## Vladislav Khvostov

Part \#1: Independent and parallel visual processing of ensemble statistics: Evidence from dual tasks

Part \#2: Confidence intervals in within-subject designs

Independent and paisillel visual processing of ensemble statistics: Evidence from dual tasks

Vladislav Khvostov and Igor Utochkin

## An example



## Greater or smaller than average?

## Ensemble summary statistics

- The visual system can compute mean (Alvarez \& Oliva, 2009), numerosity (Halberda, Sires, \& Feigenson, 2006), variance/range (Dakin \& Watt, 1997)
- Ensemble statistics can be calculated for low-level features:
- color (Gardelle \& Summerfield, 2011),
- orientation (Parkes, Lund, Angelucci, Solomon, \& Morgan, 2001),
- size (Ariely, 2001),
and for high-level features:
- emotions, gender, etc. (Sweeny \& Whitney, 2014, Haberman \& Whitney, 2007, 2009).


## Independent mechanisms



## One mechanism


«GENERAL ENSEMBLE PROCESSOR»
Mean, Numerosity
Range

## Correlational approach

## Independenc

## Prediction

Independent mechanisms


## Parallelism

Parallel access (no interference) NUMEROSTITY VAARIANCE

Non-parallel access (interference)

REPORT REPORT REPORT シ

## Parallelism test



Observers should compute only one statistics

Observers should compute both statistics

## Parallelism test

Parallel access

| MEĀN | REPORT |
| :---: | :---: |
| \{NUMEROSITY | REPORT |
| T-VARIANCE- | REPORT |

Non-parallel access


## Error in single task <br> Error in dual task

## Interference

## No interference

## Error in single task <br> Error in dual task

## Experiment 1

Whether mean and numerosity can be calculated independently and in parallel?
$\mathrm{N}=23$

## Procedure

## Bdsethearoditition 21bbdeks (MEAN七NUOKKRRSSITYY)



## Design

## MEAN baseline

## NIMEROSITY baseline

BOTH

MEAN reported first NIMEROSITY reported first

MEAN reported second

NIMEROSITY reported

## Data analysis

$$
\text { Error }=\left|\frac{\text { oobserver's response-correct response }}{\text { correct response }}\right|
$$

(1) Correlation between mean errors of 6 variables (across observers)
(2) Trial-by-trial correlation between an error
 in the mean judgment and an error in the numerosity judgment (separately for each participants)
(3) Comparison of mean errors in baseline and both conditions



Positive correlation between errors in reporting MEAN in different conditions

Reliable measure of MEAN calculation across

Auto-correlations for Numerosity judgements


## Positive correlation between errors in reporting NUMEROSITY in different conditions

Reliable measure of NUMEROSITY calculation across


No correlation between errors in reporting different statiptics

## Independence between MEAN and NUMEROSITY calculations

## Individual correlations

Only one participant showed significant correlation between raw errors in both condition

Independence between MEAN and NUMEROSITY calculations

## Average errors



No difference between mean errors in baseline condition and the first response in both condition
(both for NIMEROSITY and MEAN).

## Conclusion

## Mean and numerosity are calculated independently and in parallel

## Experiment 2

Whether mean and range can be calculated independently and in parallel?
$\mathrm{N}=20$

## Procedure

## BBkellinearoditlition 211bbdekk (MEAN $\oplus$ RRAGGEE)

Response 1


## Design

## 6 "variables"

## anara <br> MEAN

## MEAN baseline

## RANGE

## RANGE baseline

## BOTH

MEAN<br>reported first<br>RANGE<br>reported first

MEAN reported second

RANGE reported

Auto-correlations for Mean judgements


Positive correlation between errors in reporting MEAN in different conditions

Reliable measure of MEAN calculation across

Auto-correlations for Range judgements


## Positive correlation between errors in reporting RANGE

 in different conditionsReliable measure of RANGE calculation across conditions


No correlation between errors in reporting different statictics

## Independence between MEAN and RANGE calculations

## Individual correlations



No one showed significant correlation between raw errors in both condition

Independence between MEAN and RANGE calculations

## Average errors



No difference between mean errors in baseline condition and the first response in both condition
(both for RANGE and MEAN).

## Conclusions

Ensemble summary statistics (mean and numerosity, mean and range) are calculated

## independently and in parallel

Parallel access
Independent mechanisms


## Conclusions (2)

 Independent calculation of ensemble summary statistics means:(1) Different summaries are calculated by different (partly non-overlapping) brain regions.
(2) The result of one calculation does not influence the result of the other calculation (unlike in mathematical statistics)

Independent mechanisms



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## Independent and parallel visual processing of ensemble statistics: Evidence from dual tasks

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Introduction
Experiment 1
Experiment 2A
Experiment 2B
General discussion
Acknowledgments
References

## Abstract

The visual system can represent multiple objects in a compressed form of ensemble summary statistics (such as object numerosity, mean, and feature variance/range). Yet the relationships between the different types of visual statistics remain relatively unclear. Here, we tested whether two summaries (mean and numerosity, or mean and range) are calculated independently from each other and in parallel. Our participants performed dual tasks requiring a report about two summaries in each trial, and single tasks requiring a report about one of the summaries. We estimated trial-bv-trial correlations between

## Thank you for being with me till the end of the first part

# Confidence intervals in within-subject designs 

*Based on Cousineau,

## It is all from this 4-pages paper

# Confidence intervals in within-subject designs: A simpler solution to Loftus and Masson's method 

## Denis Cousineau

Université de Montréal

Within-subject ANOVAs are a powerful tool to analyze data because the variance associated to differences between the participants is removed from the analysis. Hence, small differences, when present for most of the participants, can be significant even when the participants are very different from one another. Yet, graphs showing standard error or confidence interval bars are misleading since these bars include the between-subject variability. Loftus and Masson (1994) noticed this fact and proposed an alternate method to compute the error bars. However, i) their

## The problem

## Different subjects can perform very differently which increases a size of error bars

Inconsistency between the results of ANOVA and the graph: ANOVA shows the effect, but the graph do not

## ANOVA results

an experiment with two factors, the first with two levels and the second with 5 levels

| Effect name | SS | dl | MS | F |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Factor 1 | 10621 | 1 | 10621 | 76.8 |  |
| Error | 2073 | 15 | 135 |  |  |
| Factor 2 | 11784 | 4 | 8196 | 16.4 | $* * *$ |
| Error | 4378 | 60 | 72.9 |  |  |
| Interaction | 2250 | 4 | 562 | 6.52 | $* * *$ |
| Error | 5171 | 60 | 86.2 |  |  |

[^0]
## Results of the experiment



Error bars show the mean $\pm 1$ standard error.

## The individual results of the 16 participants



The first level of the first factor.


The second level of the first

## The solution of the problem

$$
Y=X_{i j}-\bar{X}_{1}+\bar{X}
$$

## results of the the the <br> $Y=$ participant in a particular <br> _ participant + mean <br> group mean

Example of calculations
Condition

| Participant |
| :---: |
| 1 |
| 2 |
| 3 |

Mean

| 1 | 2 | 3 | Mean |
| :---: | :---: | :---: | :---: |
| 550 | 580 | 610 | 580 |
| 605 | 635 | 655 | 635 |
| 660 | 690 | 710 | 690 |
| 605 | 635 | 655 | 635 |

Condition

| Participant | 1 | 2 | 3 | Mean |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $550-580+635=60$ | $\begin{gathered} 580-580+635=63 \\ 5 \end{gathered}$ | $\begin{gathered} 610-580+635=66 \\ 5 \end{gathered}$ | 580 |
| 2 | $605-635$ | $635-635+635$ | $655-635+635$ | 635 |
| 3 | $\begin{gathered} 660-6590 \\ +635 \end{gathered}$ | $\begin{gathered} 690-690 \\ +635 \end{gathered}$ | $\begin{gathered} 710-690 \\ +635 \\ \hline \end{gathered}$ | 690 |
| Mean | 605 | 635 | 655 | 635 |

## The individual results of the 16 participants after the individual differences were removed




The graph after the individual differences were removed


Error bars show the mean $\pm 1$ standard error.
$Y=\begin{gathered}\text { results of the } \\ \text { participant in } \\ \text { particular condition }\end{gathered} \quad \begin{gathered}\text { the } \\ \text { participant } \\ \text { mean }\end{gathered}+\underset{\text { group }}{\text { thean }}$

NOTE: $Y$ is only useful for graphing purposes; for the analyses, continue to use the original data.

## Example from real life



Error bars show SEM.

## Example from real life



## Error bars show SEM.

## Hope you will use it

Thank you
For your attention


[^0]:    ***: $p<.001$

