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Vladislav Khvostov



**Part #1: Independent and parallel visual
processing of ensemble statistics: Evidence from
dual tasks**

**Part #2: Confidence intervals in within-subject
designs**

Part #1



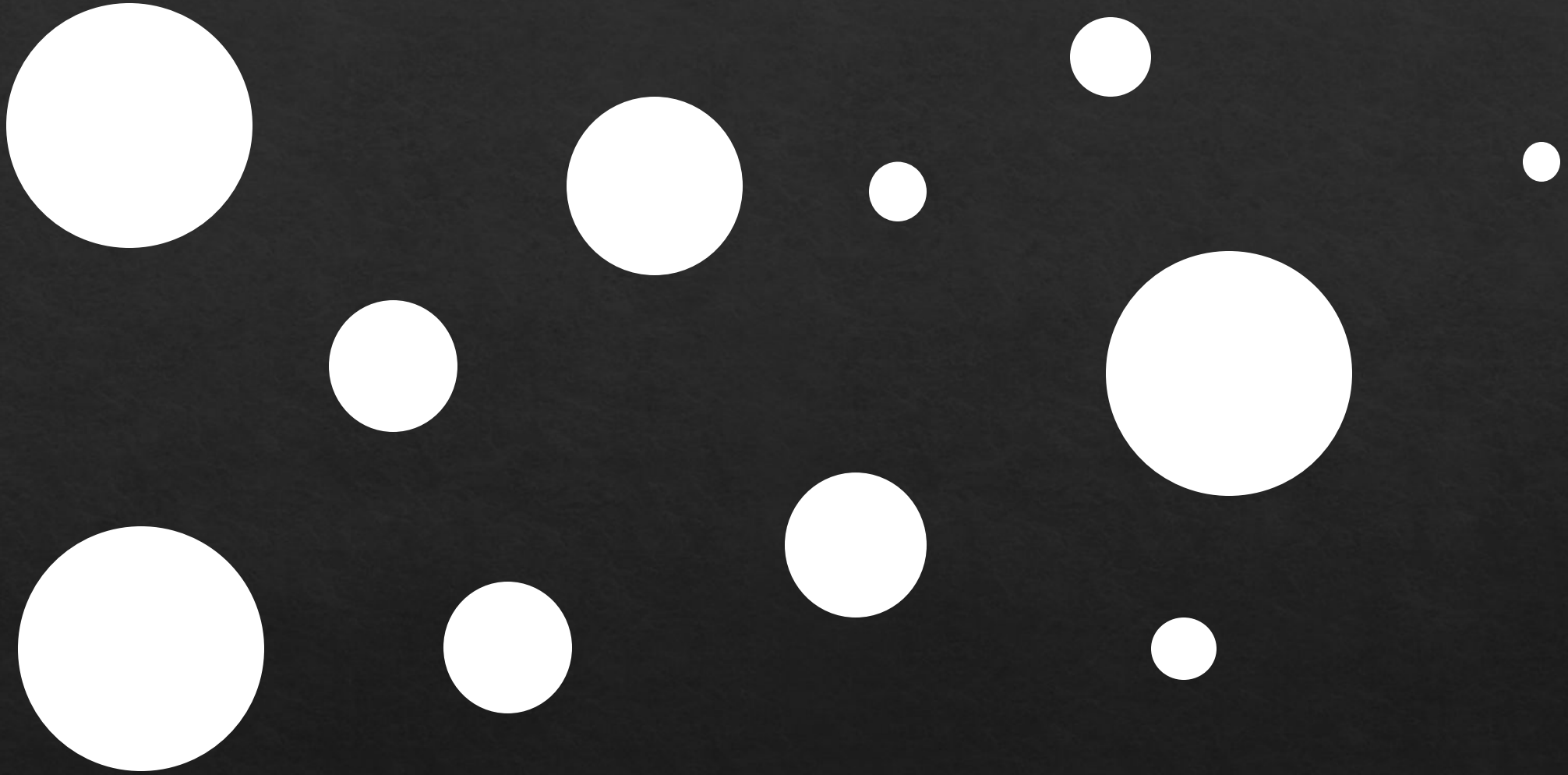
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Independent and parallel visual processing of ensemble statistics: Evidence from dual tasks

spoiler

Vladislav Khvostov
and Igor Utochkin

An example



Greater or smaller than average?



Ensemble summary statistics

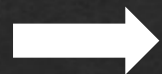
- ◆ The visual system can compute mean (Alvarez & Oliva, 2009), numerosity (Halberda, Sires, & Feigenson, 2006), variance/range (Dakin & Watt, 1997)
- ◆ Ensemble statistics can be calculated for low-level features:
 - color (Gardelle & Summerfield, 2011),
 - orientation (Parkes, Lund, Angelucci, Solomon, & Morgan, 2001),
 - size (Ariely, 2001),and for high-level features:
 - emotions, gender, etc. (Sweeny & Whitney, 2014, Haberman & Whitney, 2007, 2009).

Independent mechanisms

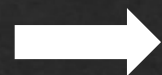
e

Independent mechanisms

INPUT



MEAN



NUMEROSITY



RANGE

One mechanism

INPUT



«GENERAL
ENSEMBLE
PROCESSOR»
Mean, Numerosity,
Range

Correlational approach

Independence

Independent mechanisms



MEAN



NUMEROSITY



RANGE

Prediction

Different
sources of
noise



No correlation
between errors in reports
of different statistics

One mechanism



«GENERAL
ENSEMBLE
PROCESSOR»
Mean, Numerosity,
Range

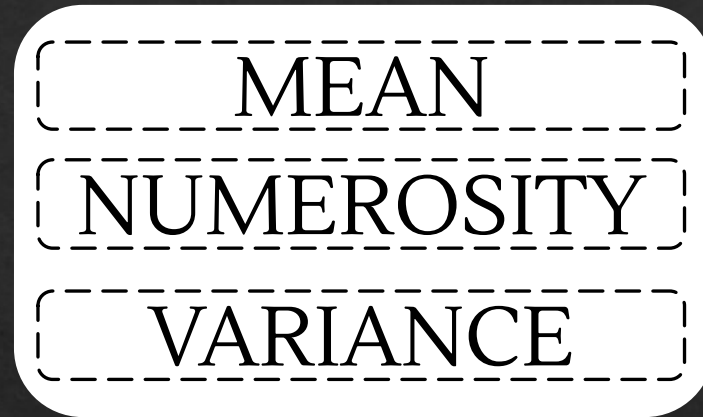
One source
of noise



Correlation
between errors in reports
of different statistics

Parallelism

Parallel
access
(no
interference)

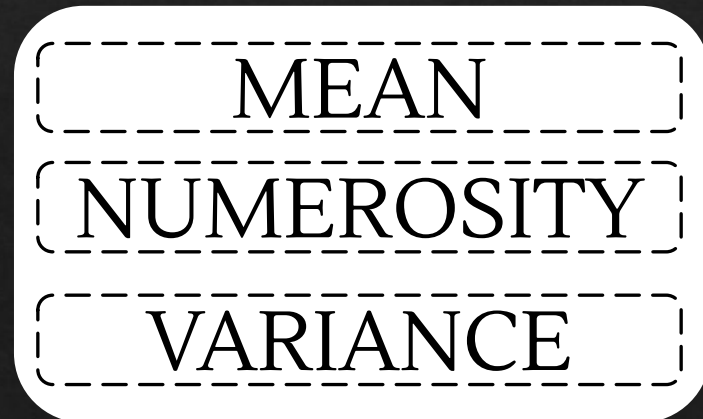


REPORT

REPORT

REPORT

Non-parallel
access
(interference)

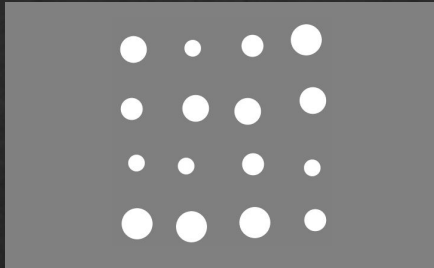


REPORT

Parallelism test

Single task

“Calculate MEAN”

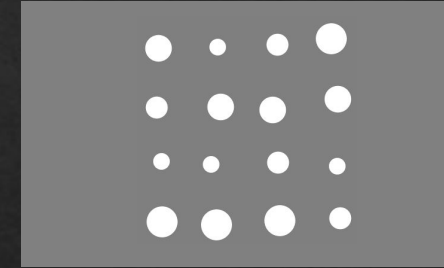


MEAN report

Observers should compute
only one statistics

Dual task

“Calculate MEAN and RANGE”



MEAN report



RANGE report

Observers should compute
both statistics

Parallelism test

Access

Prediction

Parallel access



No interference

Error in single task = Error in dual task

Non-parallel access



Interference

Error in single task < Error in dual task

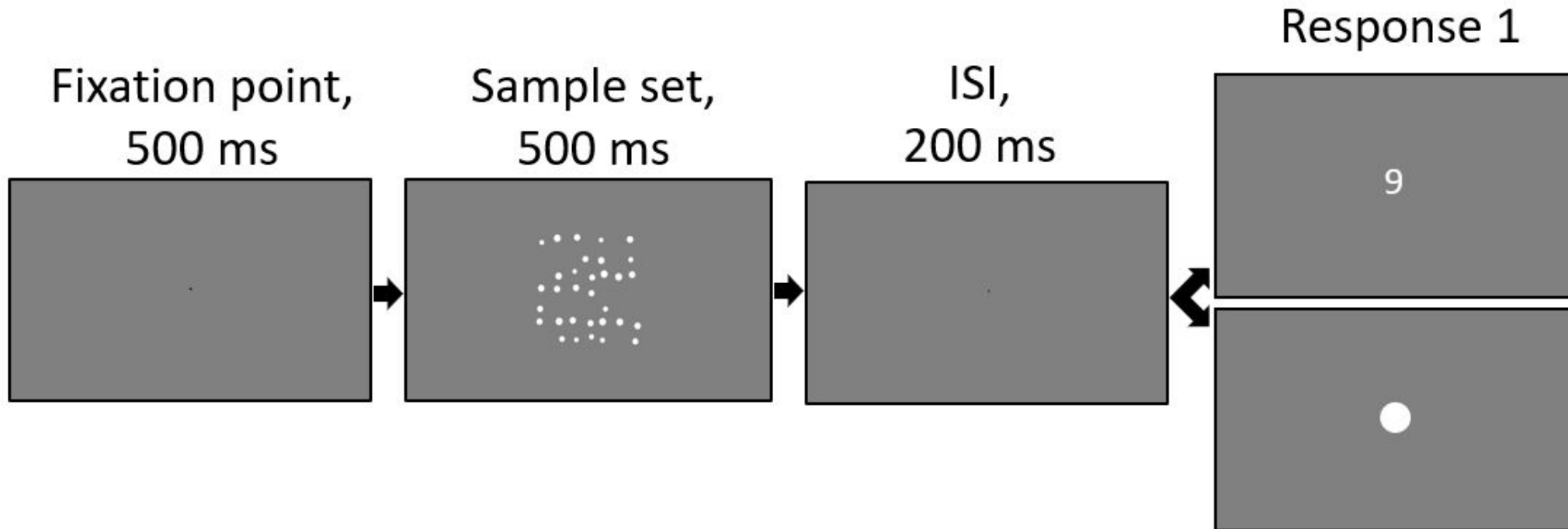
Experiment 1

Whether mean and numerosity can be calculated independently and in parallel?

N=23

Procedure

Baseline condition
2 blocks (MEAN + NUMEROSITY)



| 3 blocks | Design 6 “variables” | |
|-------------|--|--|
| MEAN | MEAN baseline | |
| NIMEROSITY | NIMEROSITY baseline | |
| BOTH | MEAN reported first NIMEROSITY reported first | MEAN reported second NIMEROSITY reported 1 |

Data analysis

$$\text{Error} = \left| \frac{\text{observer's response} - \text{correct response}}{\text{correct response}} \right|$$

(1) Correlation between mean errors of 6 variables (across observers)

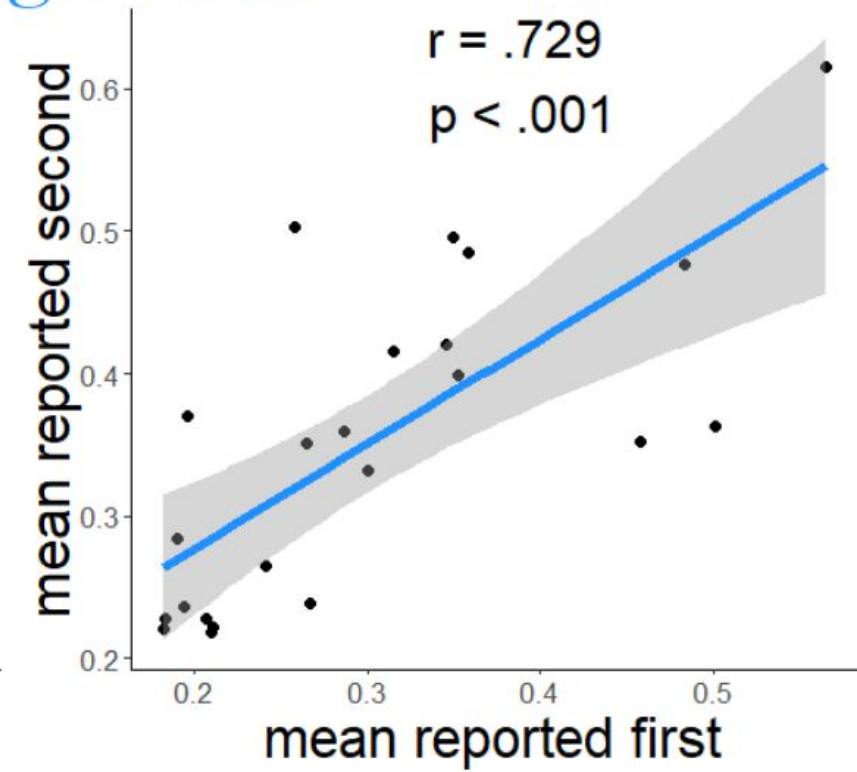
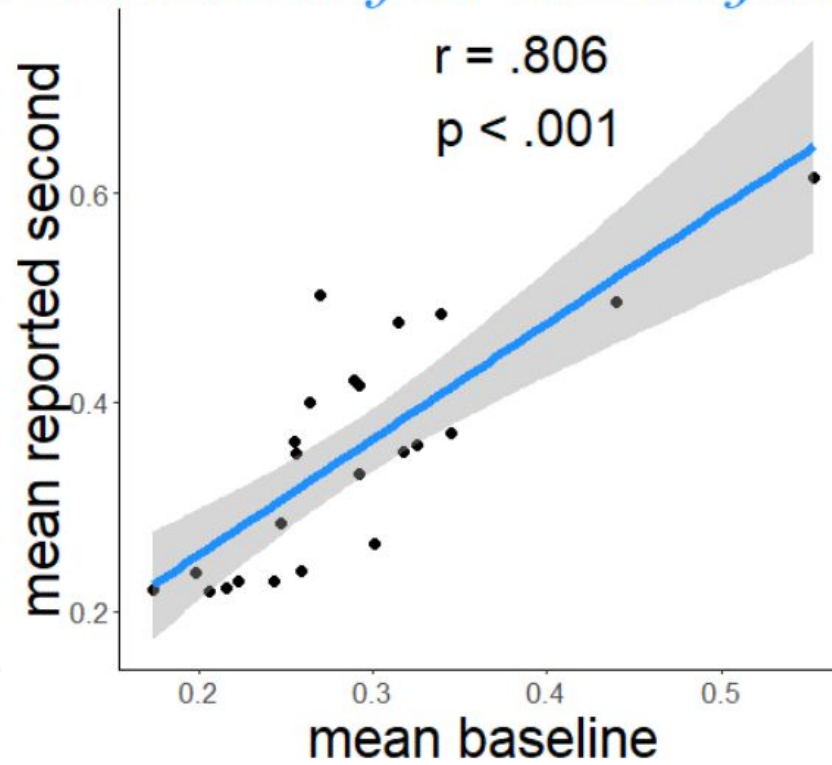
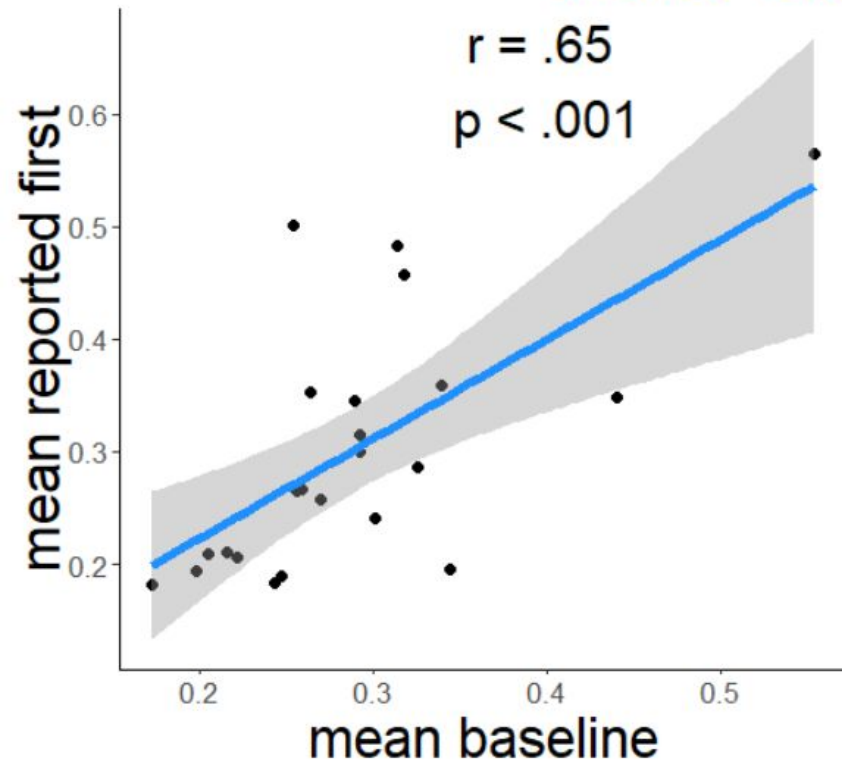
(2) Trial-by-trial correlation between an error in the mean judgment and an error in the numerosity judgment (separately for each participant)

(3) Comparison of mean errors in baseline and both conditions

Independence

Parallelism

Auto-correlations for Mean judgements

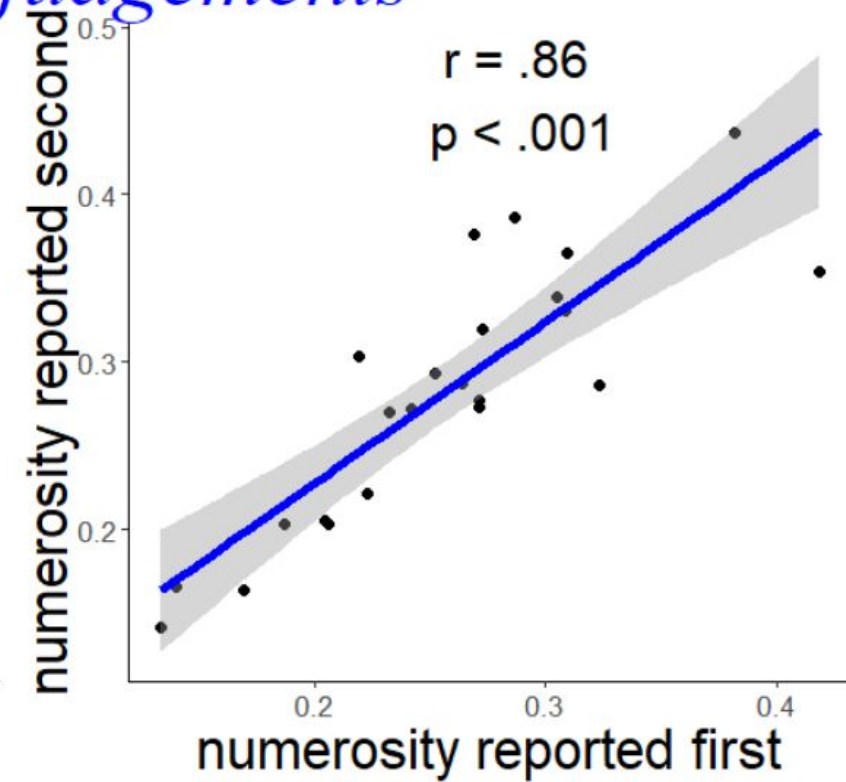
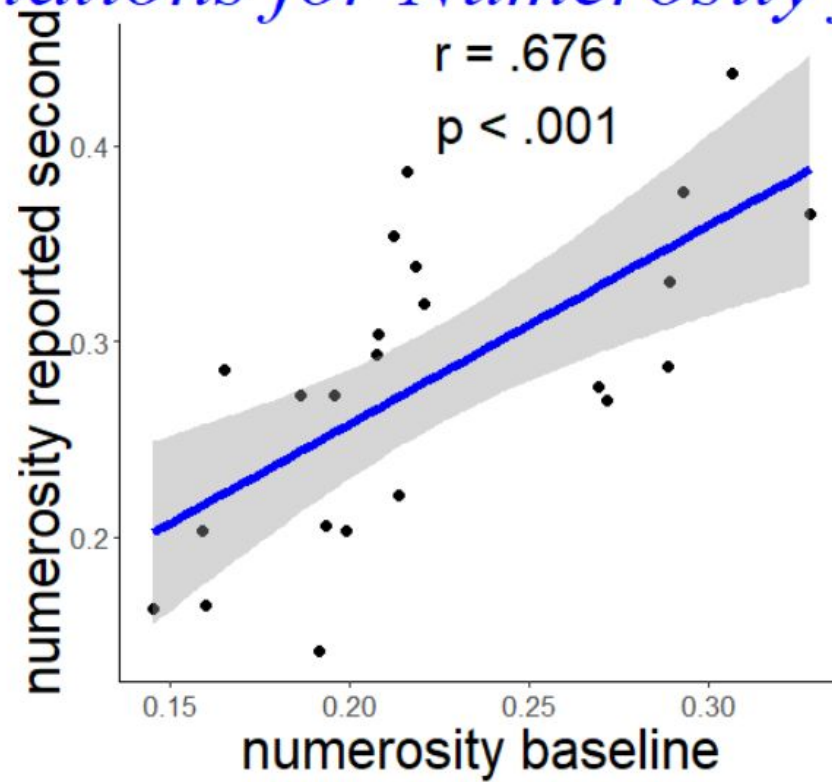
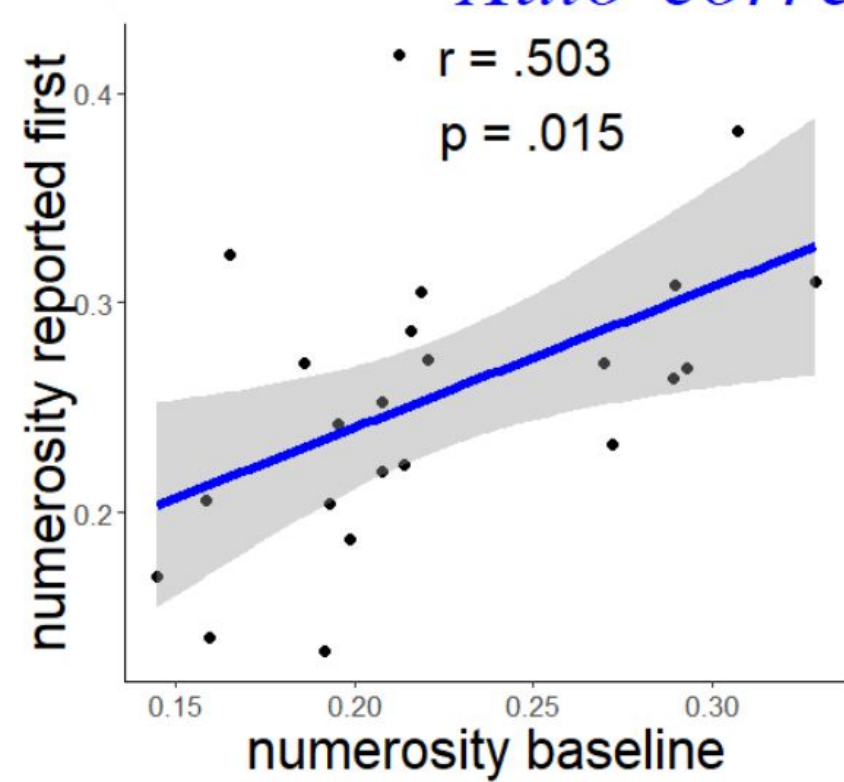


Positive correlation between errors in reporting
MEAN in different conditions



Reliable measure of MEAN calculation across

Auto-correlations for Numerosity judgements

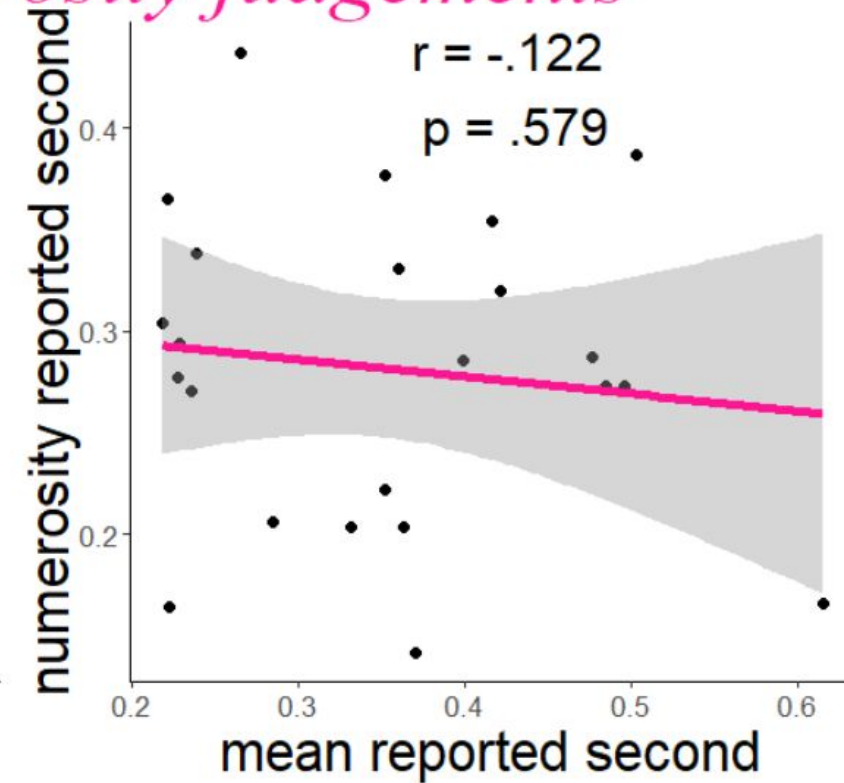
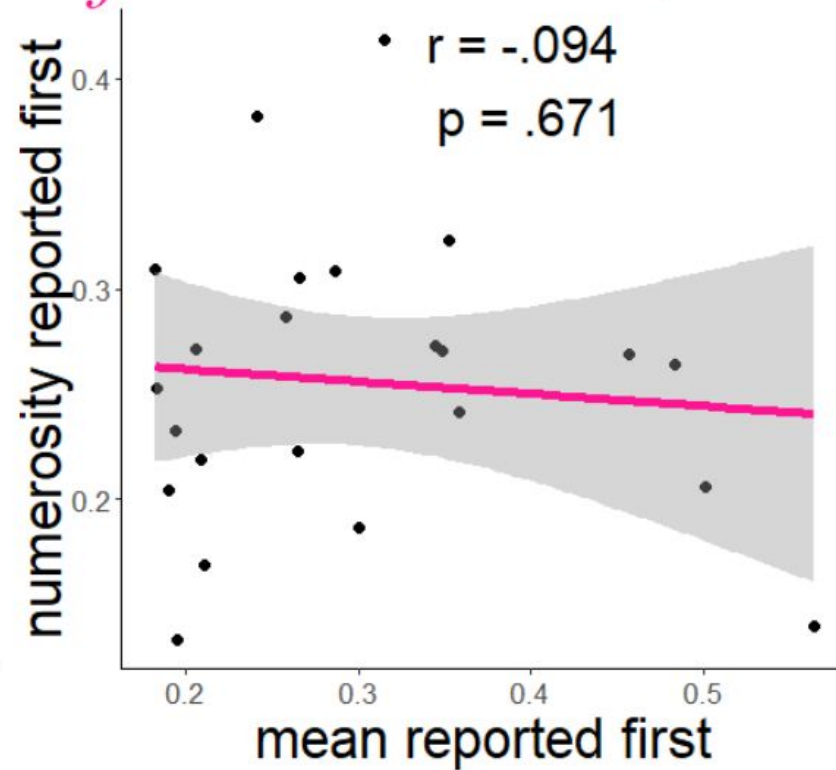
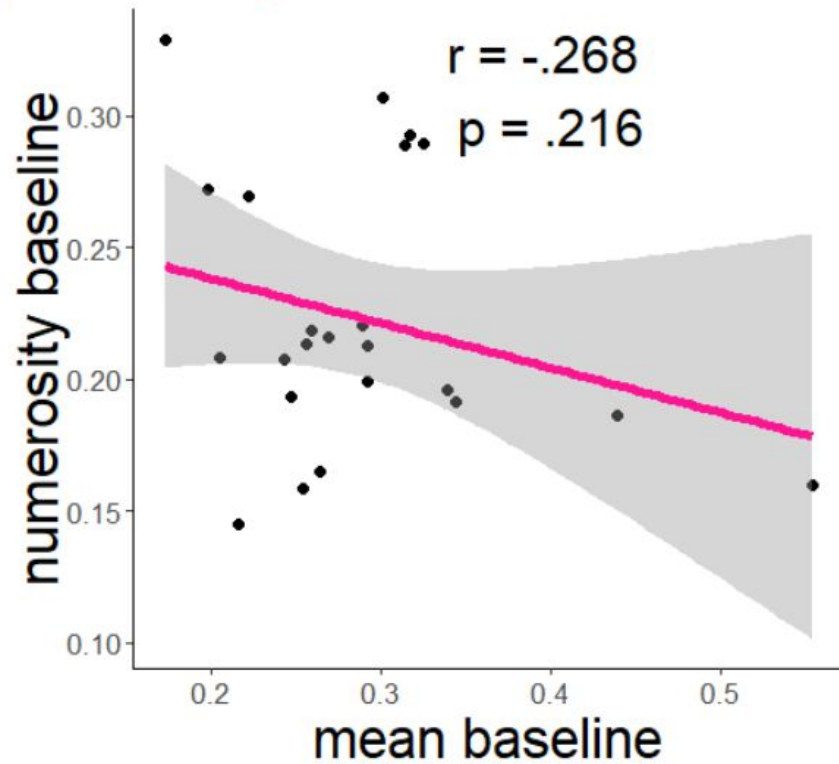


Positive correlation between errors in reporting
NUMEROSITY in different conditions



Reliable measure of NUMEROSITY calculation across

Cross-correlations for Mean and Numerosity judgements

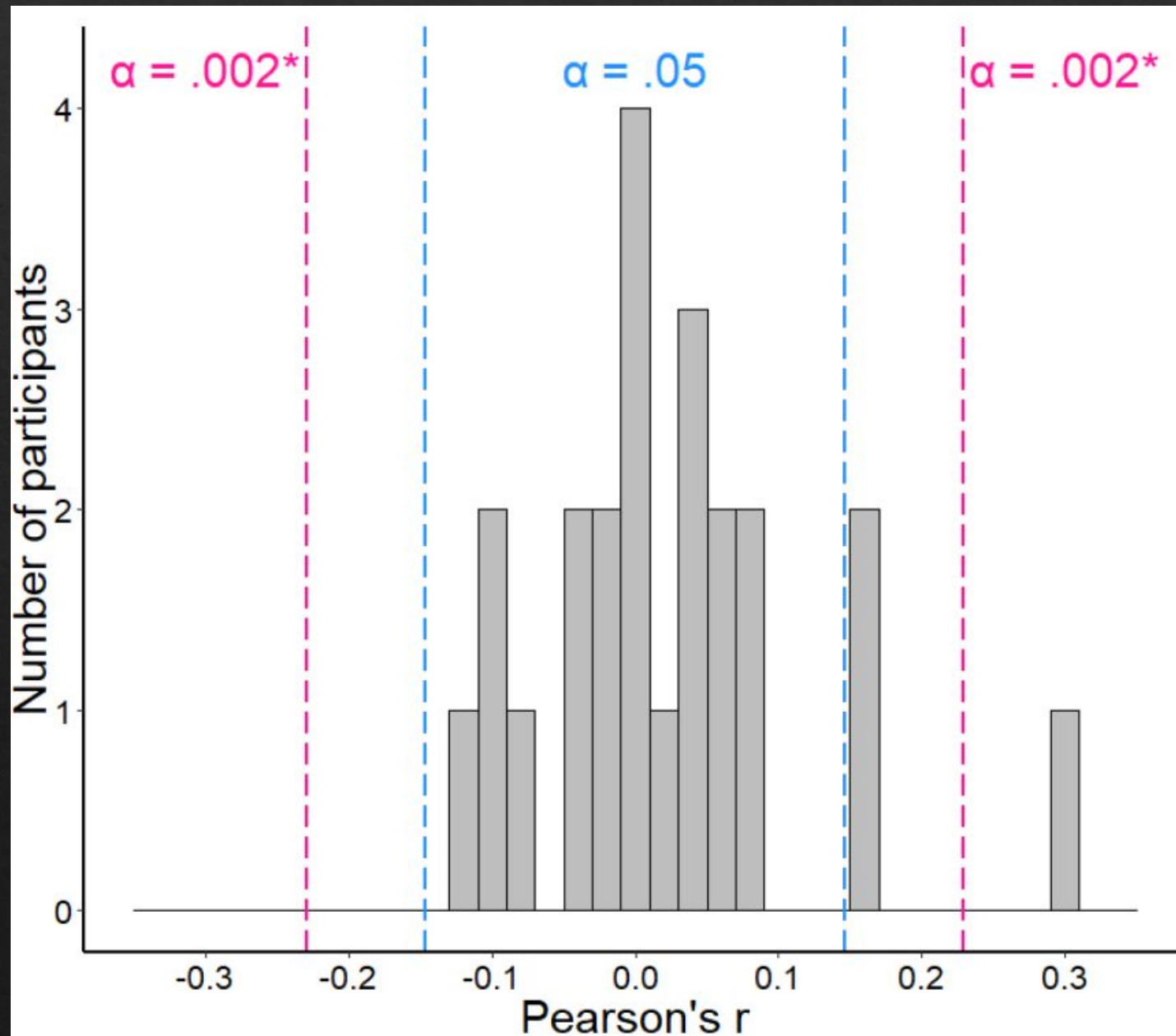


No correlation between errors in reporting different statistics



Independence between MEAN and NUMEROSITY calculations

Individual correlations

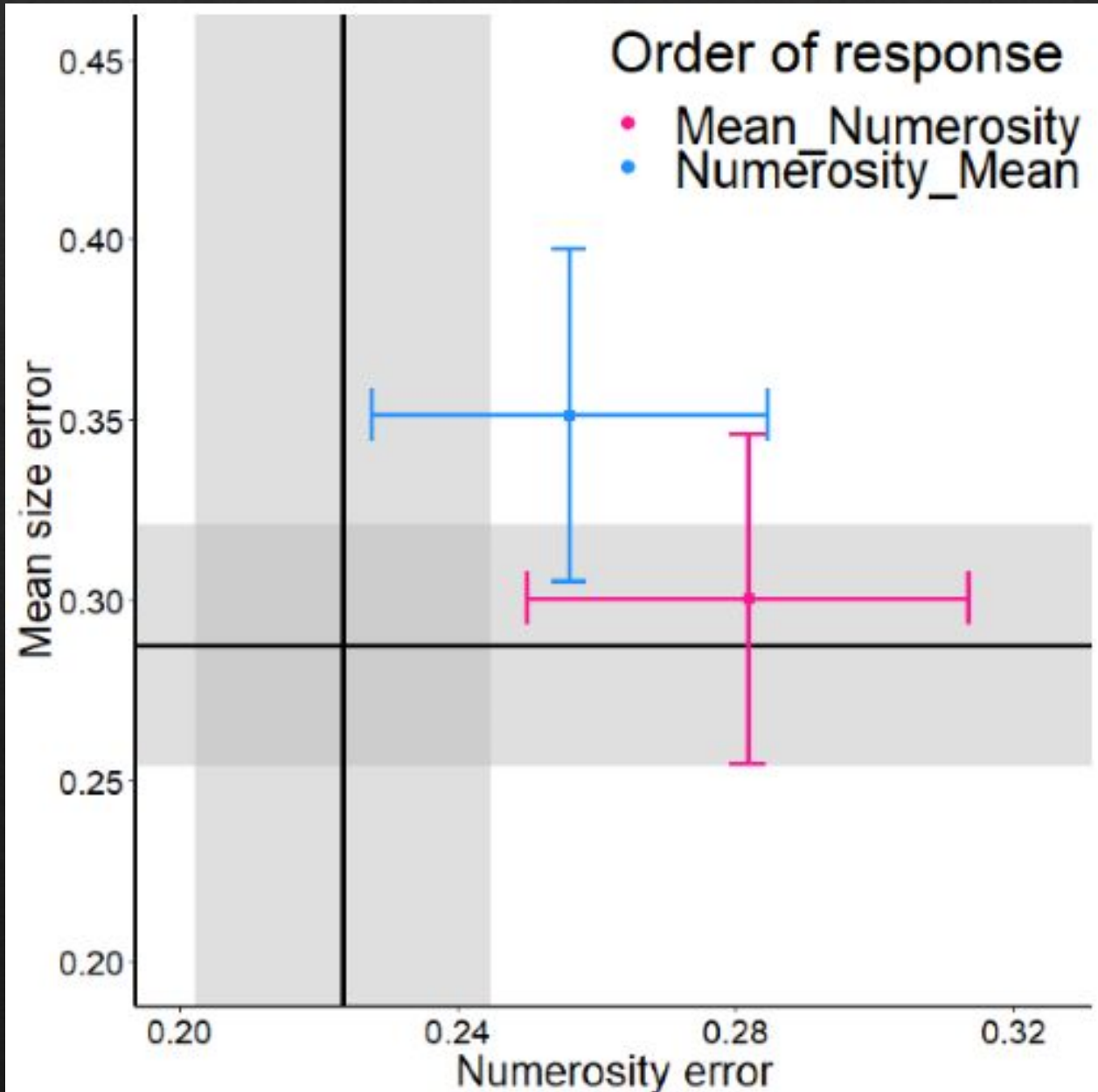


Only one participant showed significant correlation between raw errors in *both* condition



Independence between MEAN and NUMEROSITY calculations

Average errors



No difference between mean errors in *baseline condition* and the first response in *both condition* (both for NIMEROSITY and MEAN).

Conclusion

Mean and numerosity are calculated
independently and in parallel

Experiment 2

Whether mean and range can be calculated
independently and in parallel?

$N=20$

Procedure

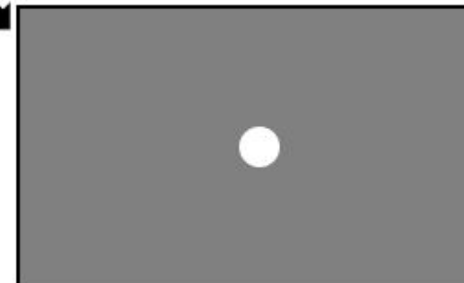
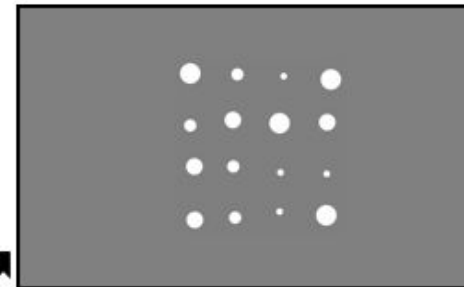
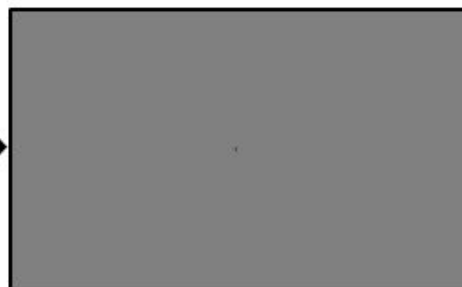
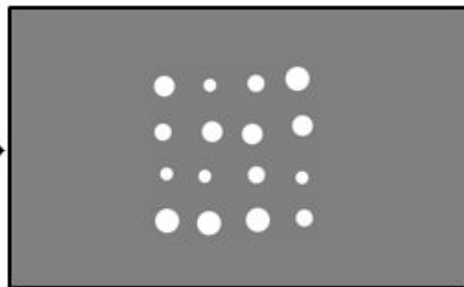
Baseline condition
2 blocks (MEAN + RANGE)

Fixation point,
500 ms

Sample set,
500 ms

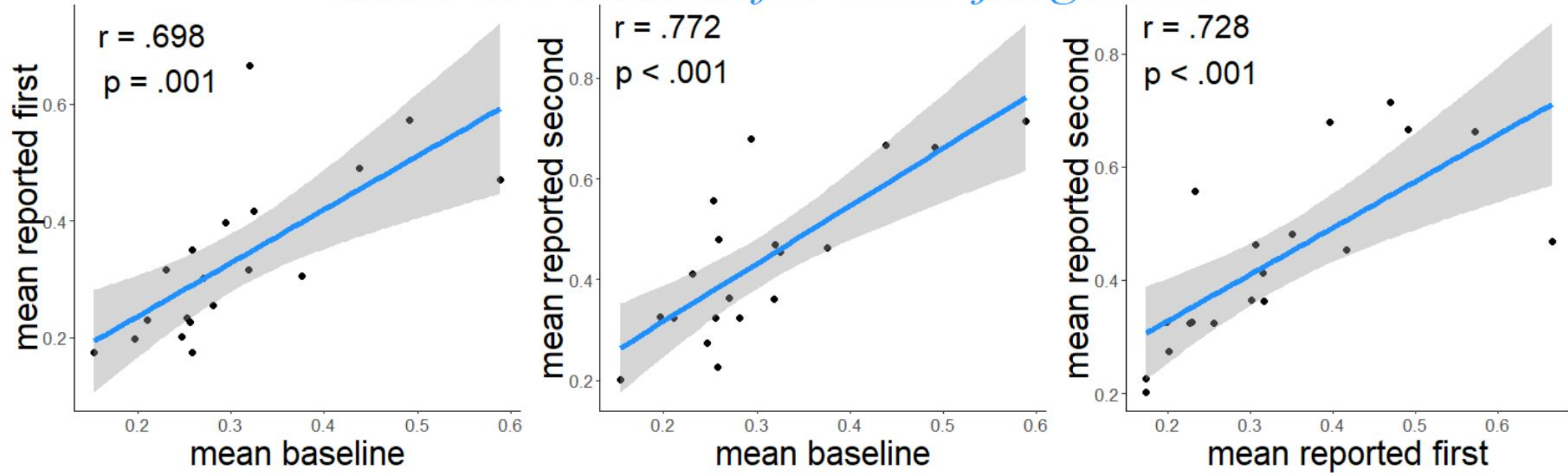
ISI,
200 ms

Response 1



| 3 blocks | Design 6 “variables” | |
|----------|---|--|
| MEAN | MEAN baseline | |
| RANGE | RANGE baseline | |
| BOTH | MEAN reported first RANGE reported first | MEAN reported second RANGE reported 1 |

Auto-correlations for Mean judgements

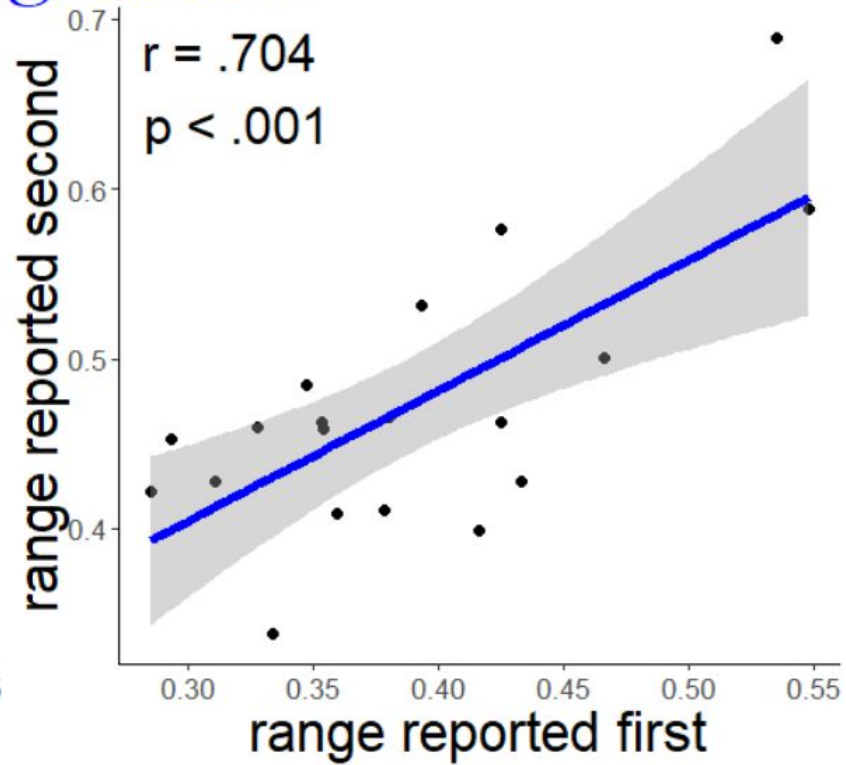
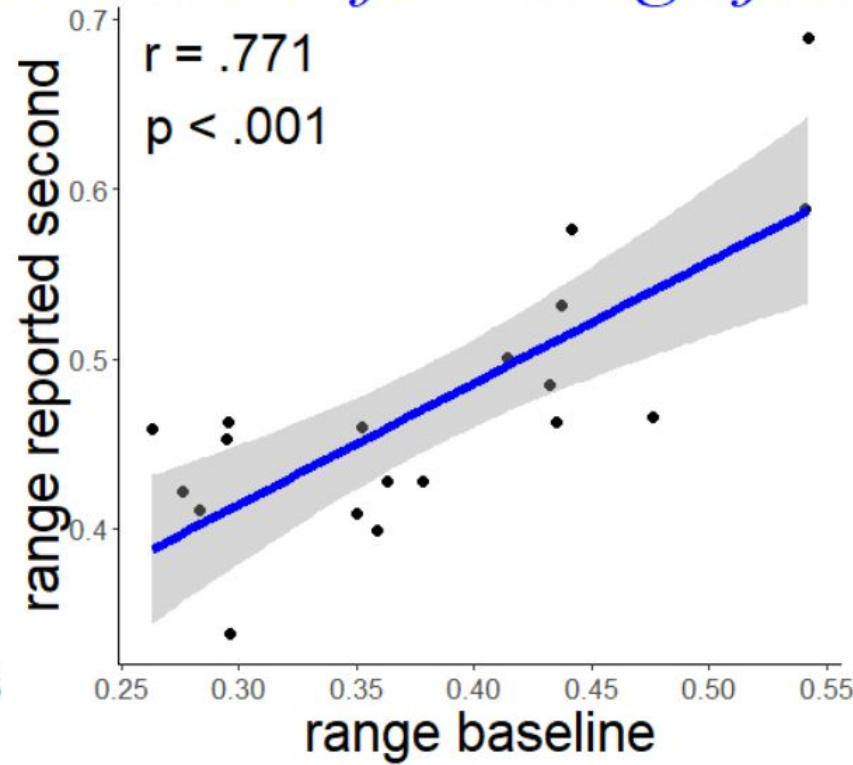
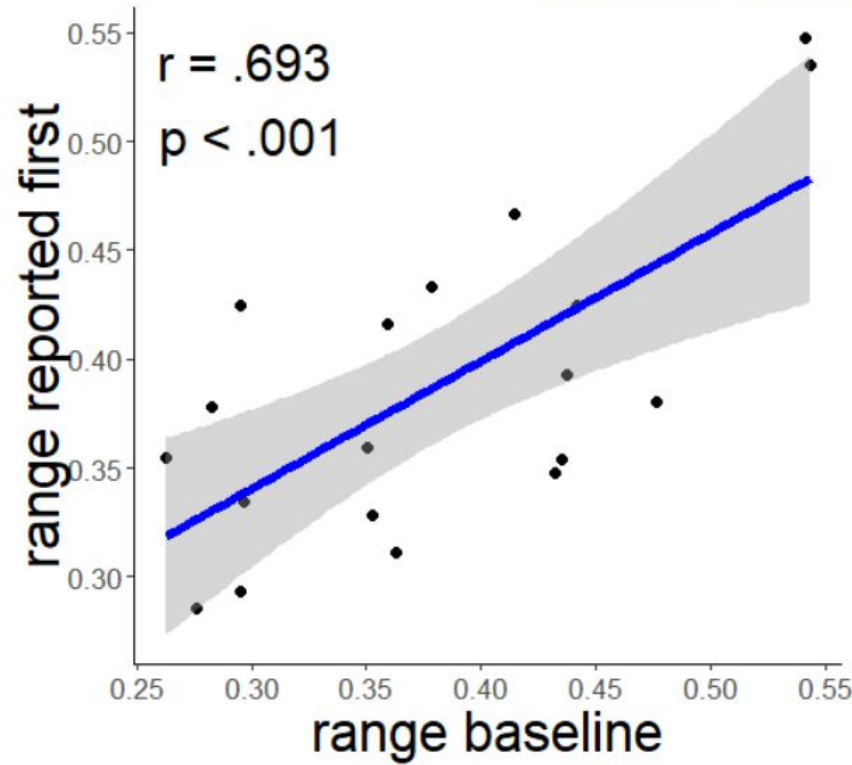


Positive correlation between errors in reporting
MEAN in different conditions



Reliable measure of MEAN calculation across

Auto-correlations for Range judgements

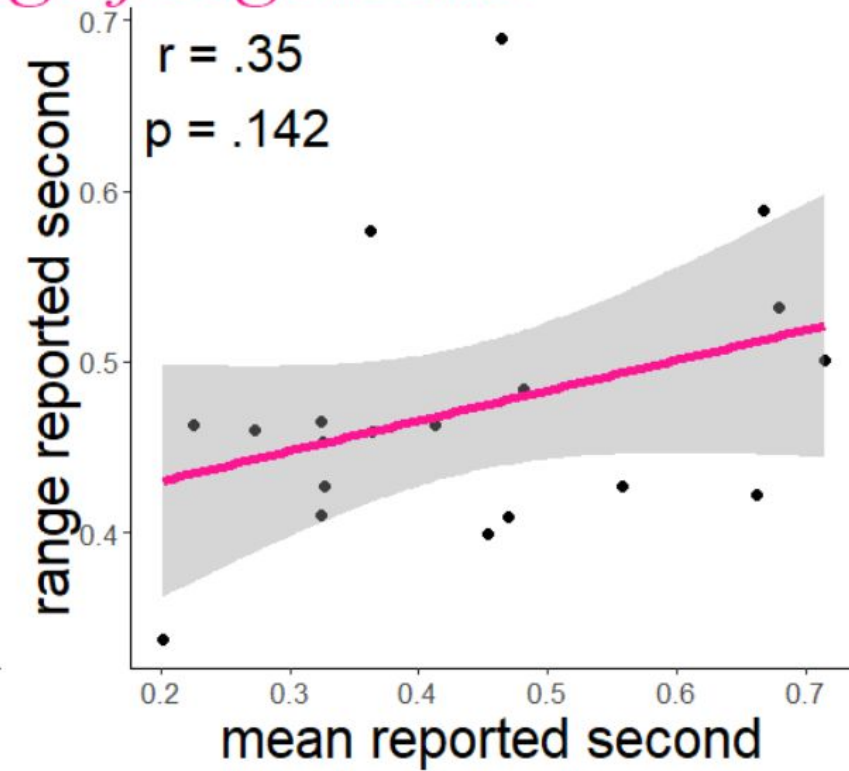
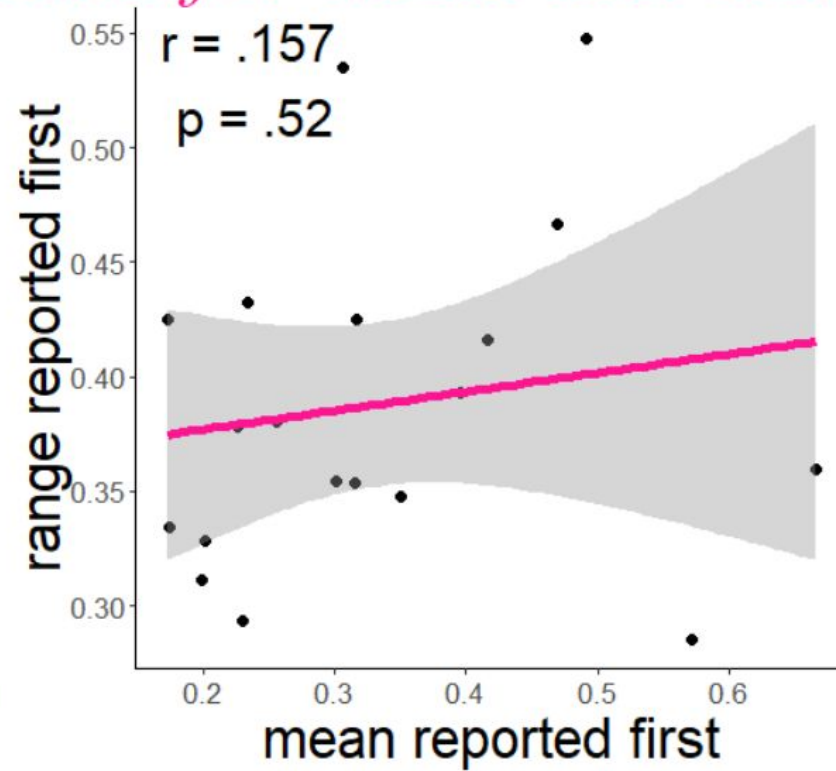
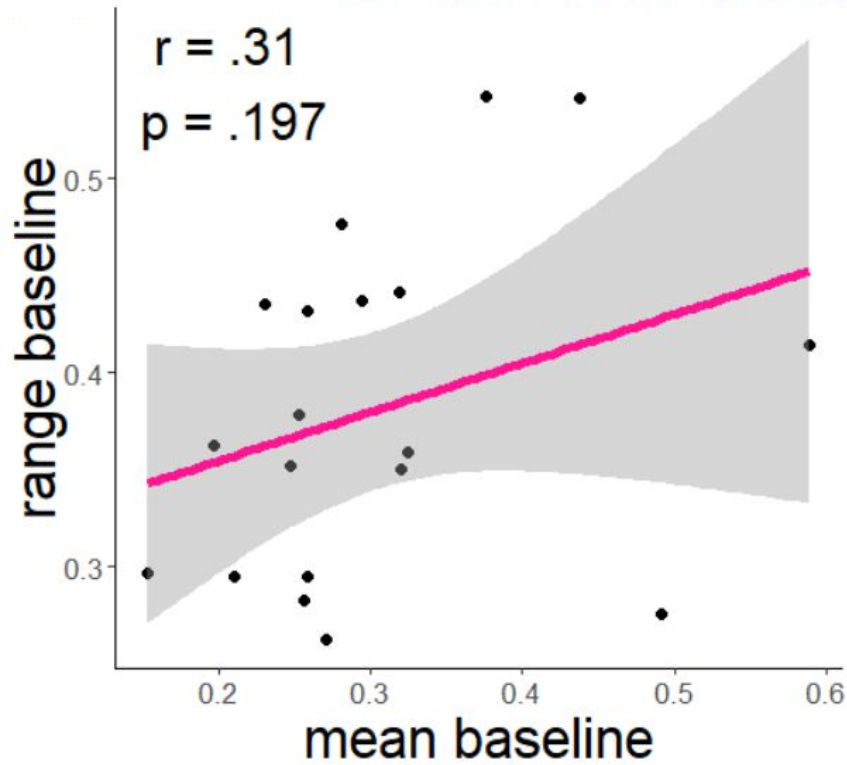


Positive correlation between errors in reporting RANGE
in different conditions



Reliable measure of RANGE calculation across conditions

Cross-correlations for Mean and Range judgements

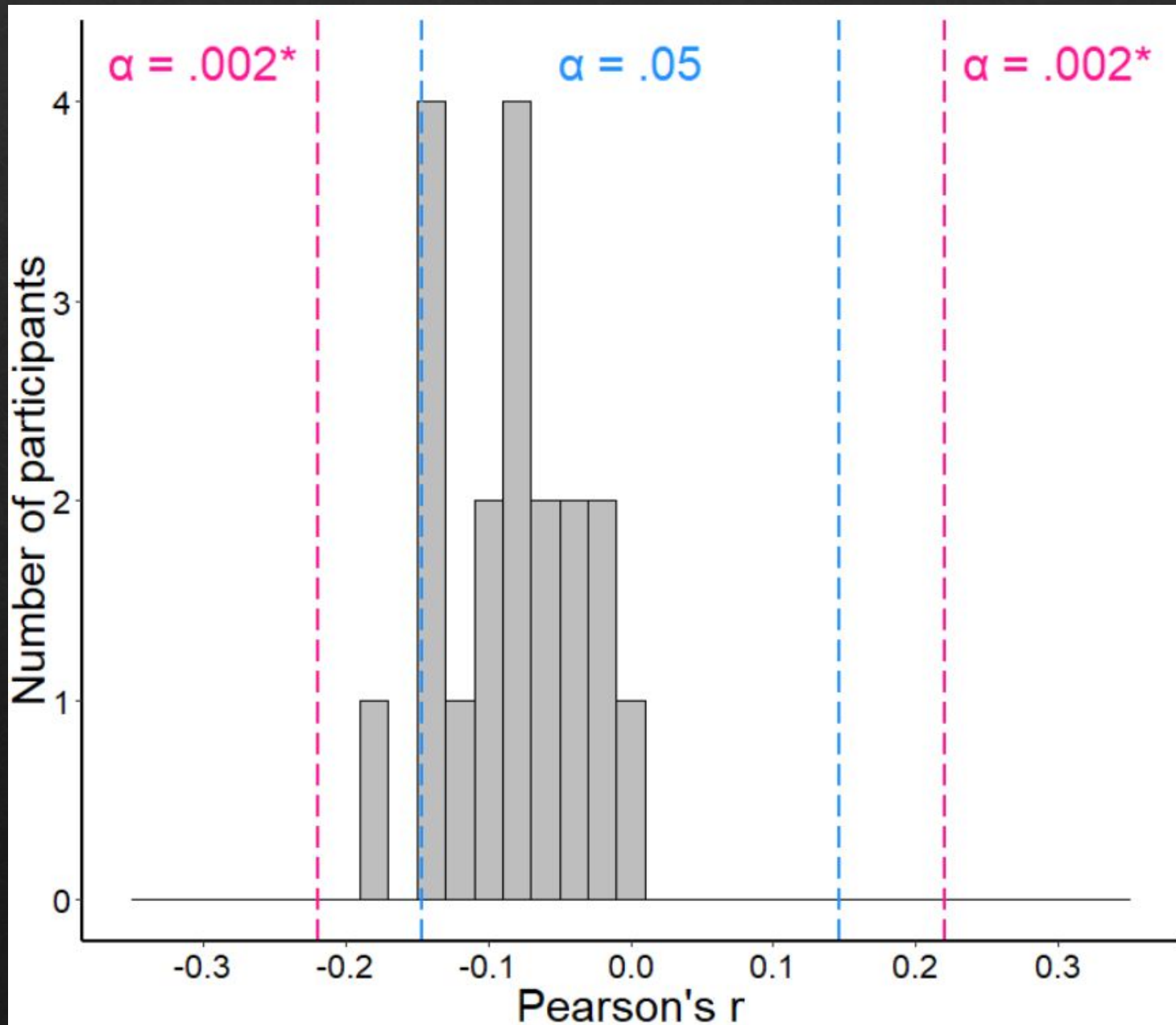


No correlation between errors in reporting different statistics



Independence between MEAN and RANGE calculations

Individual correlations

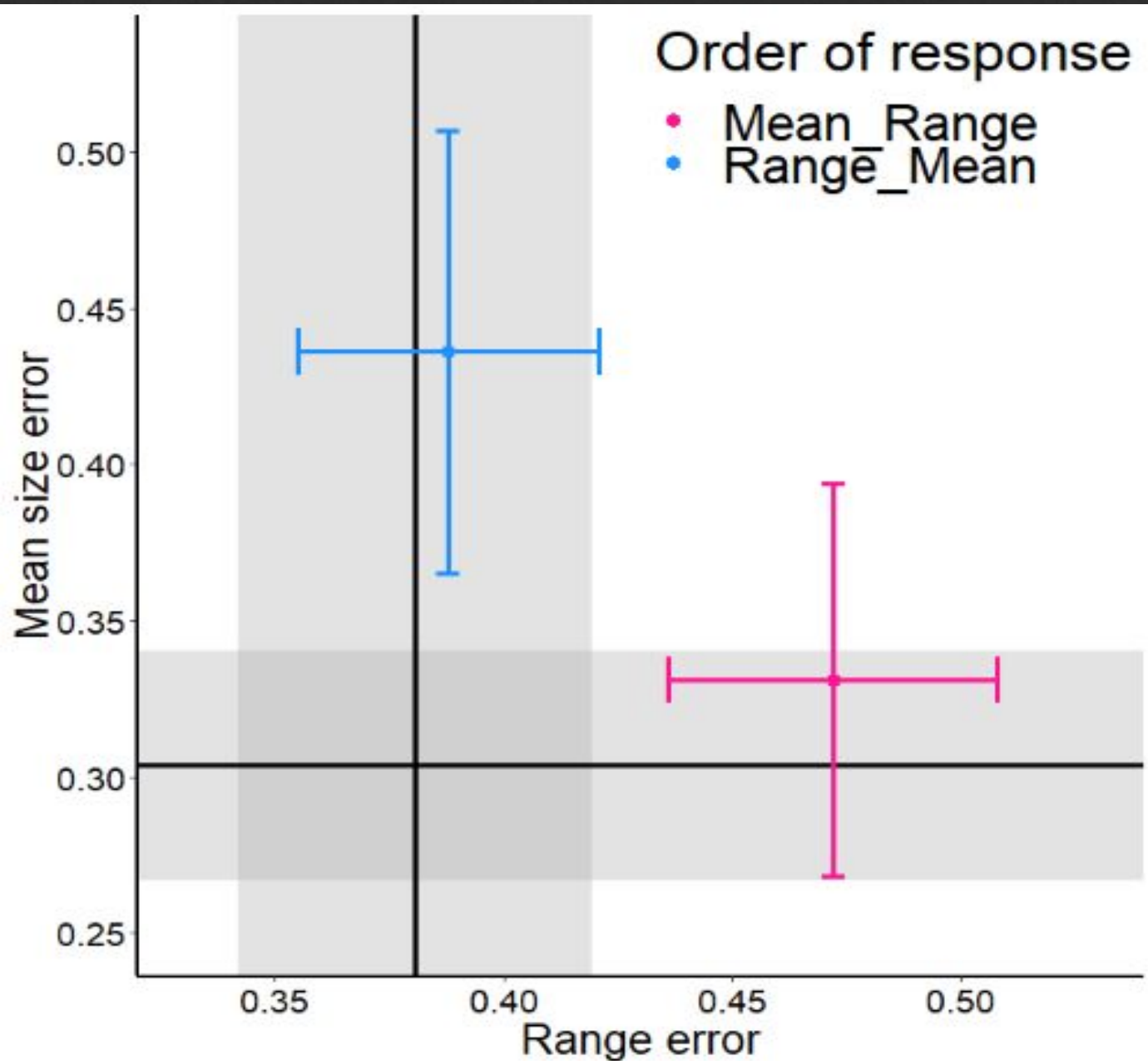


No one showed significant correlation between raw errors in *both* condition



Independence between MEAN and RANGE calculations

Average errors



No difference between mean errors in *baseline condition* and the first response in *both condition* (both for RANGE and MEAN).

Conclusions

Ensemble summary statistics (mean and numerosity, mean and range) are calculated

independently and **in parallel**

Independent mechanisms



MEAN

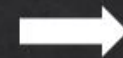
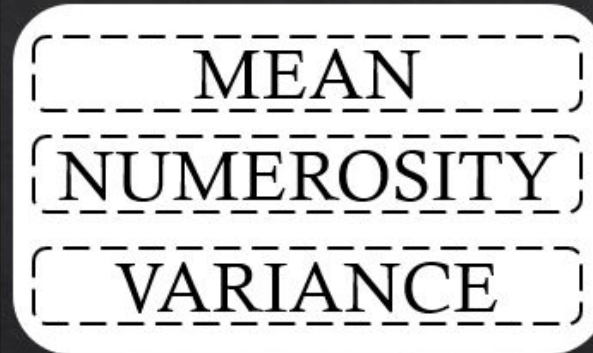


NUMEROSITY

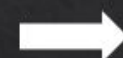


RANGE

Parallel access



REPORT



REPORT

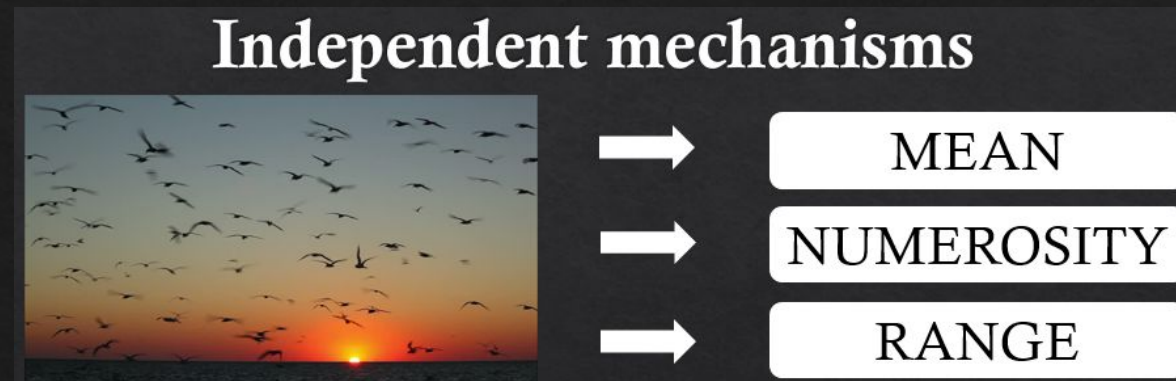


REPORT

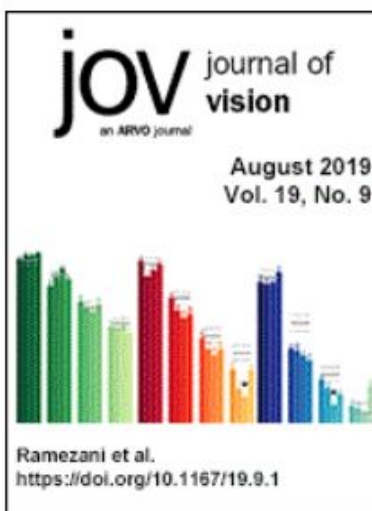
Conclusions (2)

Independent calculation of ensemble summary statistics means:

- (1) Different summaries are calculated by different (partly non-overlapping) brain regions.
- (2) The result of one calculation does not influence the result of the other calculation (unlike in mathematical statistics)



For d
please
Khvost
process
Journal



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Volume 19, Issue 9

< ISSUE >

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Article | August 2019

Independent and parallel visual processing of ensemble statistics: Evidence from dual tasks

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+ Author Affiliations

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Abstract

The visual system can represent multiple objects in a compressed form of ensemble summary statistics (such as object numerosity, mean, and feature variance/range). Yet the relationships between the different types of visual statistics remain relatively unclear. Here, we tested whether two summaries (mean and numerosity, or mean and range) are calculated independently from each other and in parallel. Our participants performed dual tasks requiring a report about two summaries in each trial, and single tasks requiring a report about one of the summaries. We estimated trial-by-trial correlations between

t
visual
tasks //
9.9.3

Thank you for being with me
till the end of the first part

Part #2



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Confidence intervals in within-subject designs

*Based on Cousineau,
2005

It is all from this 4-pages paper

Tutorials in Quantitative Methods for Psychology
2005, Vol. 1(1), p. 42-45.

DOI: 10.20982/tqmp.01.1.p042

Confidence intervals in within-subject designs: A simpler solution to Loftus and Masson's method

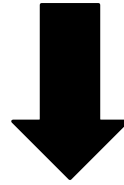
Denis Cousineau

Université de Montréal

Within-subject ANOVAs are a powerful tool to analyze data because the variance associated to differences between the participants is removed from the analysis. Hence, small differences, when present for most of the participants, can be significant even when the participants are very different from one another. Yet, graphs showing standard error or confidence interval bars are misleading since these bars include the between-subject variability. Loftus and Masson (1994) noticed this fact and proposed an alternate method to compute the error bars. However, i) their

The problem

Different subjects can perform very differently which increases a size of error bars



Inconsistency between the results of ANOVA and the graph:
ANOVA shows the effect, but the graph do not

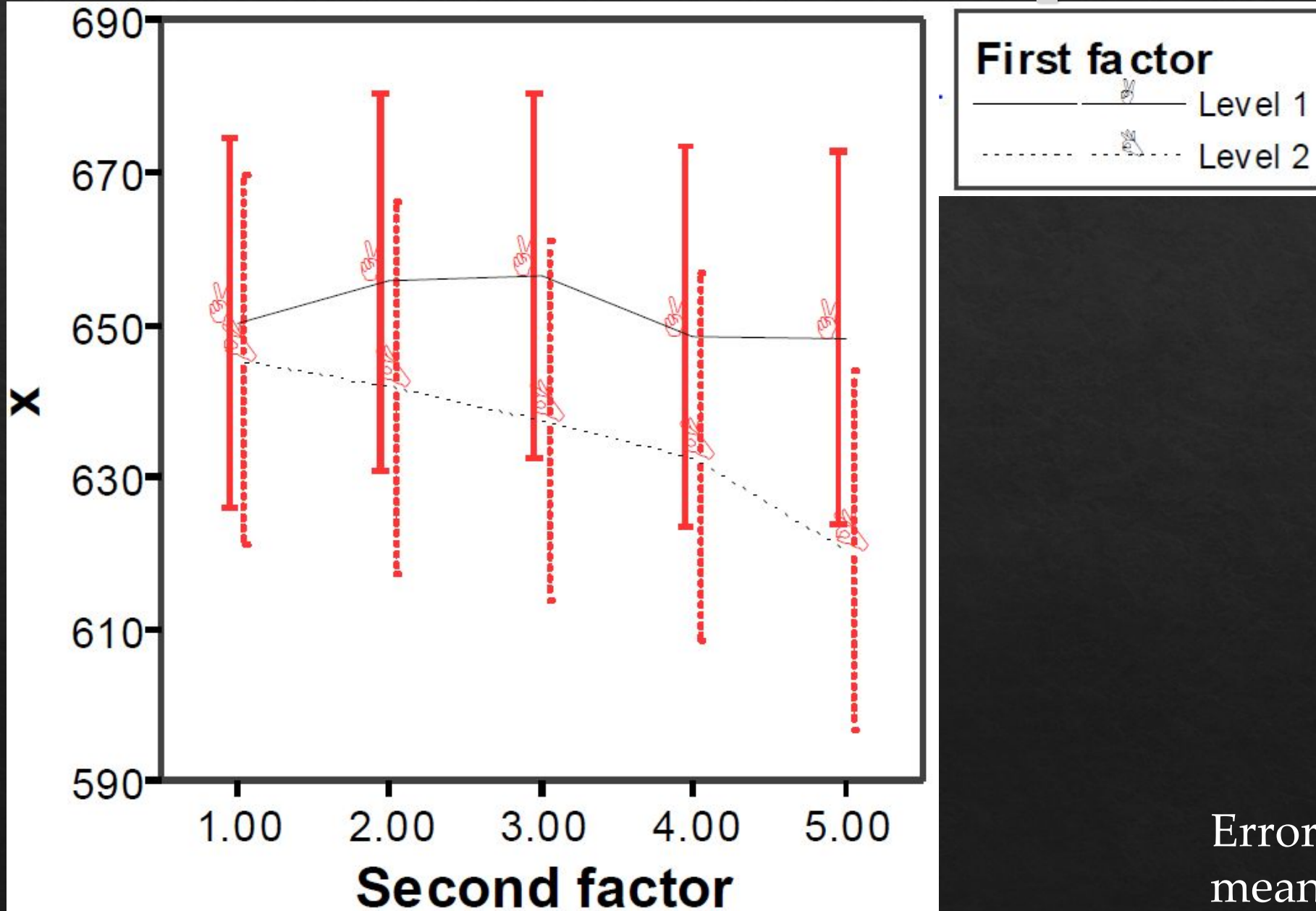
ANOVA results

an experiment with two factors, the first with two levels and the second with 5 levels

| Effect name | SS | df | MS | F | |
|-------------|-------|----|-------|------|-----|
| Factor 1 | 10621 | 1 | 10621 | 76.8 | *** |
| Error | 2073 | 15 | 135 | | |
| Factor 2 | 11784 | 4 | 8196 | 16.4 | *** |
| Error | 4378 | 60 | 72.9 | | |
| Interaction | 2250 | 4 | 562 | 6.52 | *** |
| Error | 5171 | 60 | 86.2 | | |

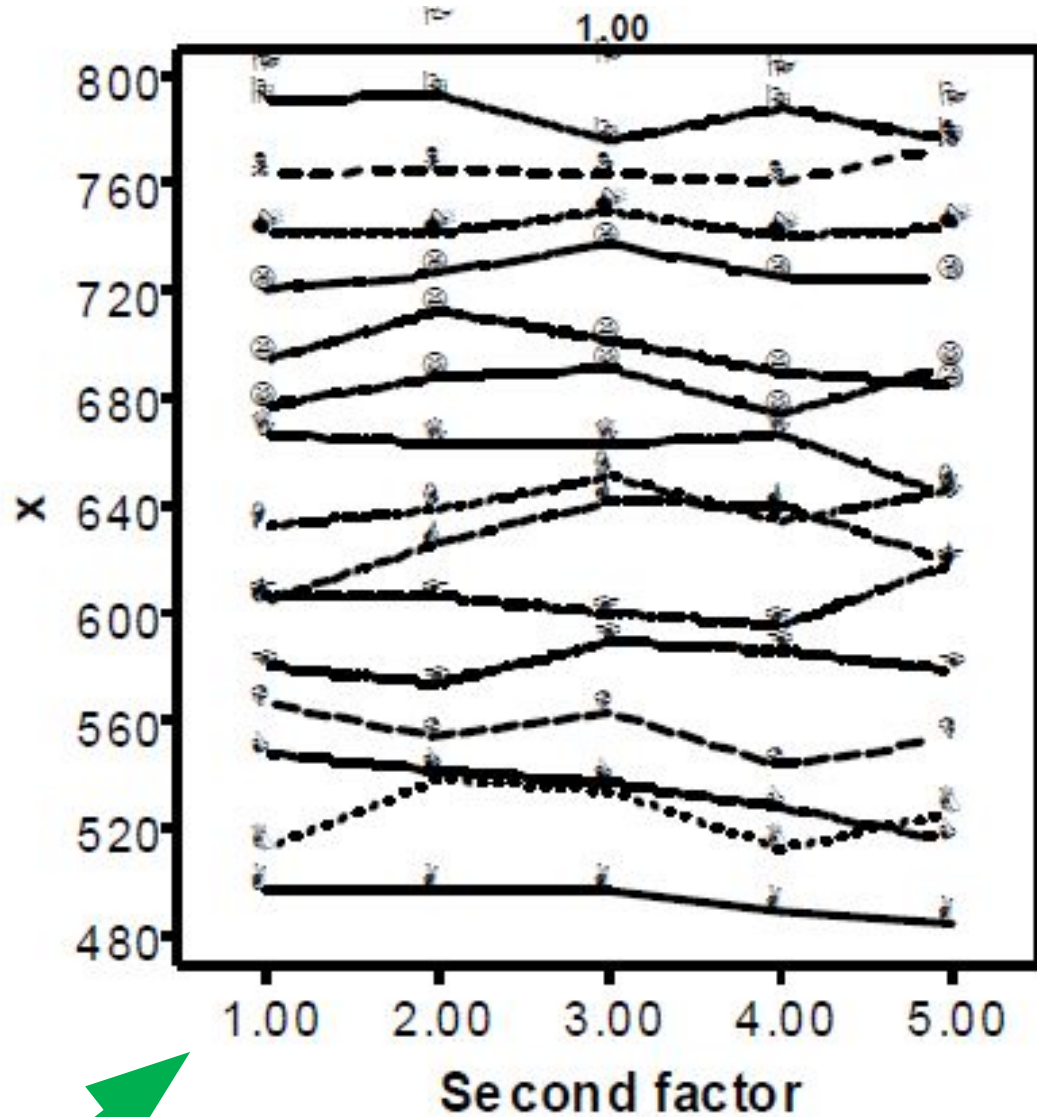
***: $p < .001$

Results of the experiment

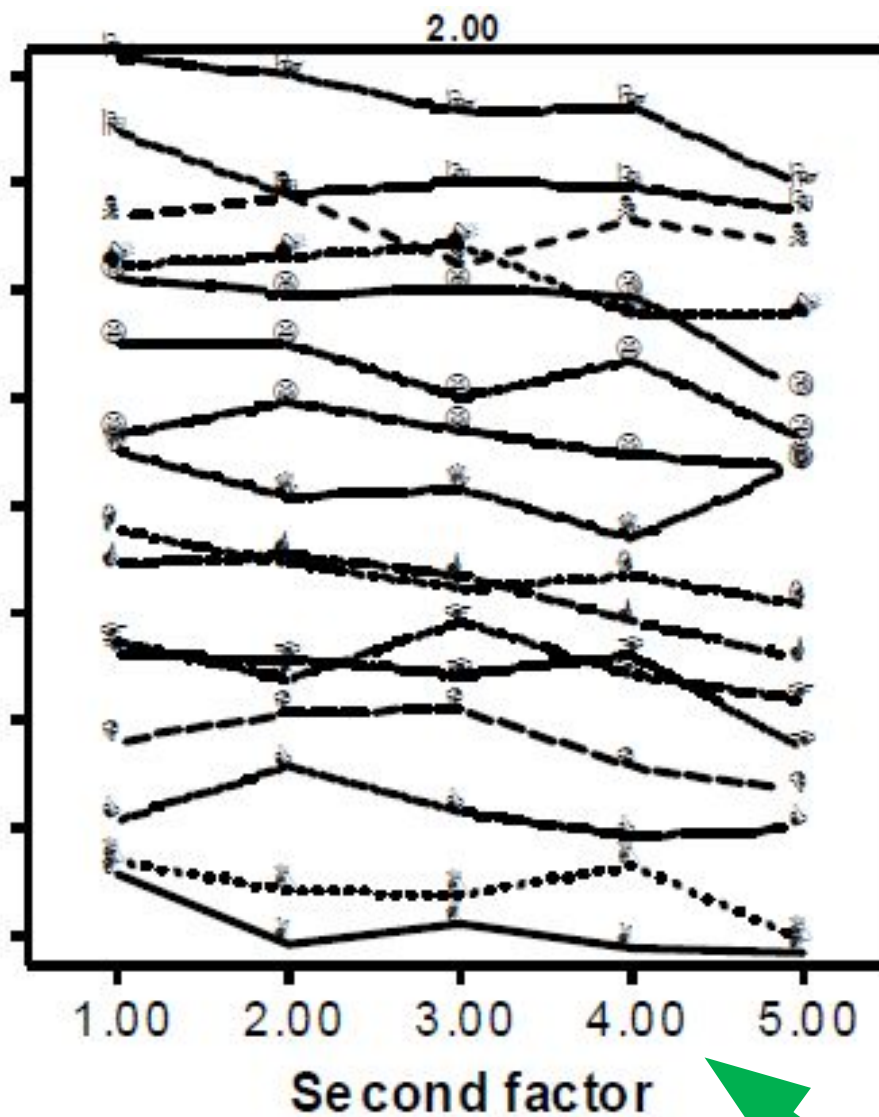


Error bars show the mean \pm 1 standard error.

The individual results of the 16 participants



The first level of the first factor.



The second level of the first

The solution of the problem

$$Y = X_{ij} - \bar{X}_1 + \bar{X}$$

$$Y = \begin{array}{c} \text{results of the} \\ \text{participant in a} \\ \text{particular} \\ \text{condition} \end{array} - \begin{array}{c} \text{the} \\ \text{participant} \\ \text{mean} \end{array} + \begin{array}{c} \text{the} \\ \text{group} \\ \text{mean} \end{array}$$

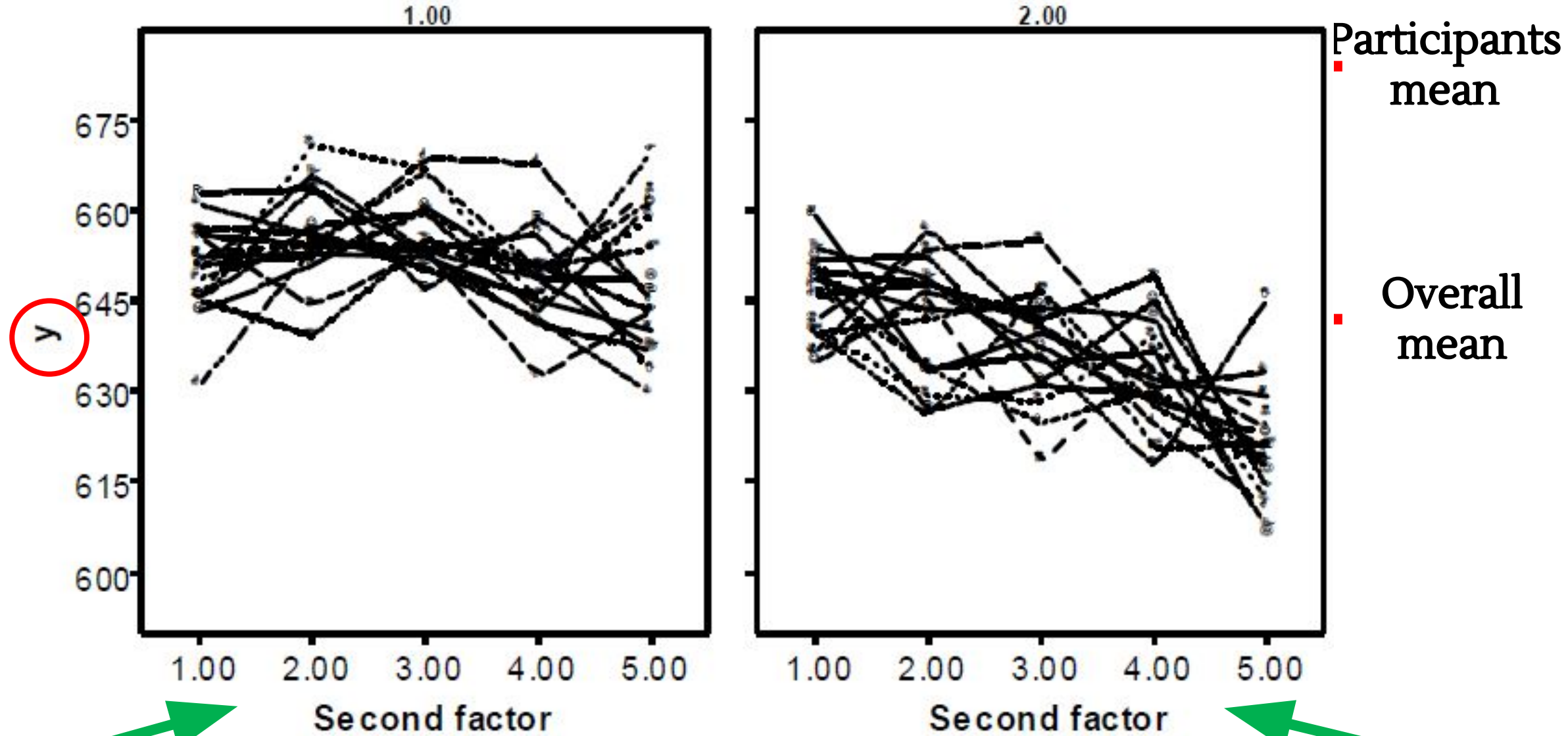
Example of calculations

| Participant | Condition | | | Mean |
|-------------|-----------|-----|-----|------|
| | 1 | 2 | 3 | |
| 1 | 550 | 580 | 610 | 580 |
| 2 | 605 | 635 | 655 | 635 |
| 3 | 660 | 690 | 710 | 690 |
| Mean | 605 | 635 | 655 | 635 |



| Participant | Condition | | | Mean |
|-------------|-------------------------|-------------------------|-------------------------|------|
| | 1 | 2 | 3 | |
| 1 | $550 - 580 + 635 = 605$ | $580 - 580 + 635 = 635$ | $610 - 580 + 635 = 665$ | 580 |
| 2 | $605 - 635 + 635 = 605$ | $635 - 635 + 635 = 635$ | $655 - 635 + 635 = 655$ | 635 |
| 3 | $660 - 690 + 690 = 660$ | $690 - 690 + 690 = 690$ | $710 - 690 + 690 = 710$ | 690 |
| Mean | 605 | 635 | 655 | 635 |

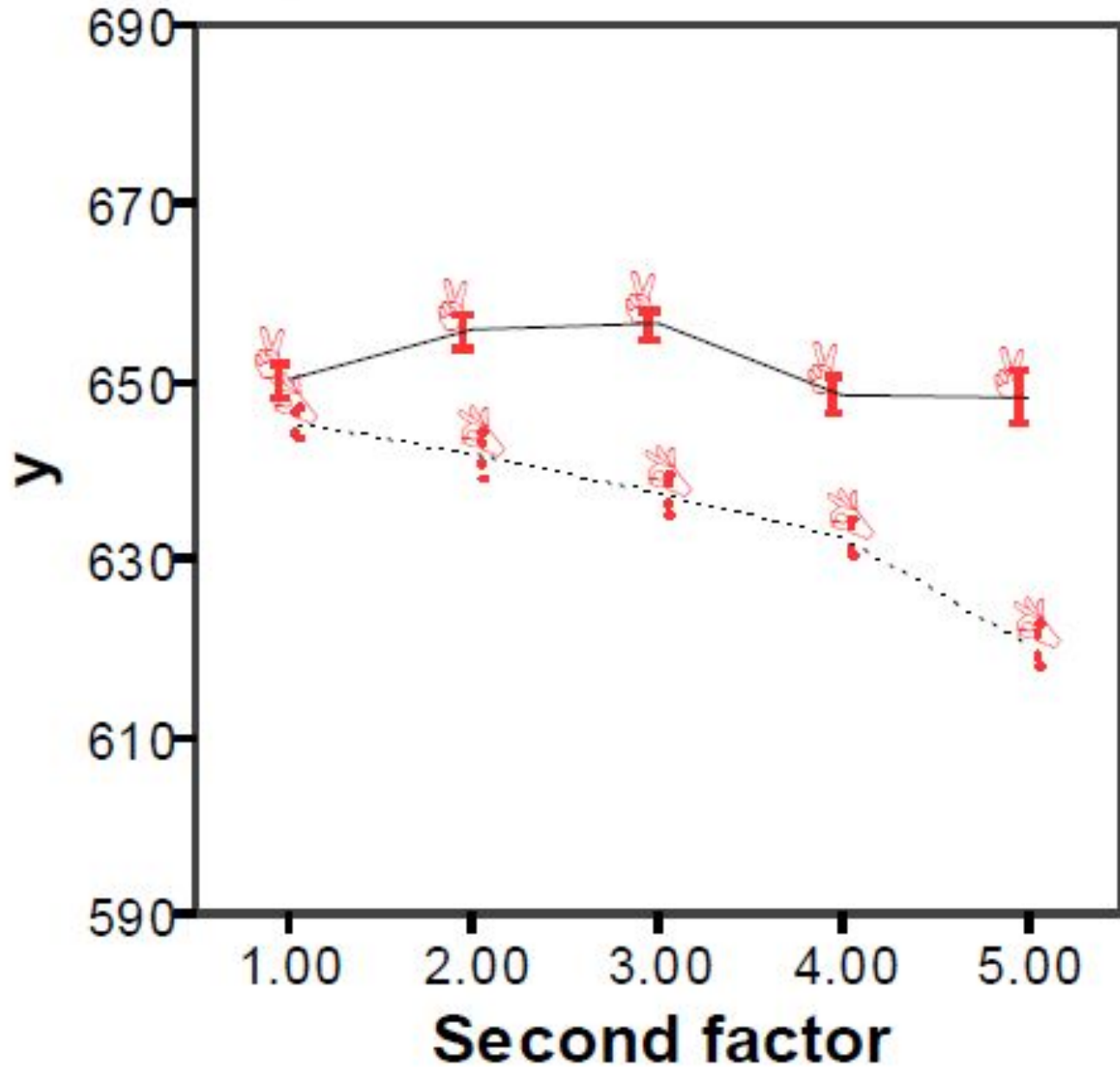
The individual results of the 16 participants after the individual differences were removed



The first level of the first factor.

The second level of the first

The graph after the individual differences were removed



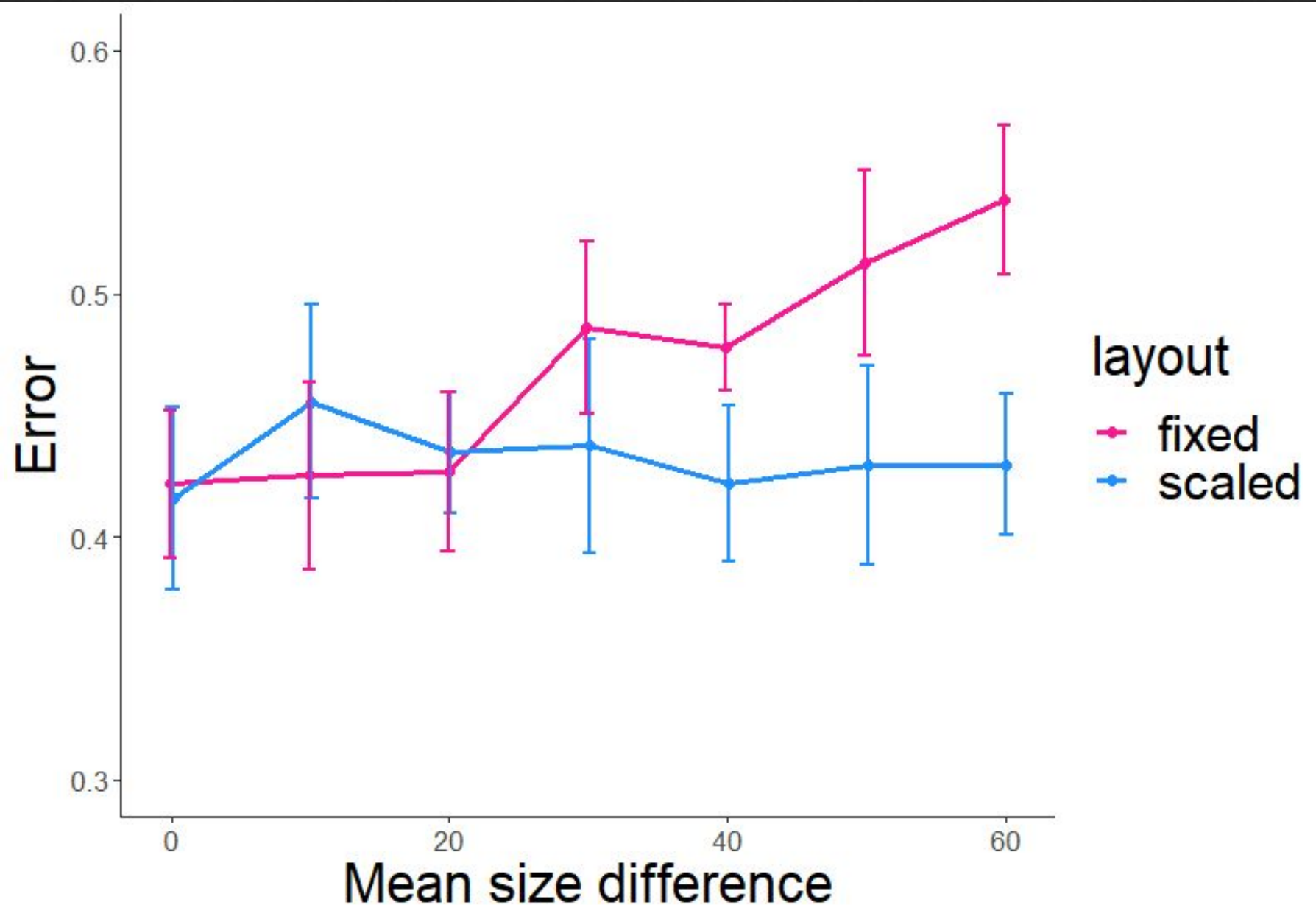
Error bars show the
mean ± 1 standard error.

$$Y = X_{ij} - \bar{X}_1 + \bar{X}$$

$Y =$ results of the the the
participant in participant group
particular condition — mean + mean

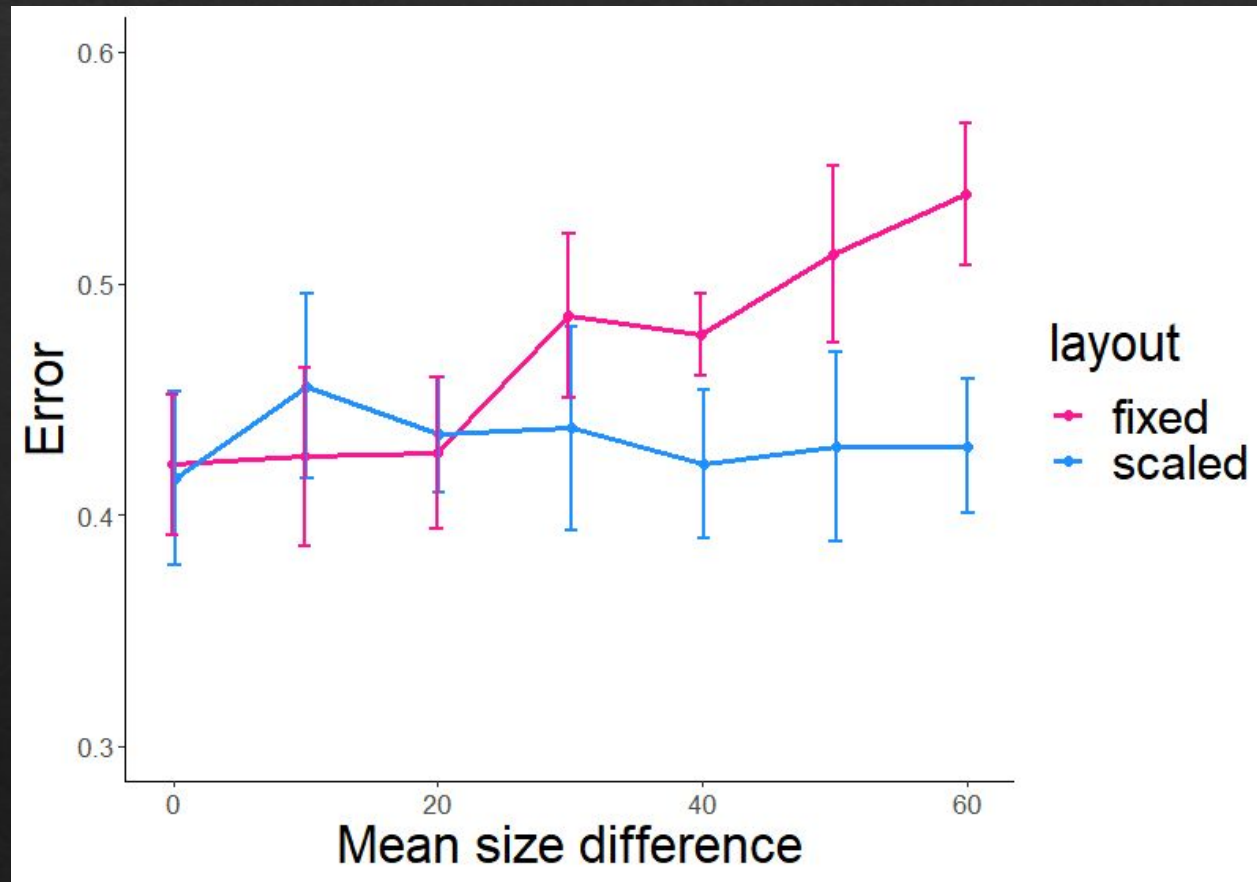
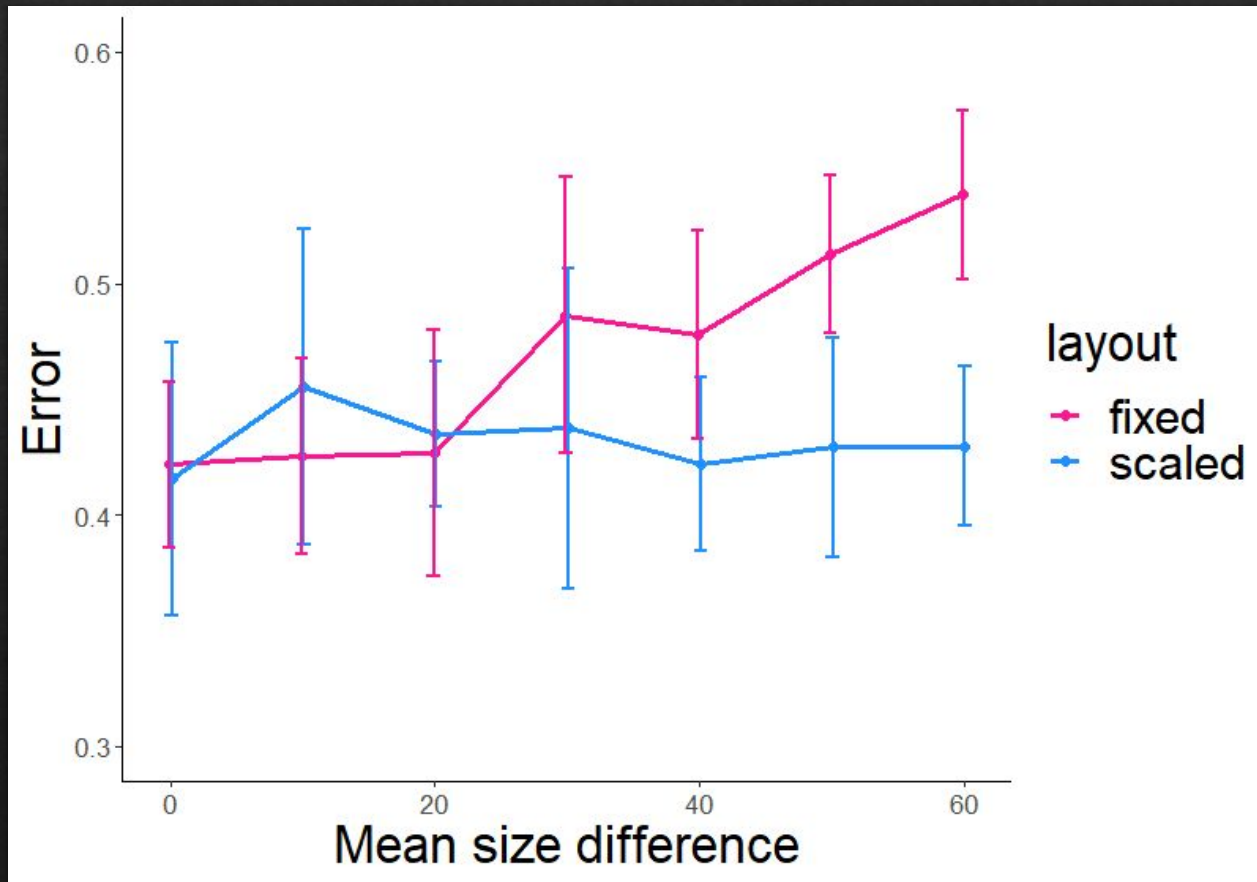
NOTE: Y is only useful for graphing purposes; for the analyses, continue to use the original data.

Example from real life



Error bars show SEM.

Example from real life



Error bars show SEM.

Hope you will use it

Thank you
For your attention