## Sample Solutions

Central Europe Regional Contest 2007

## B: Billboard



## Billboard - Problem



- Test all existing subsets
- $2^{256}$ possibilities for the $16 \times 16$ board - 8


## Billboard - Main Idea



- What if we somehow knew the tapped tiles in the first row?


## Billboard - Main Idea



- We can try what happens with the row
- WOW! It is easy to find the second one!


## Billboard - Main Idea



- We can try what happens with the row
- WOW! It is easy to find the second one!


## Billboard - Main Idea



- Let's also do it...
- The third row becomes evident
- ... and so on


## Billboard - Solution

- Ok, but how to find the first row?
- We will try all possibilities!
- Approx. $2^{16}$ * $16^{2}$


## C: Phone Cell



## Cell - Problem

- Find a circle that covers most points
- Center may not be in an existing point $\square \square$ Solution will always touch 2 points



## Cell - Simple Solution

- Take all pairs, find a circle
- Then all other points must be tested
- $\square$ Time: $\mathrm{n}^{3}$



## Cell -Solution

" For each point, use "sweep" technique - Find „interesting angles" and sort them


## Cell -Solution

- One sorting for each point
$\square$ Time: $n^{2} . \log n$
- Carefully with floating point numbers!


## H: Hexagon



## Hexagon - Idea

- All combinations of 2 green points



## Hexagon - Solution

- Handle "special" cases


## Hexagon -Solution II

- Dynamic Programming
- For all area subsets (16), find the best solution using each parcel


## K: Keys



## Keys - Idea

- Breadth-First search
- Combination of position and keys (!)
- 4 keys => 16 combinations


## Keys - Idea

- Position (1,7) + Red Key
$\square(1,8)+$ Red/Yellow
$\square(1,6)+$



## Logic

## 



NORO-


## Logic - Problem

- Problem? There is no problem
- "Only" follow the connections
- Compute logical operations


## Logic - Potential Pitfalls

## - Gates with no input

- AND $\square 1$
- OR $\quad 0$
- XOR $\square 0$


## Logic - Potential Pitfalls

## - Splitting and joining paths

- => We must remember, what has already been computed



## N: Numbers

$10101010100101_{-2}=-10907$

## Numbers - Solution

- TO decimal:
- Use the formula in the problem statement

$$
4257_{-10}=-4000+200-50+7=-3843
$$

## Numbers - Solution

- FROM decimal:
- Use remainders (modulo)
- Careful with the negative numbers!
- $4237 \bmod 10=7 \quad \rightarrow 423$
- $-423 \bmod 10=7 \quad->-43$
- $43 \bmod 10=3 \quad \rightarrow 4$
- $-4 \bmod 10=6 \quad->-1$
- $1 \bmod 10=1$

$$
\text { -> } 16377
$$

## P: Polygon



## Polygon - Problem

- Find the order of polygon vertices





## Polygon - Idea

- Sort the vertices by their X coordinate


6


## Polygon - Idea

r => Find their horizontal neighbor


## Polygon - Idea

- Sort by Y => vertical neighbor



## Polygon - Solution

- Now, each vertex knows its neighbors
- Start with the first, and walk around



## Polygon - Solution

- Count Left / Right turns
" Left > Right? => counter-clockwise
L?



## R: Roshambo



## S: Robotic Sort



## Sort - Problem

- Naive approach - reverse in an array
- Little bit better: remember reversed - Quadratic time $\square 100000^{2} \because$



## Sort - Another Approach

- Double-linked list
- Problem finding the „forward direction"



## Sort - Solution

- Combined solution: use both
- Linked list + array of reversed
- The array time: O(rev_before)
- After SQRT(n) steps: reorder
- $\square$ n.SQRT(n) time


## Sort - Solution II

- Other possibilities - ???
- Heap
- Interval Trees
-...?


## W: Water



## Water - Problem

- Find the Center of Mass
- Amount of water with the lowest center



## Water - Idea

- Split the glass into horizontal slices - Volume of one slice: $\pi . r^{2} . d$



## Water - Solution

- Center of Mass of the glass
- Weighted average of all slices



## Water - Solution

- Add the water "slowly"
- Center of water mass



## Water - Solution

- Combine both centers (weighted average)



## Water - Solution

- Water reached the center ? => END!
- (Linear time needed only)



## Statistics

|  | RT | TL | WA | PE | AC |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Billboard | 1 | 11 | 8 | 1 | 22 |
| Cell | 5 | 17 | 17 | 1 | 12 |
| Hexagon | 4 | 7 | 13 | 0 | 4 |
| Keys | 1 | 10 | 14 | 3 | 42 |
| Logic | 1 | 1 | 31 | 0 | 4 |
| Numbers | 11 | 5 | 65 | 0 | 46 |
| Polygon | 6 | 11 | 24 | 0 | 37 |
| Roshambo | 6 | 1 | 10 | 16 | 66 |
| Sort | 3 | 24 | 0 | 0 | 1 |
| Water | 1 | 2 | 1 | 0 | 1 |

