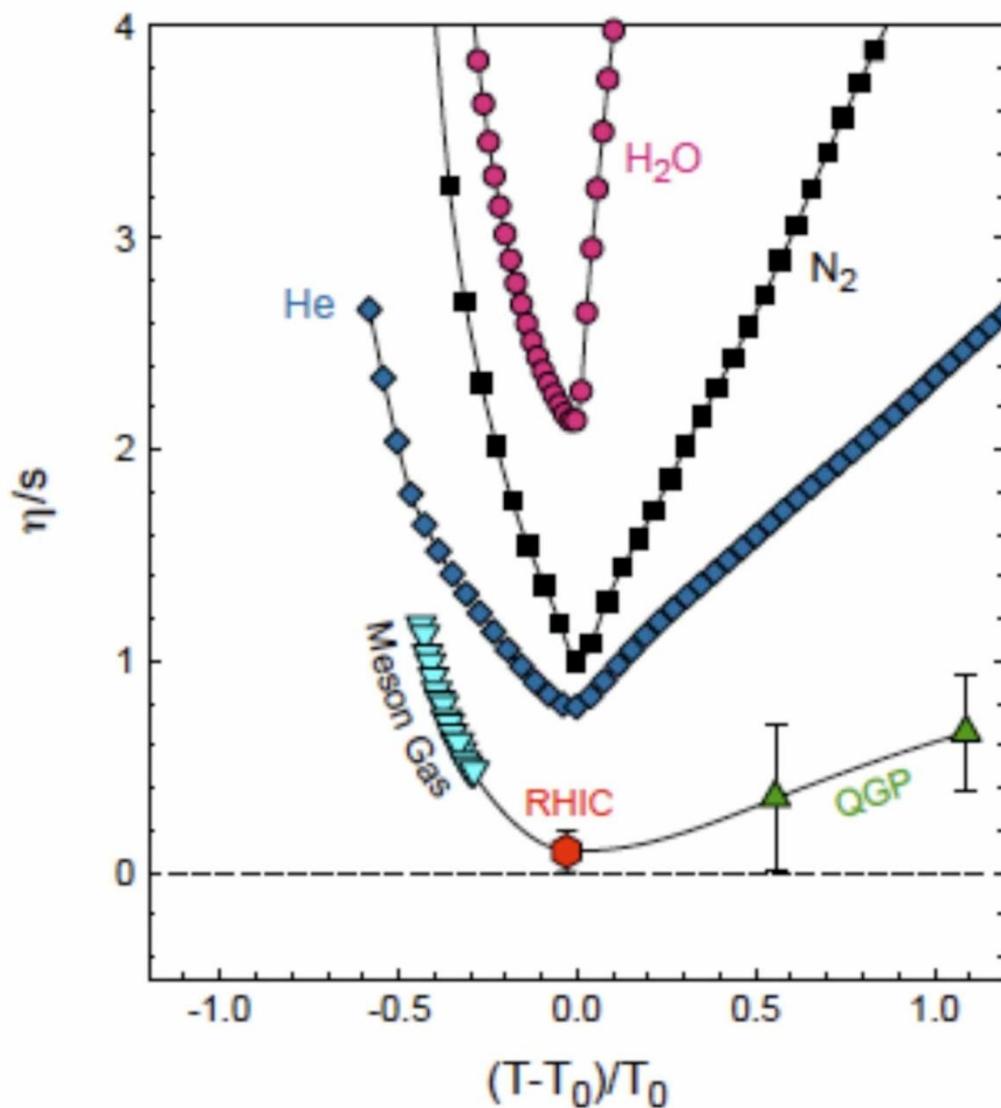


RHIC

RHIC Collisions



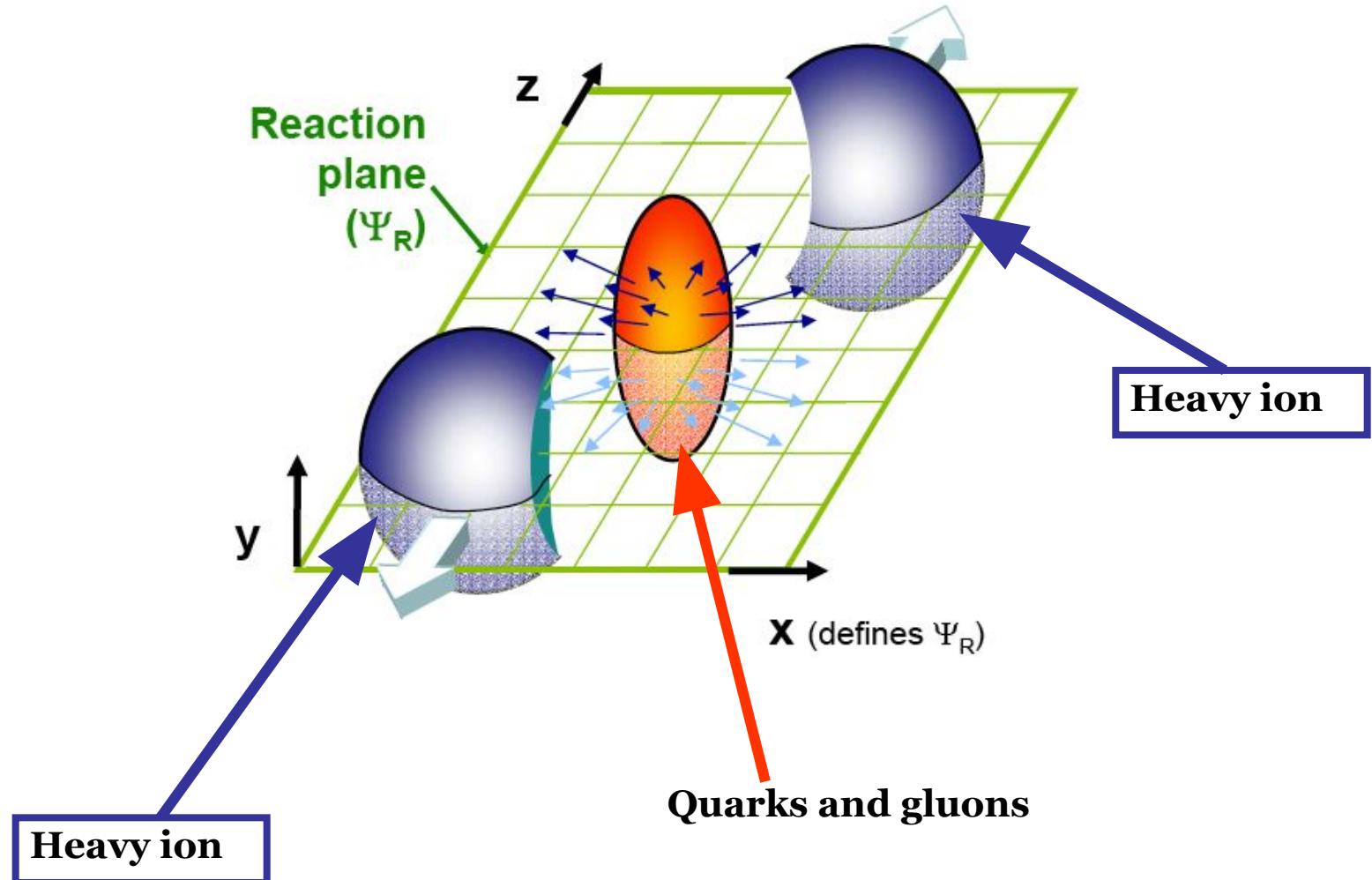
Вязкость К-Г плазмы чрезвычайно мала



Below I use a lot of slides made
by
M.N. Chernodub, P.V.
Buividovich and D.E. Kharzeev

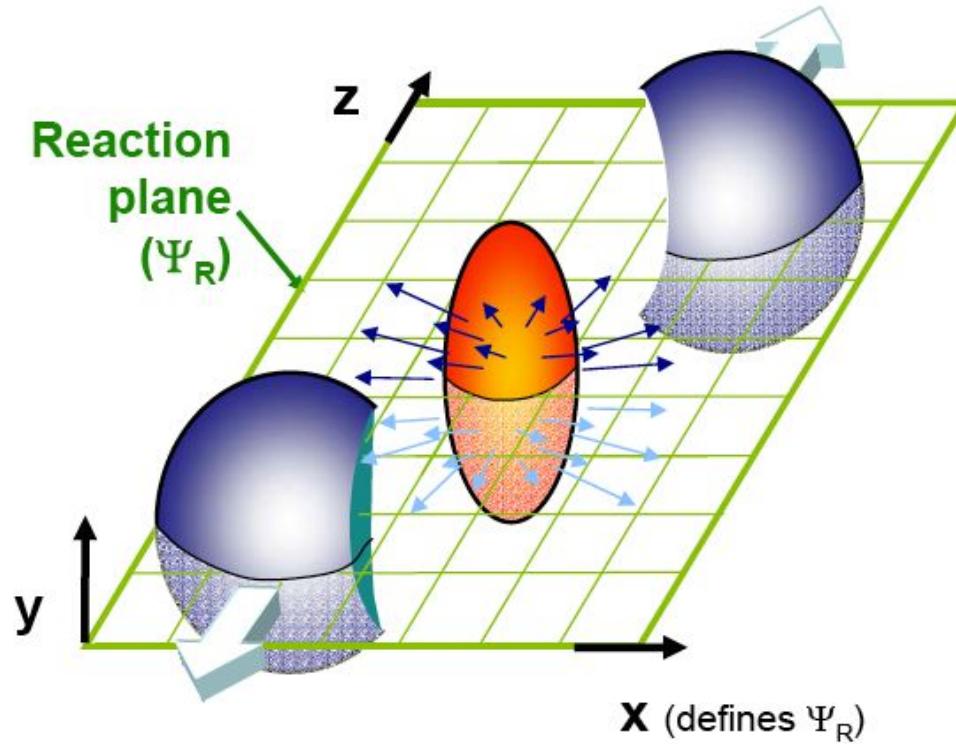
Magnetic fields in non-central collisions

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]



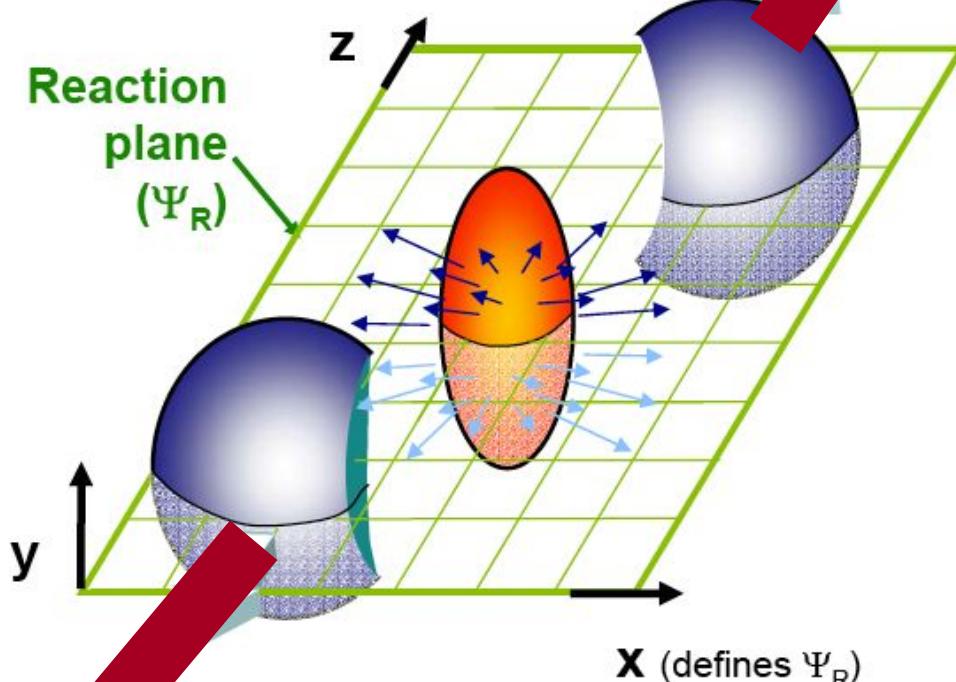
Magnetic fields in non-central collisions

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]



- [1] K. Fukushima, D. E. Kharzeev, and H. J. Warringa, Phys. Rev. D **78**, 074033 (2008), URL <http://arxiv.org/abs/0808.3382>.
- [2] D. Kharzeev, R. D. Pisarski, and M. H. G. Tytgat, Phys. Rev. Lett. **81**, 512 (1998), URL <http://arxiv.org/abs/hep-ph/9804221>.
- [3] D. Kharzeev, Phys. Lett. B **633**, 260 (2006), URL <http://arxiv.org/abs/hep-ph/0406125>.
- [4] D. E. Kharzeev, L. D. McLerran, and H. J. Warringa, Nucl. Phys. A **803**, 227 (2008), URL <http://arxiv.org/abs/0711.0950>.

Magnetic fields in non-central collisions



Charge is large
Velocity is high

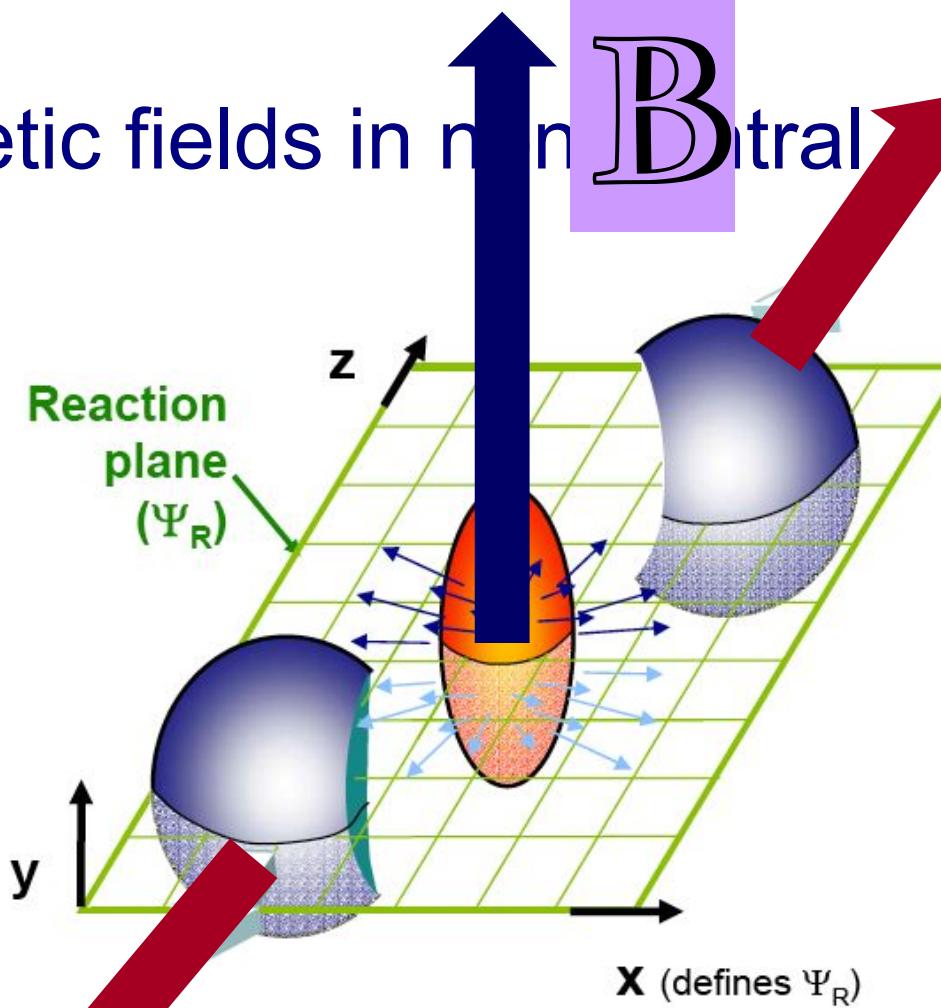
Thus we have
two very big
currents

The medium is filled by electrically charged particles

Large orbital momentum, perpendicular to the reaction plane

Large magnetic field along the direction of the orbital momentum

Magnetic fields in non-central collisions



Two very big currents produce a very
big magnetic field

The medium is filled by electrically charged particles

Large orbital momentum, perpendicular to the reaction plane

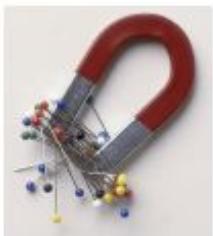
Large magnetic field along the direction of the orbital momentum

Comparison of magnetic fields

D.Kharzeev



The Earth's magnetic field 0.6 Gauss



A common, hand-held magnet
The strongest steady magnetic fields achieved so far in the laboratory 4.5×10^5 Gauss

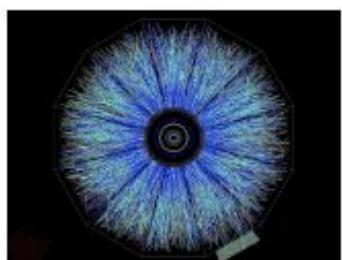
The strongest man-made fields ever achieved, if only briefly 10^7 Gauss



Typical surface, polar magnetic fields of radio pulsars 10^{13} Gauss

Surface field of Magnetars 10^{15} Gauss

<http://solomon.as.utexas.edu/~duncan/magnetar.html>



Off central Gold-Gold Collisions at 100 GeV per nucleon
 $eB(\tau=0.2 \text{ fm}) = 10^3 \sim 10^4 \text{ MeV}^2 \sim 10^{17} \text{ Gauss}$

Magnetic forces are of the order of strong interaction forces

first time in my life I see such effect

$$eB \approx \Lambda_{QCD}^2$$

Magnetic forces are of the order of strong interaction forces

first time in my life I see such effect

$$eB \approx \Lambda_{QCD}^2$$

We expect the influence of magnetic field on strong interaction physics

Magnetic forces are of the order of strong interaction forces

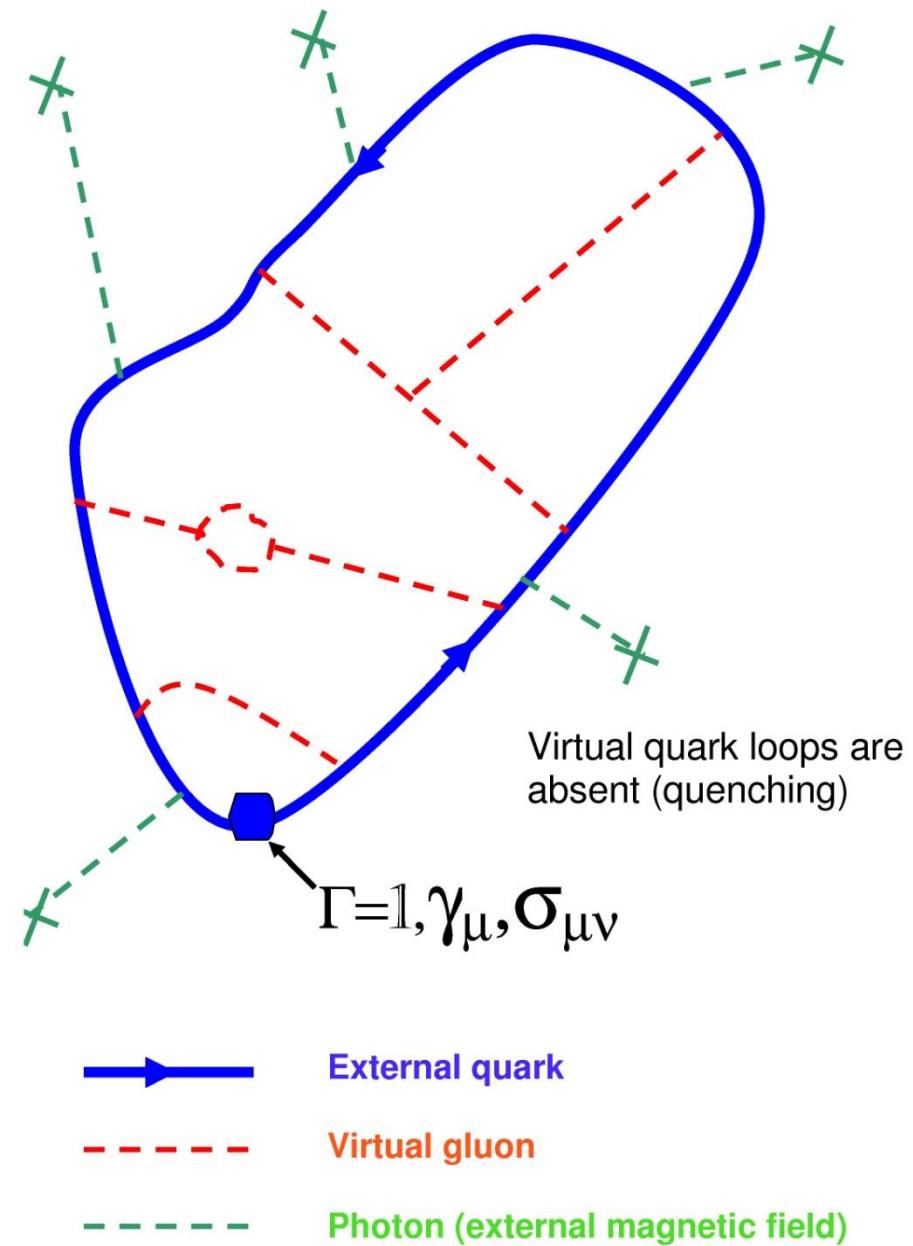
first time in my life I see such effect

$$eB \approx \Lambda_{QCD}^2$$

We expect the influence of magnetic field on
strong interaction physics

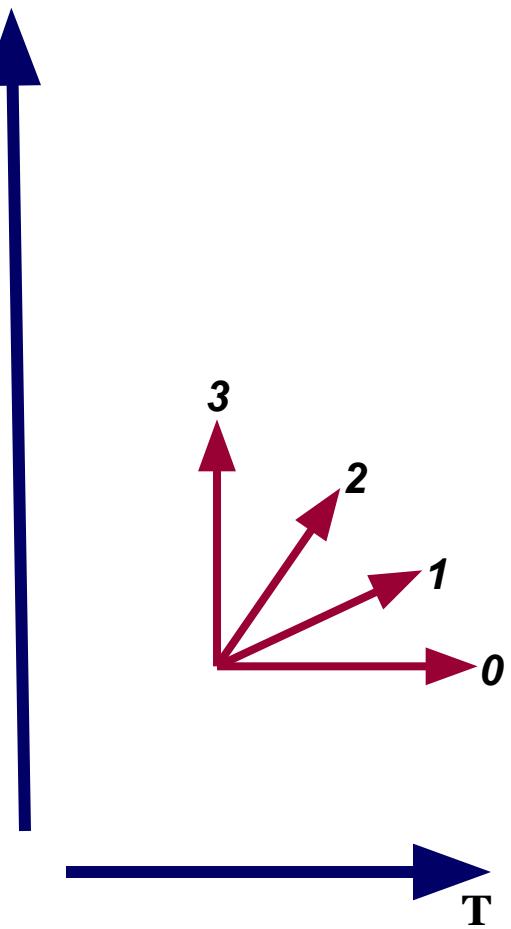
The effects are nonperturbative,
it is impossible to perform analytic calculations
and we use

Lattice Calculations



We calculate

in the external magnetic field and in the presence of the vacuum gluon fields



Quenched vacuum, overlap Dirac operator, external magnetic field

$$eB = \frac{2\pi qk}{L^2}; eB \geq 250 \text{ Mev}$$

Chiral Magnetic Effect

[Fukushima, Kharzeev, Warringa, McLerran '07-'08]

Electric current appears at regions

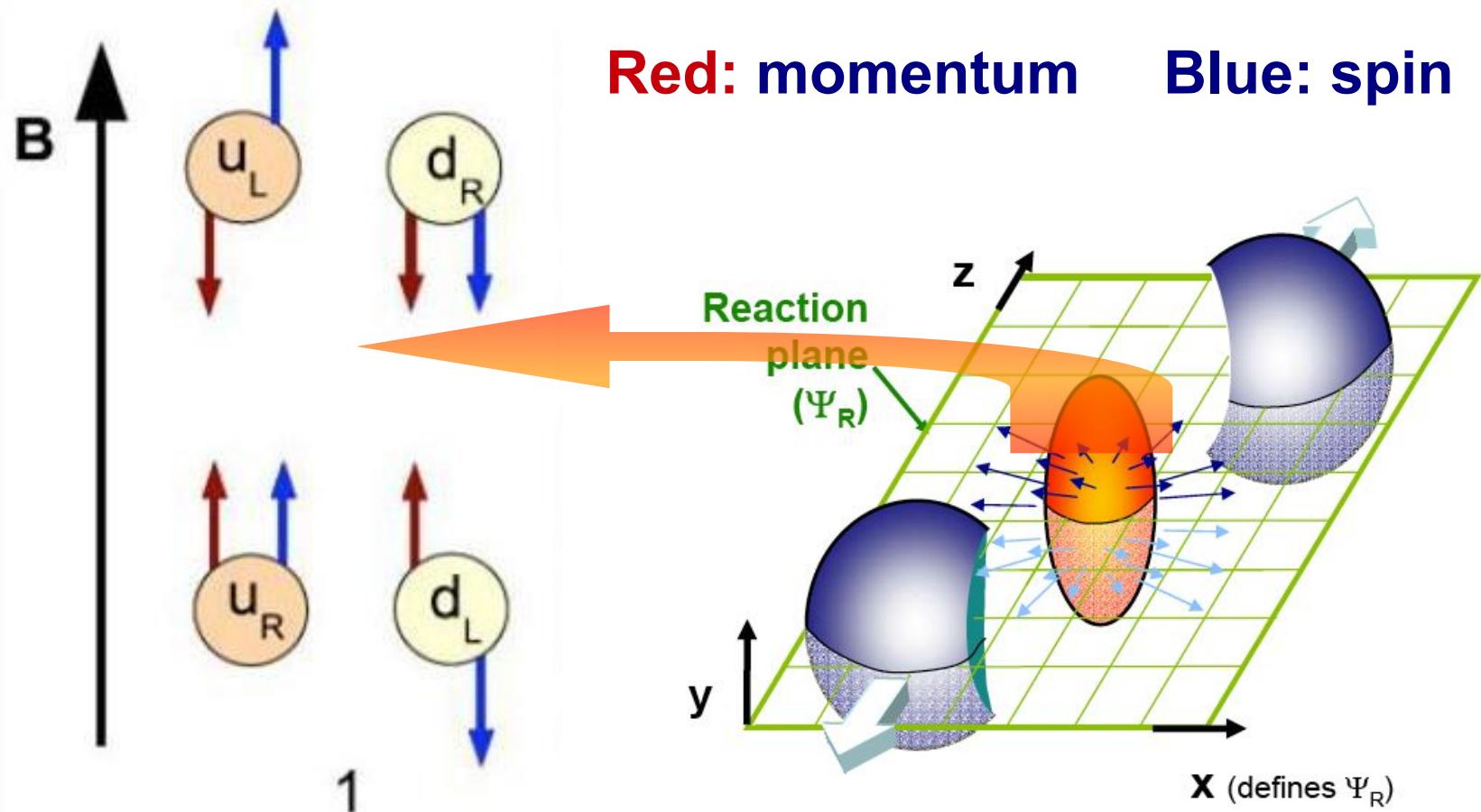
- 1. with non-zero topological charge density**
- 2. exposed to external magnetic field**

Experimentally observed at RHIC :

charge asymmetry of produced particles at heavy ion collisions

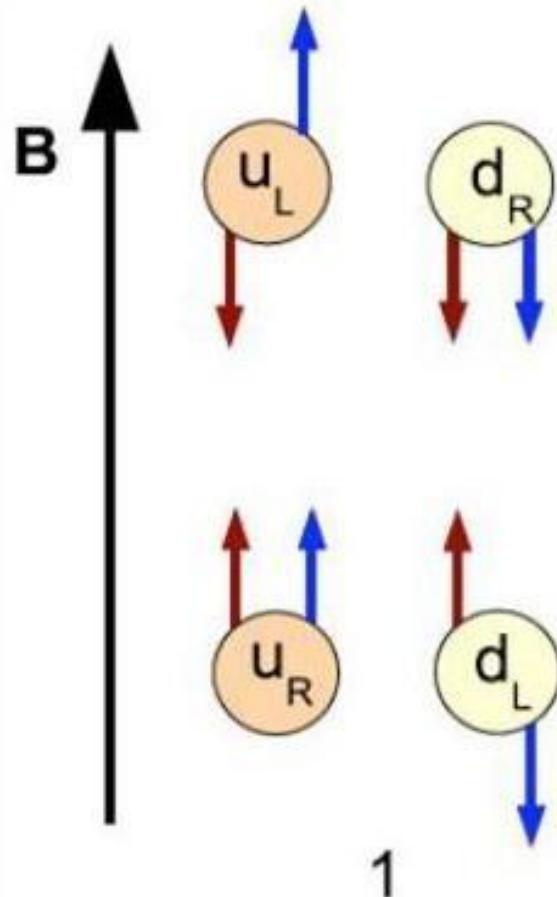
Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

1. Massless quarks in external magnetic field.



Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

1. Massless quarks in external magnetic field.



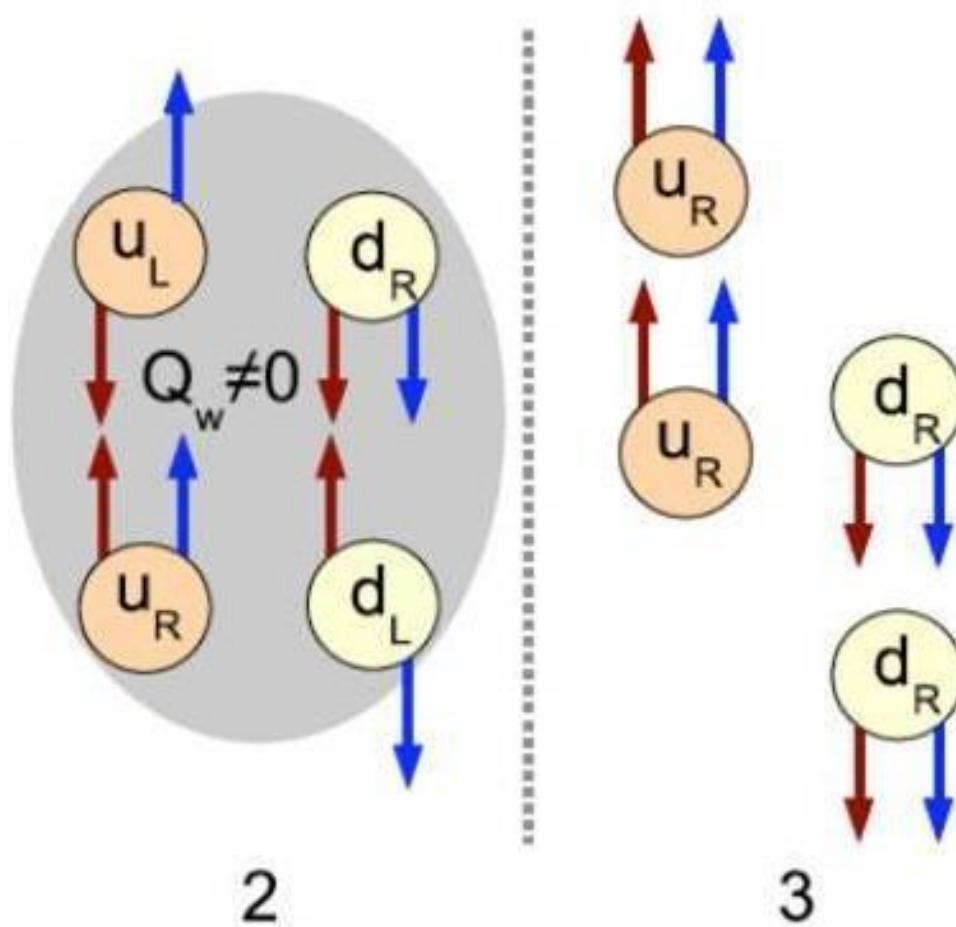
Red: momentum

Blue: spin



Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

2. Quarks in the instanton field.



Red: momentum
Blue: spin

Effect of topology:

$$u_L \rightarrow u_R$$

$$d_L \rightarrow d_R$$

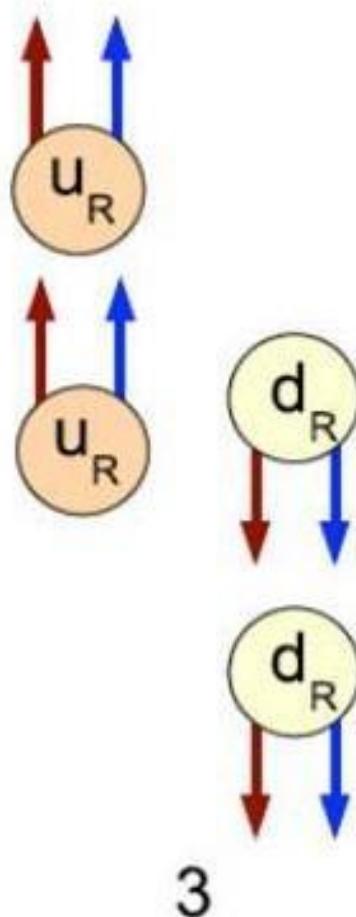
Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

3. Electric current along magnetic field

Red: momentum

Blue: spin

Effect of topology:



$$u_L \rightarrow u_R$$

$$d_L \rightarrow d_R$$

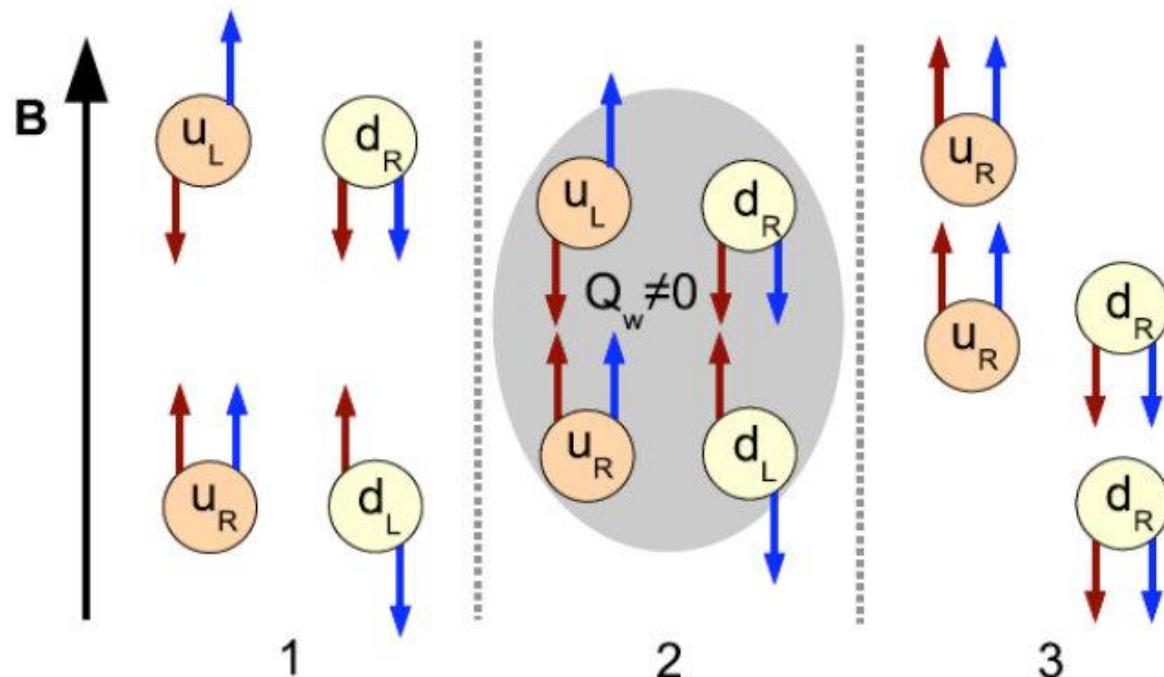
u-quark: $q=+2/3$

d-quark: $q= -$

$1/3$

Chiral Magnetic Effect by Fukushima, Kharzeev, Warringa, McLerran

**3. Electric current is along
magnetic field
In the *instanton* field**



Red: momentum
Blue: spin

Effect of topology:

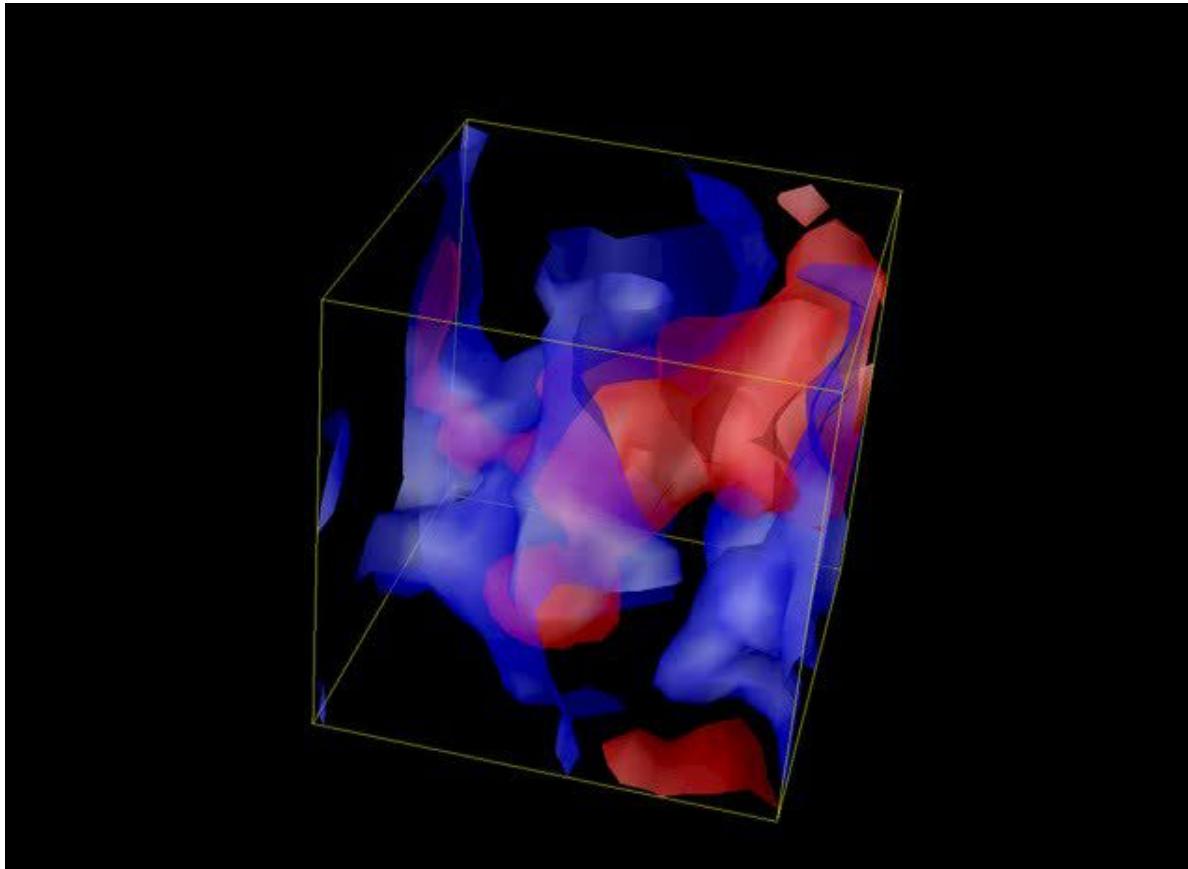
$$u_L \rightarrow u_R$$

$$d_L \rightarrow d_R$$

u-quark: $q=+2/3$

d-quark: $q= - 1/3$

Topological charge density in quantum QCD vacuum has fractal structure



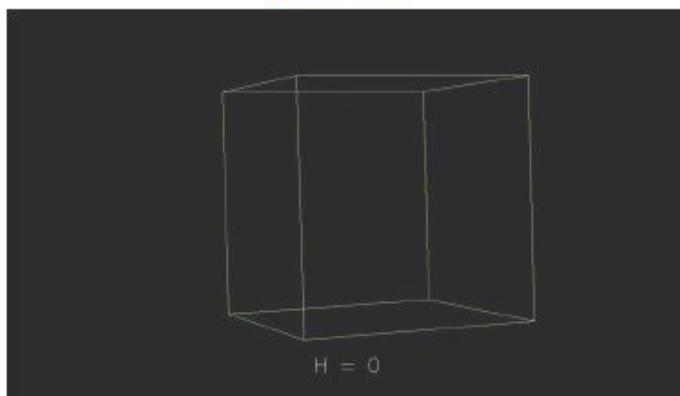
In quantum vacuum we expect big fluctuations of charge squared

$$\langle j_3 \rangle = 0; \quad \langle j_3^2 \rangle \neq 0;$$

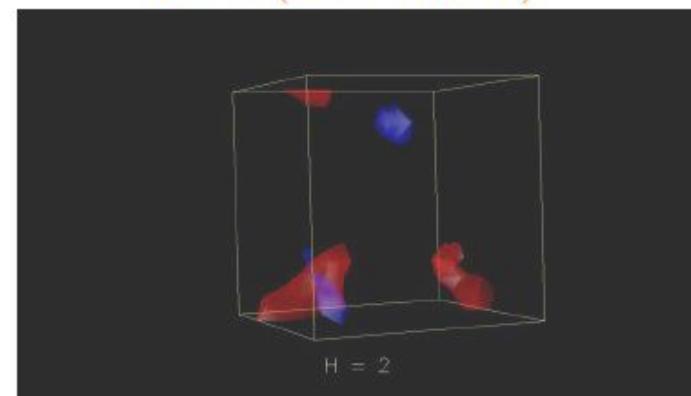
Chiral Magnetic Effect on the lattice, charge separation

Density of the electric charge vs. magnetic field

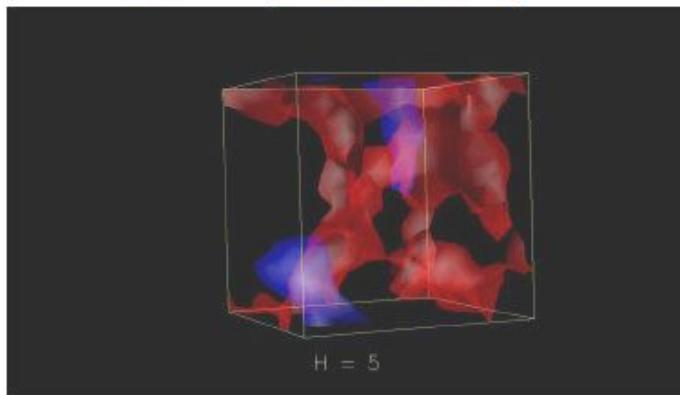
$$B = 0$$



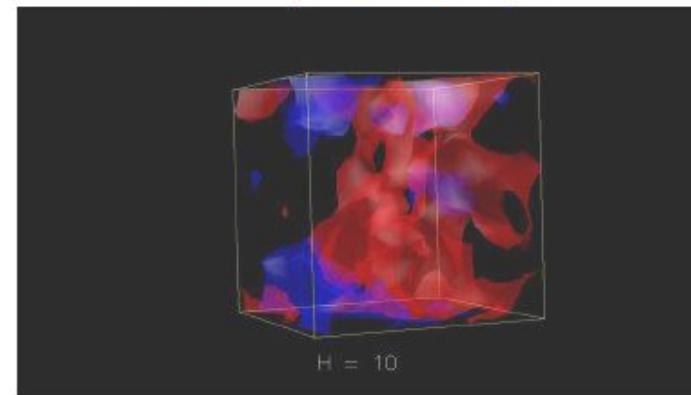
$$B = (500 \text{ MeV})^2$$



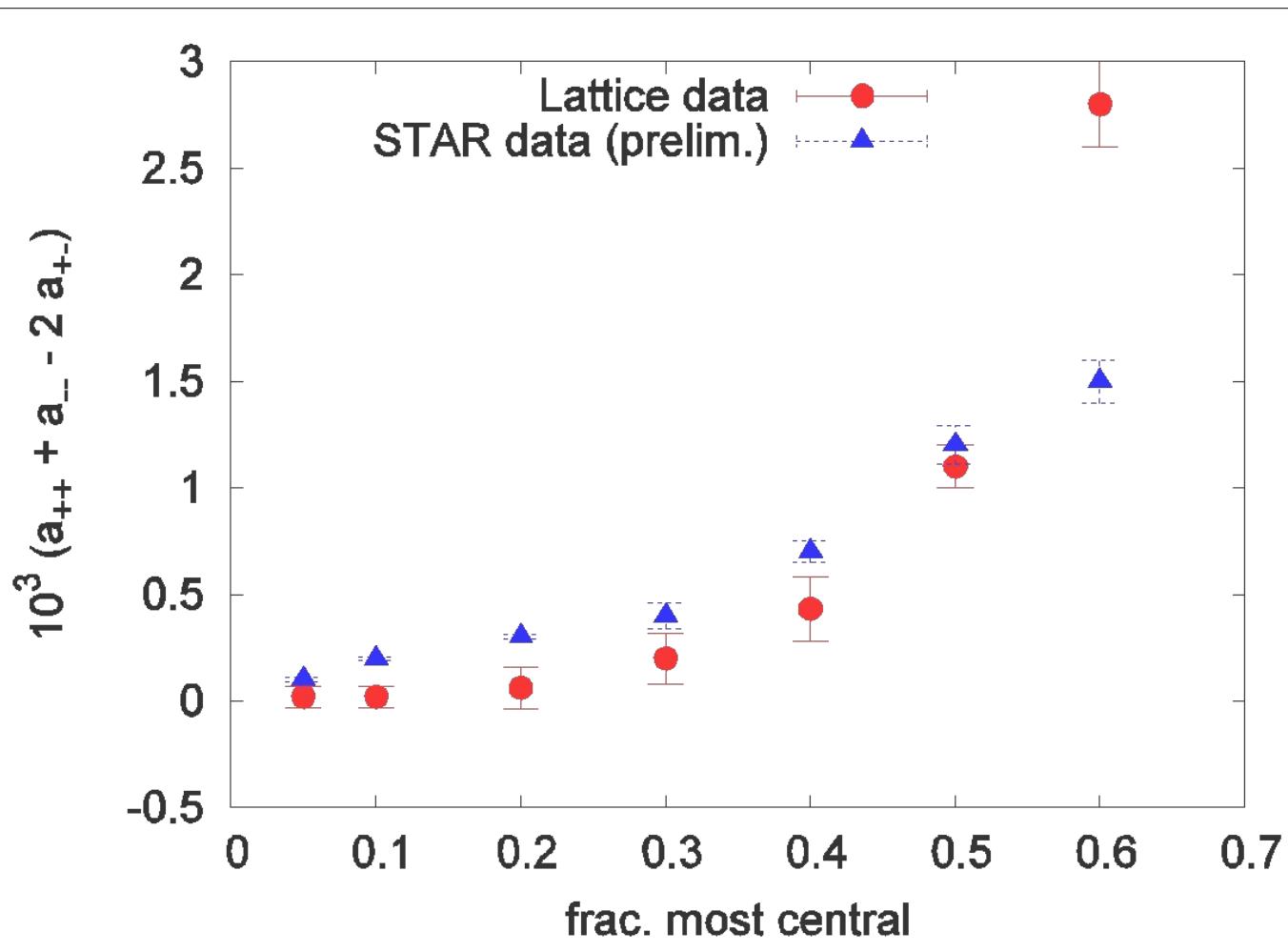
$$B = (780 \text{ MeV})^2$$



$$B = (1.1 \text{ GeV})^2$$



Chiral Magnetic Effect, EXPERIMENT VS LATTICE DATA (Au+Au)



Chiral Magnetic Effect, EXPERIMENT VS LATTICE DATA

$$a_{ab} = \frac{1}{N_e} \sum_{e=1}^{N_e} \frac{1}{N_a N_b} \sum_{i=1}^{N_a} \sum_{j=1}^{N_b} \cos(\phi_{ia} + \phi_{jb})$$

$$\frac{\langle (\Delta Q)^2 \rangle}{N_q^2} = a_{++} + a_{--} - 2a_{+-}$$

D. E. Kharzeev,
L. D. McLerran, and
H. J. Warringa,
Nucl. Phys. A 803,
227 (2008),

$$= \frac{4\pi\tau^2\rho^2R^2}{3N_q^2} \left(\langle j_\parallel^2 \rangle + 2\langle j_\perp^2 \rangle \right)$$

experiment

$R \approx 5 \text{ fm}$
 $\rho \approx 0.2 \text{ fm}$
 $\tau \approx 1 \text{ fm}$

our fit

our lattice data at $T=350 \text{ MeV}$

Preliminary results: conductivity of the vacuum

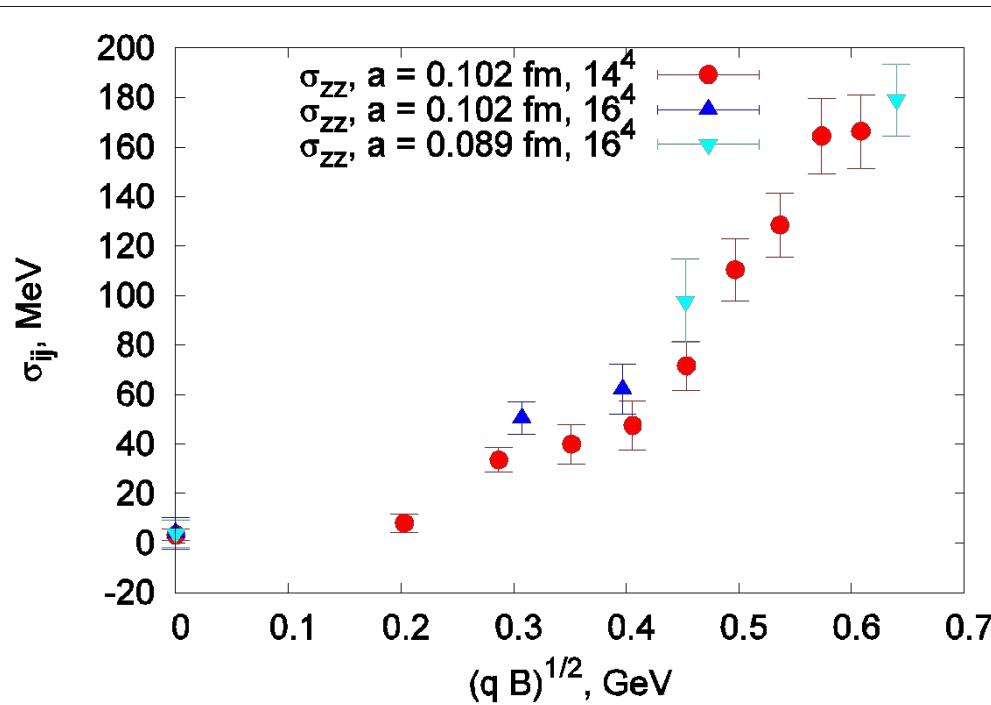
Qualitative definition of conductivity σ

$$\langle j_\mu(x) j_\nu(y) \rangle = C + A \cdot \exp\{-m|x - y|\}$$

$$\sigma \propto C$$

Preliminary results: conductivity of the vacuum

Conductivity at T=0

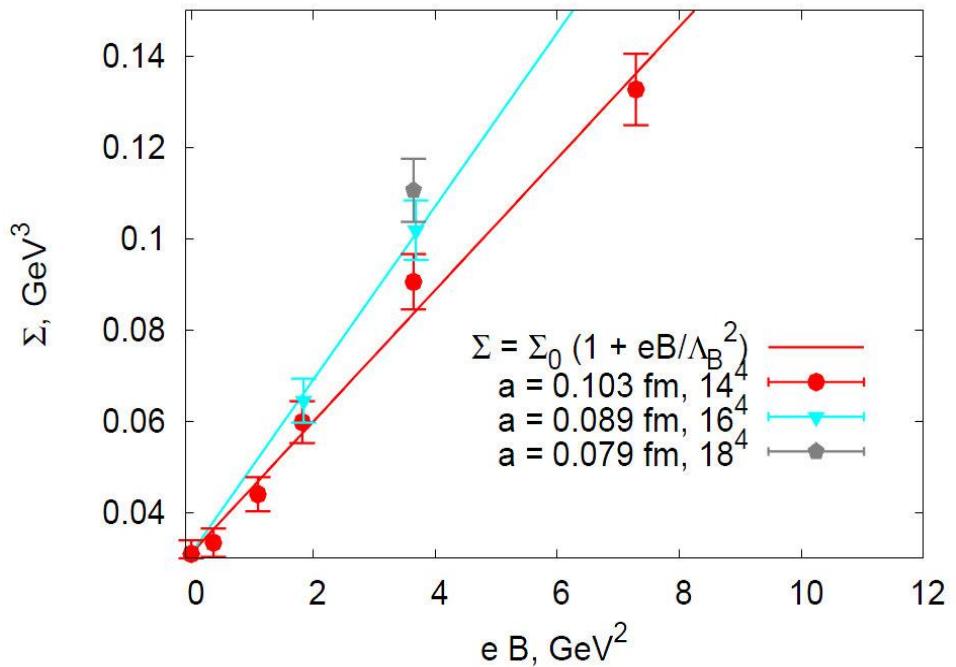


2. Chiral condensate in QCD

$$\Sigma = - \langle \bar{\psi} \psi \rangle$$

$$m_\pi^2 f_\pi^2 = m_q \langle \bar{\psi} \psi \rangle$$

Chiral condensate vs. field strength



$$\Sigma = \Sigma_0 \left(1 + \frac{eB}{\Lambda_B^2} \right)$$

- Our value for Λ_B :

$$\Lambda_B^{\text{fit}} = (1.41 \pm 0.14 \pm 0.20) \text{ GeV}$$

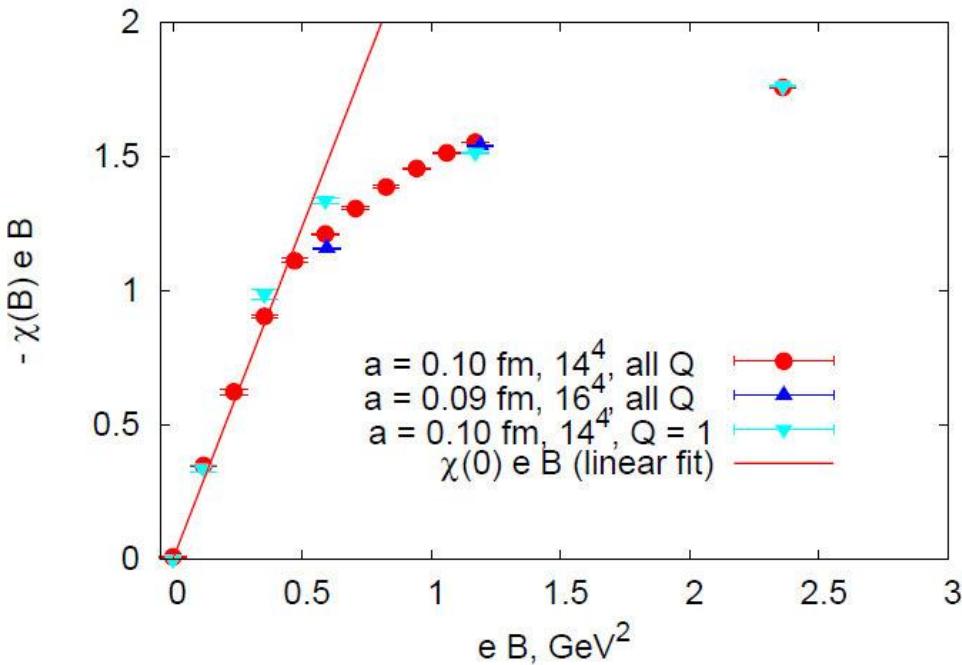
- χ PT result:

$$\begin{aligned} \Lambda_B^{\chi PT} &= 1.96 \text{ GeV} & (F_\pi = 130 \text{ MeV} - \text{real world}) \\ \Lambda_B^{\chi PT} &= 1.36 \text{ GeV} & (F_\pi = 90 \text{ MeV} - \text{quenched}) \end{aligned}$$

- Chiral condensate at $B = 0$: $\Sigma_0^{\text{fit}} = [(310 \pm 6) \text{ MeV}]^3$

We are in agreement with the chiral perturbation theory: the chiral condensate is a linear function of the strength of the magnetic field!

3. Magnetization of the vacuum as a function of the magnetic field



Spins of virtual quarks turn parallel to the magnetic field



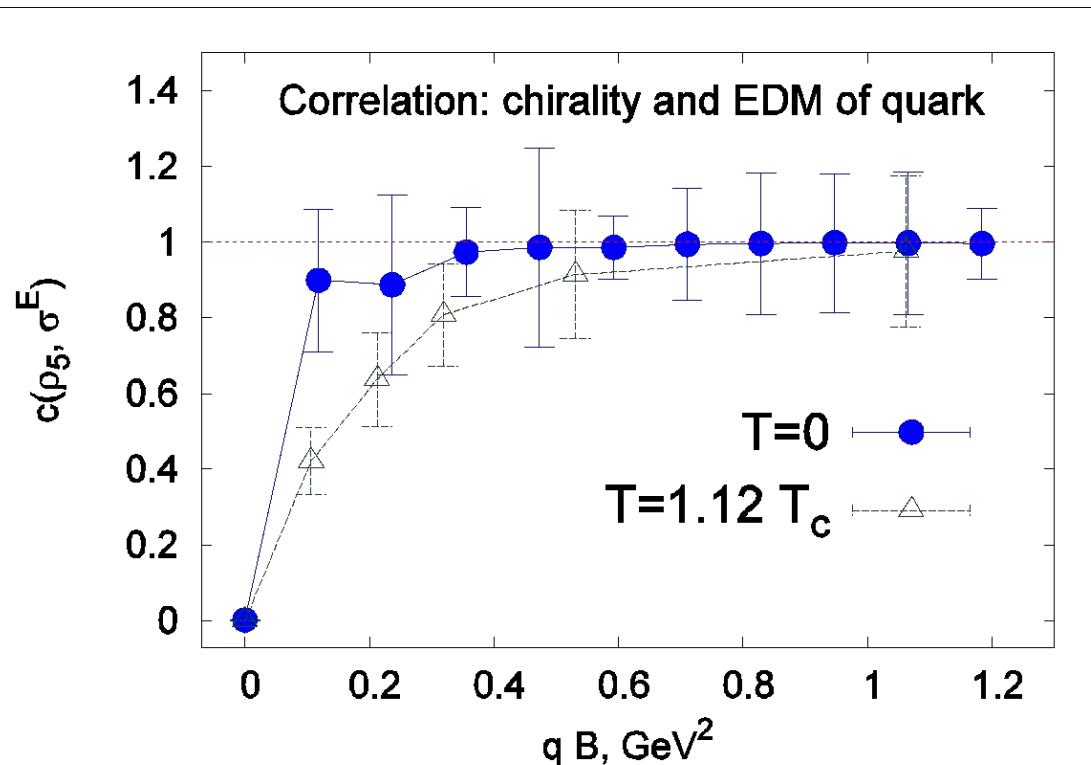
$$\langle \bar{\psi} \sigma_{\alpha\beta} \psi \rangle = \chi \langle \bar{\psi} \psi \rangle F_{\alpha\beta}$$

$$\sigma_{\alpha\beta} = \frac{1}{2i} [\gamma_\alpha, \gamma_\beta]$$

$\langle \bar{\psi} \psi \rangle \chi = -46(3) \text{ Mev} \leftrightarrow \text{our result}$
 $\langle \bar{\psi} \psi \rangle \chi \approx -50 \text{ Mev} \leftrightarrow \text{QCD sum rules}$
 (I.I. Balitsky, 1985, P. Ball, 2003.)

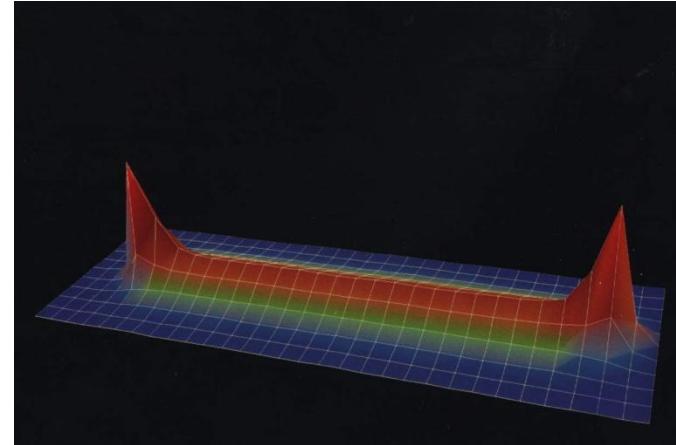
4. Generation of the anomalous quark electric dipole moment along the axis of magnetic field

yLarge correlation between square of the electric dipole moment
 $\rho_5 = \bar{\psi} \gamma_5 \psi$
 $\sigma_{0i} = i \bar{\psi} [\gamma_0, \gamma_i] \psi$ **and chirality**



THEORY

To explain



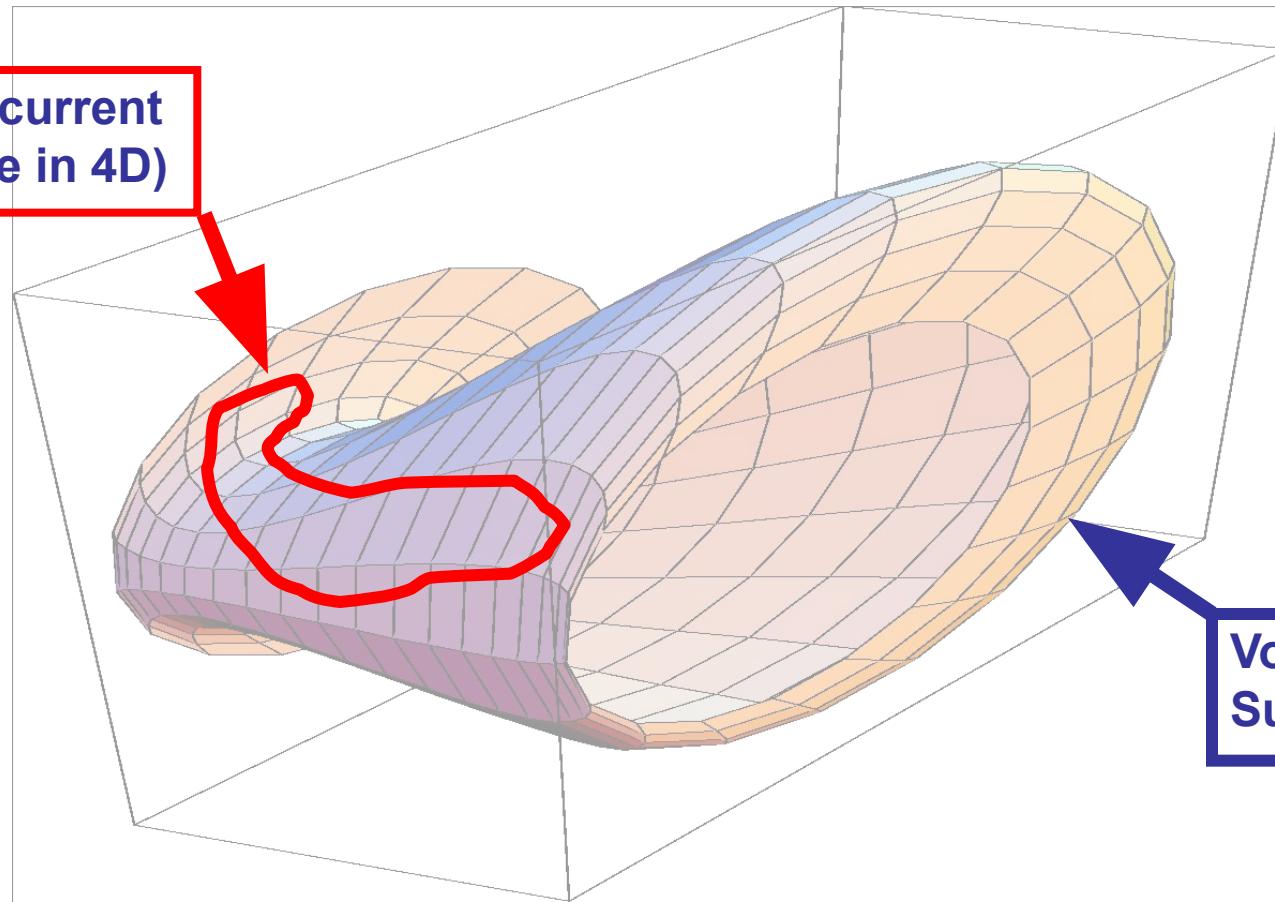
We have to prove in gluodynamics that

$$\langle W(C) \rangle = \langle \text{Tr } P \exp \left\{ \oint_C i A_\mu dx_\mu \right\} \rangle \propto \exp \{-\sigma \cdot \text{Area}\}$$

SU(2) gauge theory

J.Ambjorn, J.Giedt and J.Greensite, JHEP 0002 (2000) 033. A.V.Kovalenko, M.I.Polikarpov, S.N.Syritsyn and V.I.Zakharov, Phys. Rev. D71 (2005) 054511; Phys. Lett. B613 (2005) 52; Ph. de Forcrand and M. Pepe, Nucl. Phys. B598 (2001) 557.

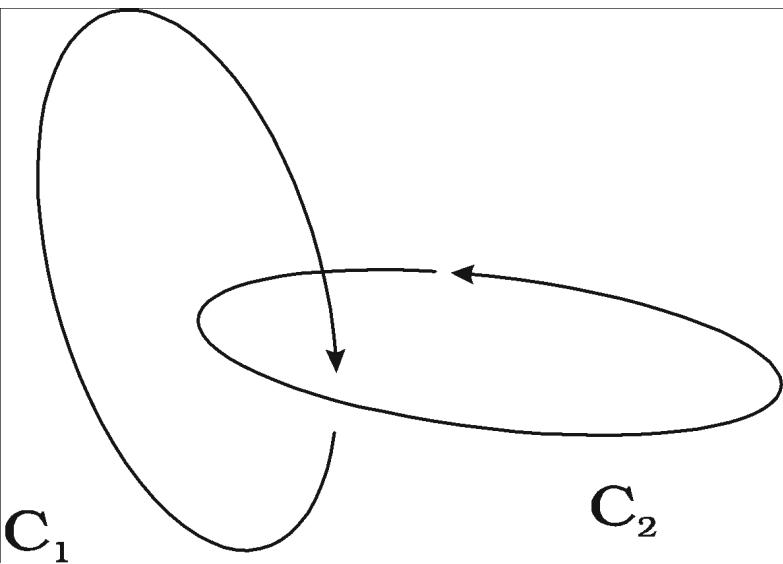
Monopole current
(closed line in 4D)



Vortex (closed
Surface in 4D)

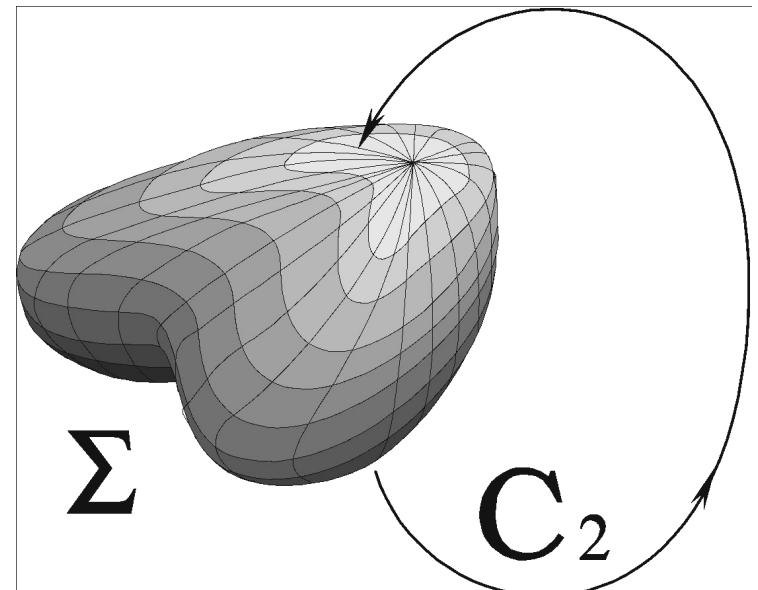
Linking number

3D



4D

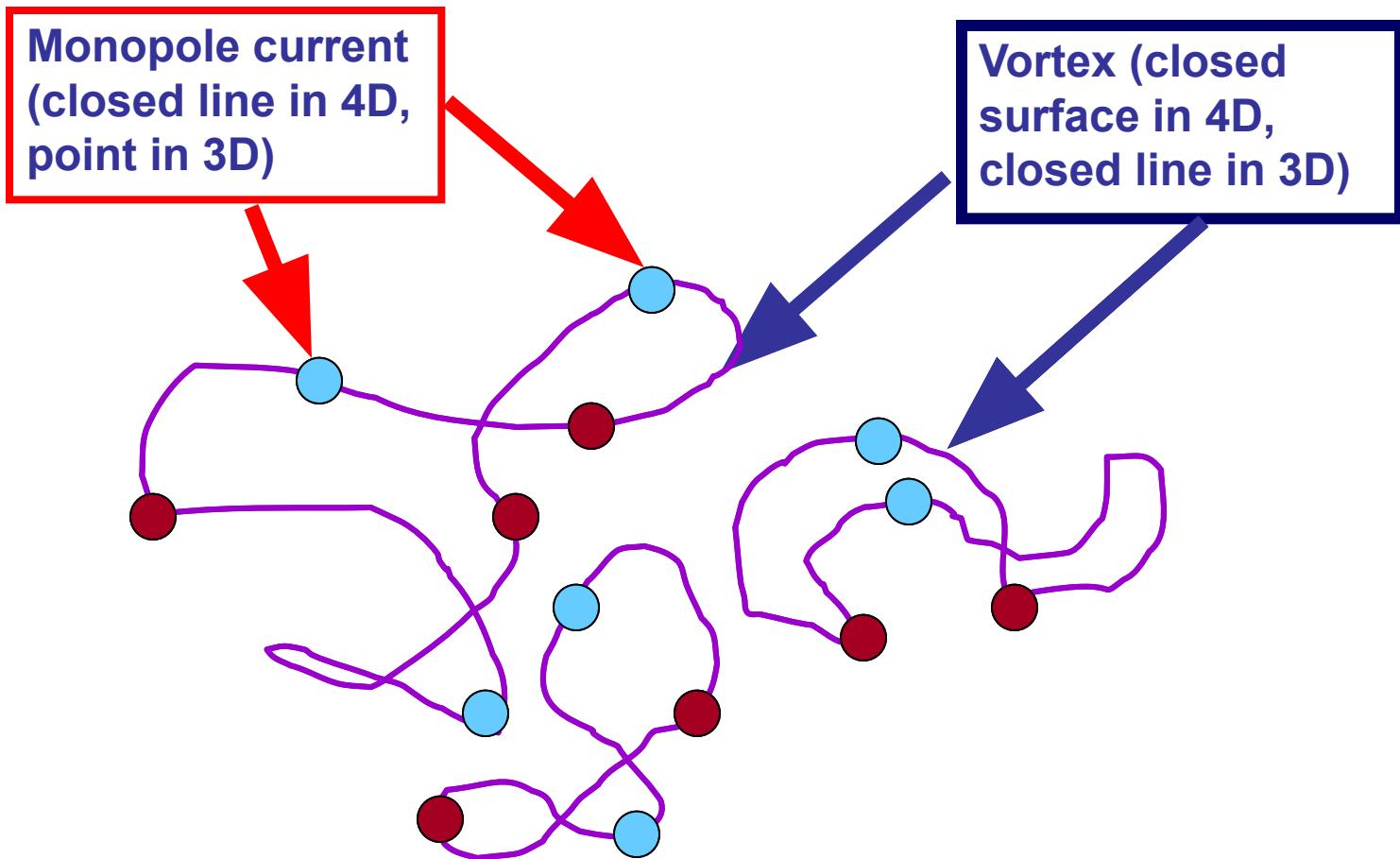
$$L = \frac{1}{8\pi^2} \int_{C_1} d\Sigma_{\alpha\beta}(x) \int_{C_2} dy_\gamma \epsilon_{\alpha\beta\gamma\delta} \partial_\delta \frac{1}{|x-y|}$$



$$L = \frac{1}{4\pi} \int_{C_1} dx_i \int_{C_2} dy_k \epsilon_{ikl} \partial_l \frac{1}{|x-y|}$$

Pure gauge theory

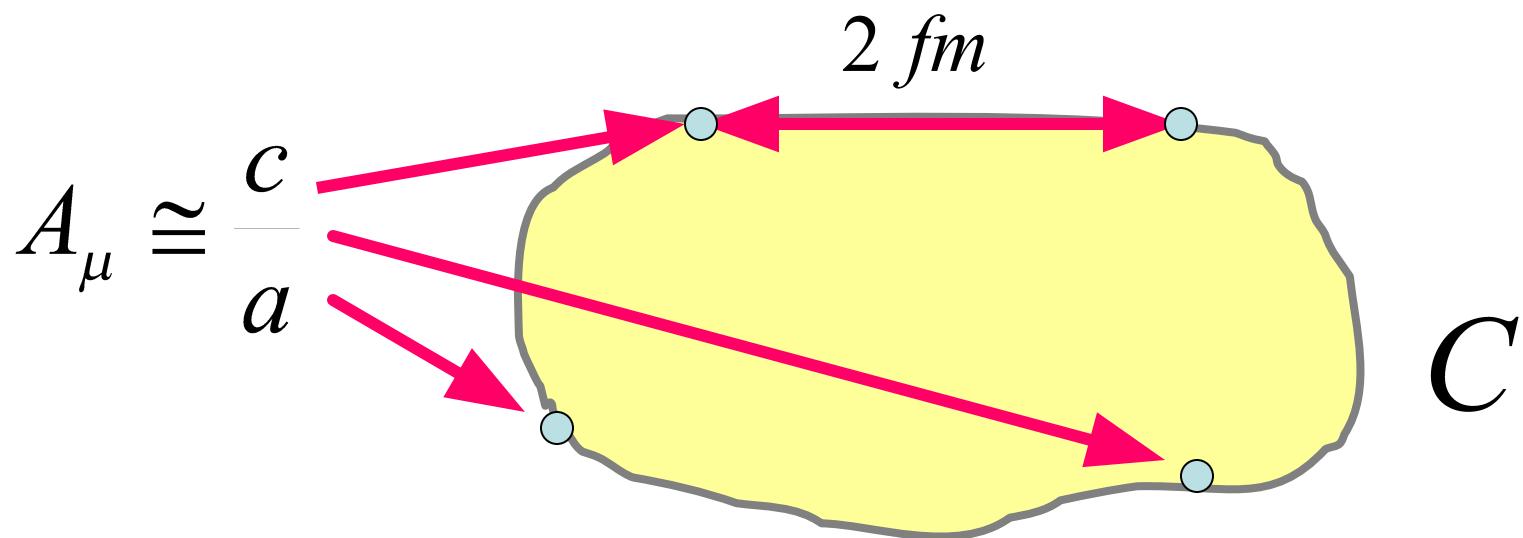
(what we see on 3d slice of 4D lattice)



THEORY

All information about confinement, quark condensate and any Wilson loop is encoded in 3d branes

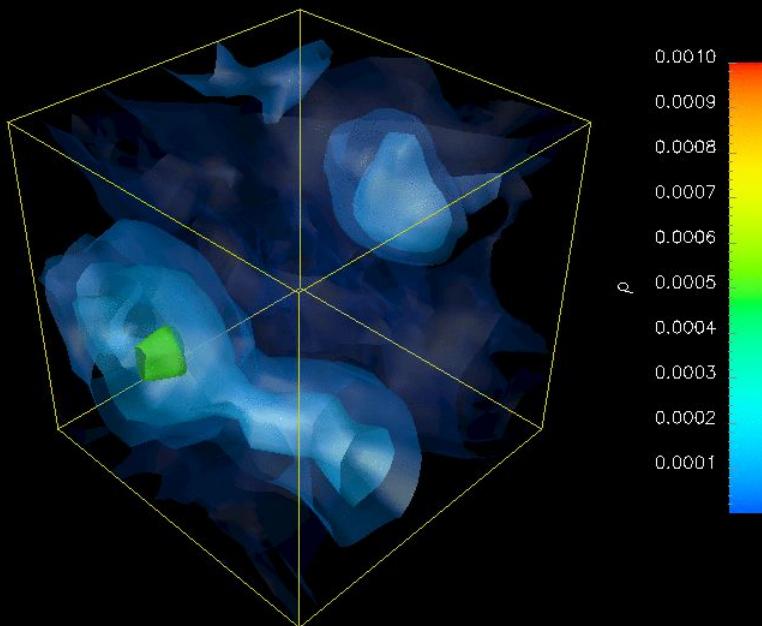
Holography



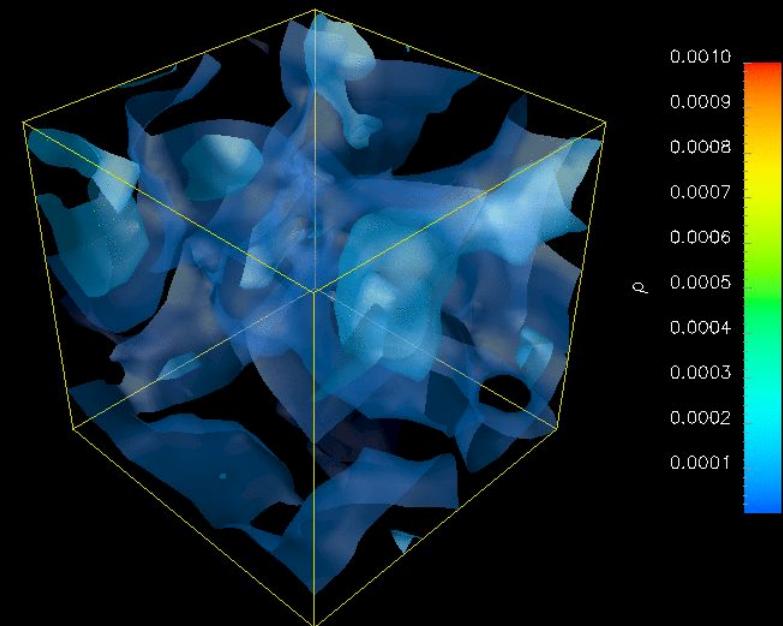
THEORY

Chiral symmetry breaking and topological susceptibility
is due to low-dimensional regions

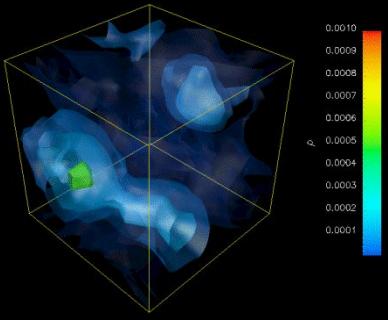
Time slices for ρ^2 , $\rho_\lambda(x) = \psi_\lambda^+(x)\psi_\lambda^-(x)$



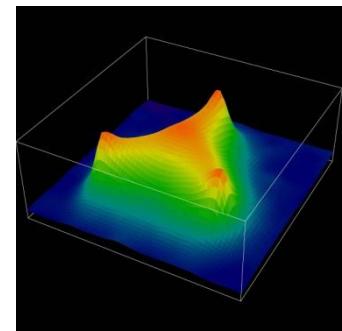
IPR=5.13
chirality=-1



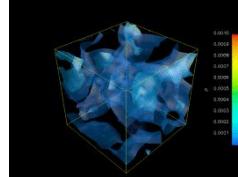
IPR=1.45
chirality=0



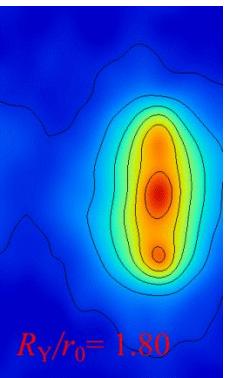
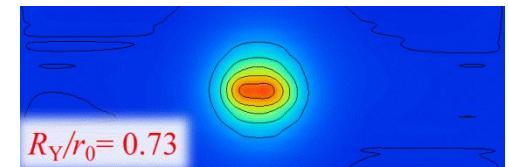
Instead of Conclusions



Computer simulations a) reproduce well known hadron properties b) predict new phenomena c) help to create new theoretical ideas.

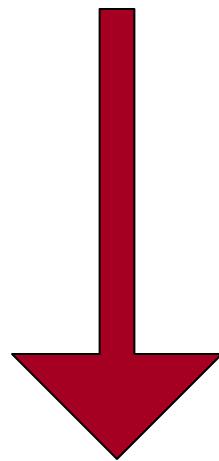


- Low dimensional objects (regions) are responsible for most interesting nonperturbative effects: chiral symmetry breaking, topological susceptibility and confinement.



- The era of traditional quantum field theory (Feynman graphs, perturbation theory) is over, nonperturbative field theory is close in spirit to solid state theory; we have to study dislocations, fractals, phase transitions etc.

<http://www.lattice.itep.ru>



Education

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всемирно
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теоретик **Валентин
Иванович Захаров**



Наш студент это тот, кому
интересна теоретическая
физика и/или
информатика и/или
математическая физика
и/или суперкомьютеры
(или все вместе).